

New Results from the Muon g-2 Experiment at BNL

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BNL AGS E821

E821 Collaboration

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g-factors and Magnetic Moments

$$\vec{\mu}_s = g_s \left(\frac{e}{2m} \right) \vec{s}$$

Dirac theory of pointlike, spin 1/2 particles $\rightarrow g_s = 2$

The anomalous magnetic moment a is defined

$$a = \frac{g_s - 2}{2}$$

Long history of fundamental physics

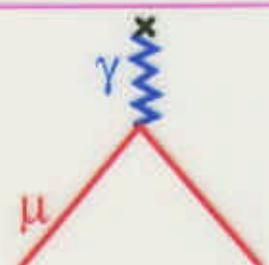
- QED calculations, precision measurements of a_e
- Baryon g-factors very different from 2
- Tests of very short distance scales: a_μ

CERN III: 7 ppm

BNL E821: 0.35 ppm

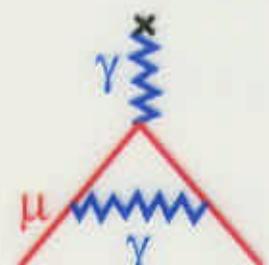
Theoretical Understanding of g-factors

Q
E
D



$$g = 2$$

+ many H.O.T.s

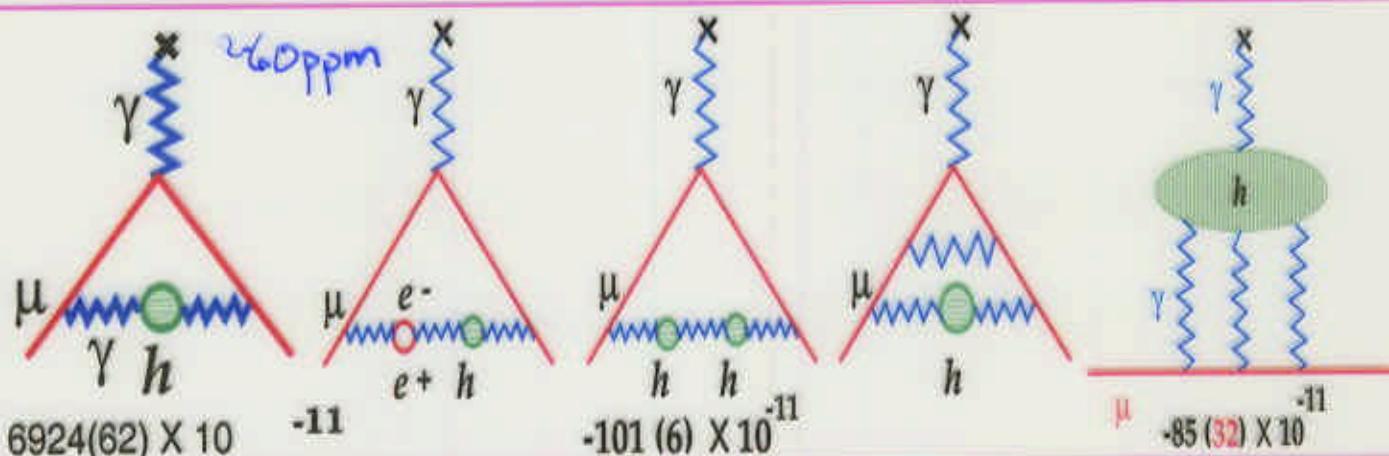


Kusch and Foley,
Schwinger, 1947

$$+ \frac{\alpha}{\pi}$$

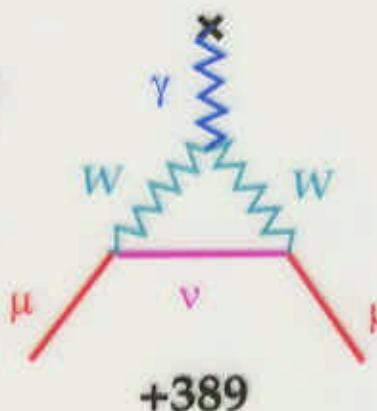
$$116\ 584\ 705.7(2) \times 10^{-11}$$

Strong



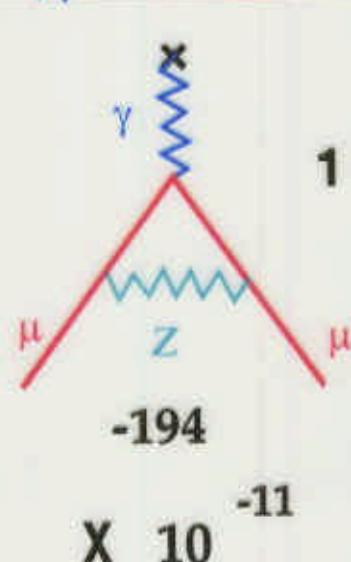
Strong error ~ 0.6 ppm

Weak

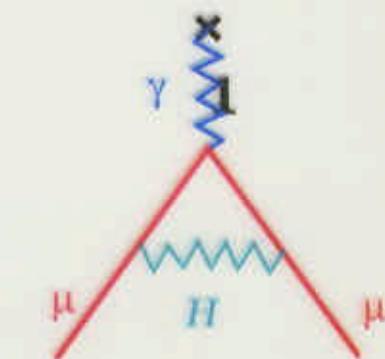


$$\times 10^{-11}$$

~ 1.3 ppm



$$\times 10^{-11}$$



$\alpha_\mu(\text{HAD})$ Scorecard

Where's the error²?



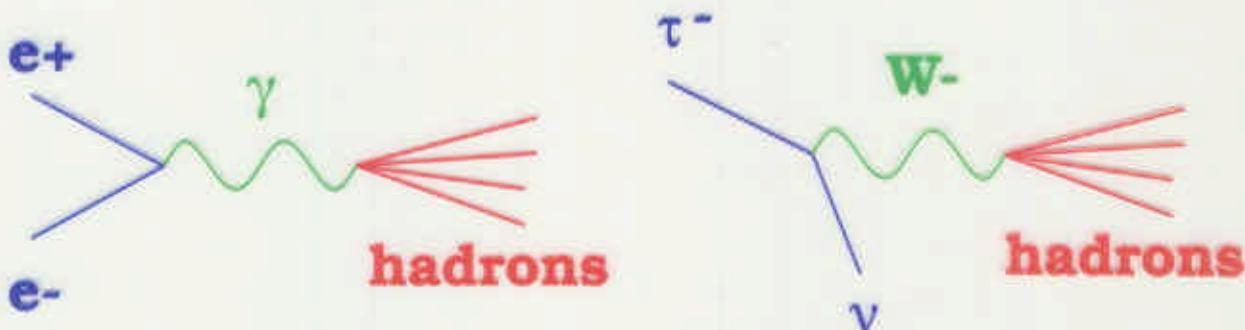
with $\tau \Rightarrow (0.5)^2$

$(0.2)^2$ $(0.3)^2$

Error² (ppm)²

$\overline{\tau} \Rightarrow (0.7)^2$
or

Tau decay data



- 1) CVC : relate $e^+ e^- \Rightarrow 2n$ pion cross sections with tau decay rate to $2n$ pions
 \Rightarrow major part of total low energy contribution (isovector piece)
- 2) Status: results more or less consistent but tau decay data is systematically higher than that from $e^+ e^-$.
 - \Rightarrow deviation largest in latest 4 pion data sets. More modest in 2 pion
 - \Rightarrow Preliminary indication: 2 pion discrepancy has not grown
 - \Rightarrow Coming soon : new analysis of full LEP tau decay data set (M. Davier)

Hadronic Vacuum Polarization

Experimental measurements of R

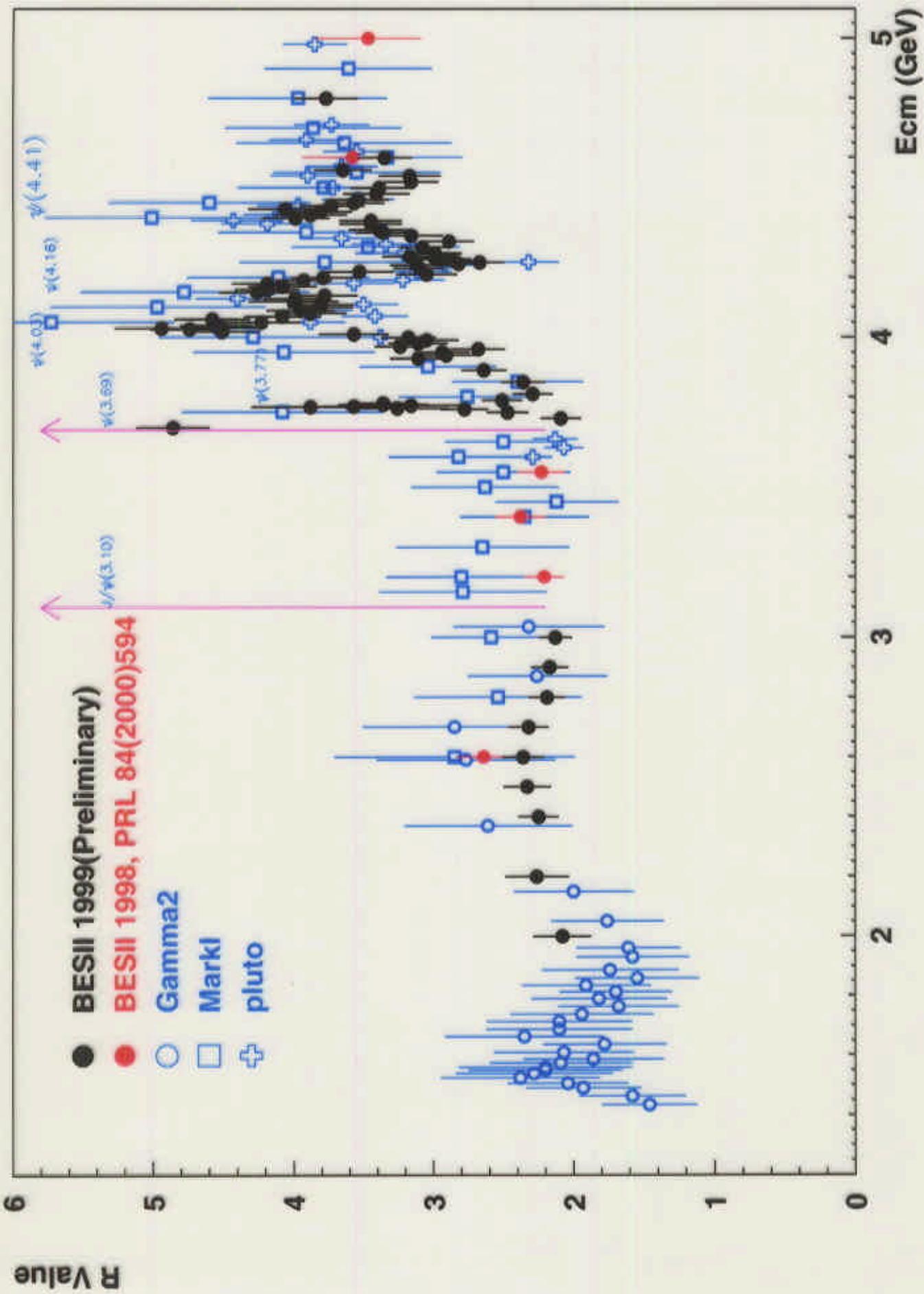
$$R(s) = \frac{\sigma_{tot}(e^+e^- \rightarrow \text{Hadrons})}{\sigma_{tot}(e^+e^- \rightarrow \mu^+\mu^-)}$$

are used as input

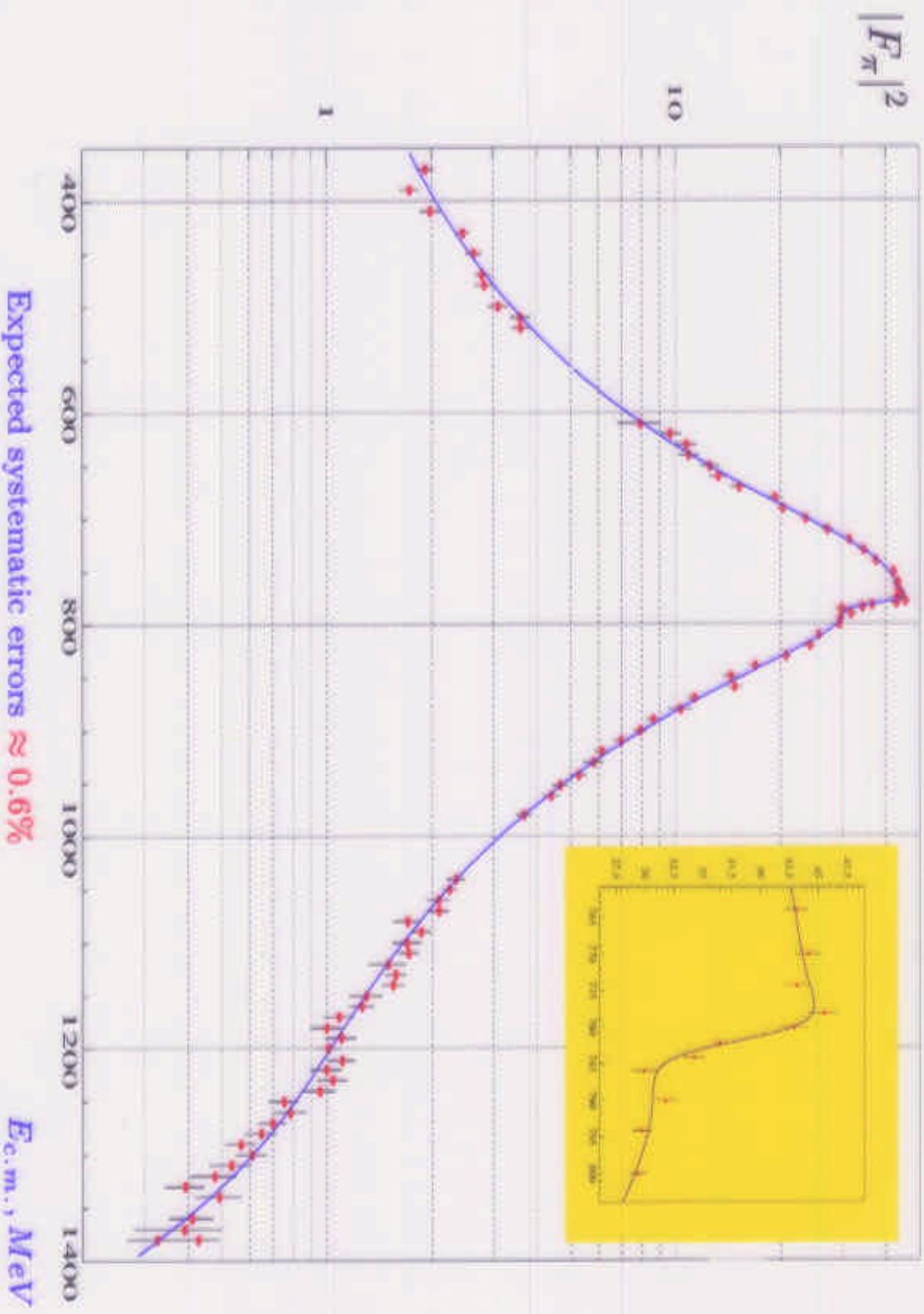
$$a_\mu(\text{Had}; 1) = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^\infty \frac{ds}{s^2} K(s) R(s)$$

Recent Developments

- Energy sweep at BES, includes 9 points from 2.0 to 3.1 GeV with 5 to 10 percent errors
→ impact on $a_\mu(\text{Had})$ TBA
- Using data from e^+e^- only, new data from CMD2 and SND ($E < 1.4$ GeV) have reduced *overall* error from 14 to 9×10^{-10} (0.8 ppm) (S. Eidelman).
- Energy, luminosity and detector upgrades are planned (VEPP2000)



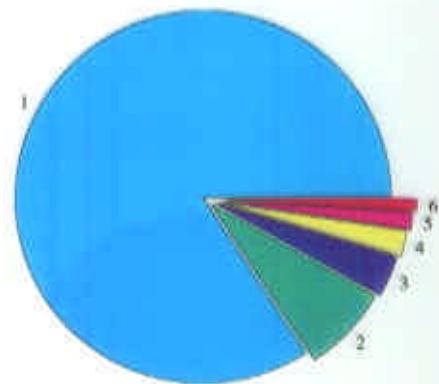
Pion formfactor study at VEPP-2M



Hadronic Contribution to Muon Anomalous Magnetic Moment from VEPP-2M Data

$$a_\mu = \frac{g-2}{2}$$

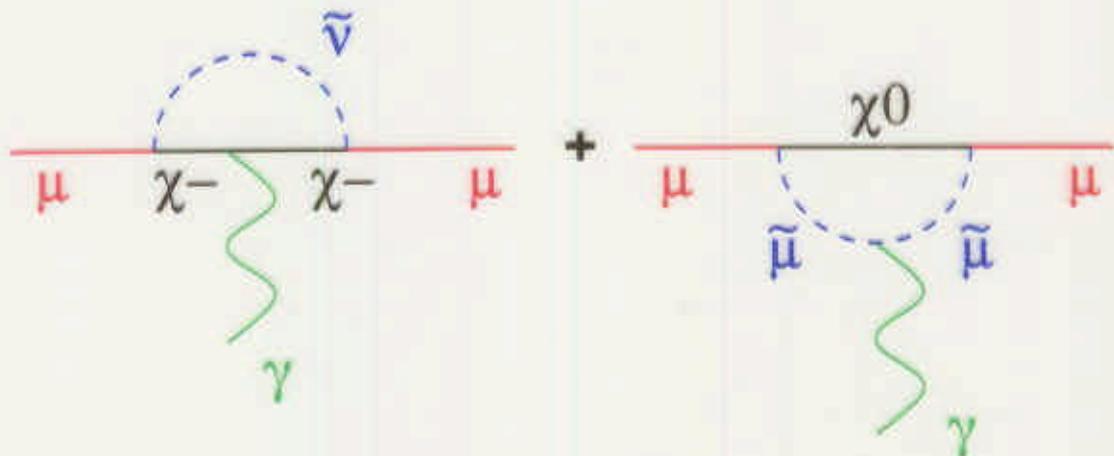
$$a_\mu^{had}(total) = 70.2 \times 10^{-9} \text{ (60.21 ppm)}$$



$$a_\mu^{had}(VEPP-2M) = 60.18 \times 10^{-9} \text{ (51.61 ppm)}$$

	Channel	Contr. ppm	Cross section error, %	Error in a_μ , ppm
1	$\pi^+ \pi^-$	43.19	0.6	0.26
2	$\pi^+ \pi^- \pi^0$	3.88	1.5	0.06
3	$K^+ K^-$	1.81	5.2	0.09
4	$K_L K_S$	1.12	1.9	0.02
5	$\pi^+ \pi^- \pi^0 \pi^0$	0.77	7	0.05
6	$\pi^+ \pi^- \pi^+ \pi^-$	0.53	7	0.04
7	$\pi^0 \gamma, \eta \gamma$	0.31	6	0.02
	Total	51.61		0.29

Supersymmetry

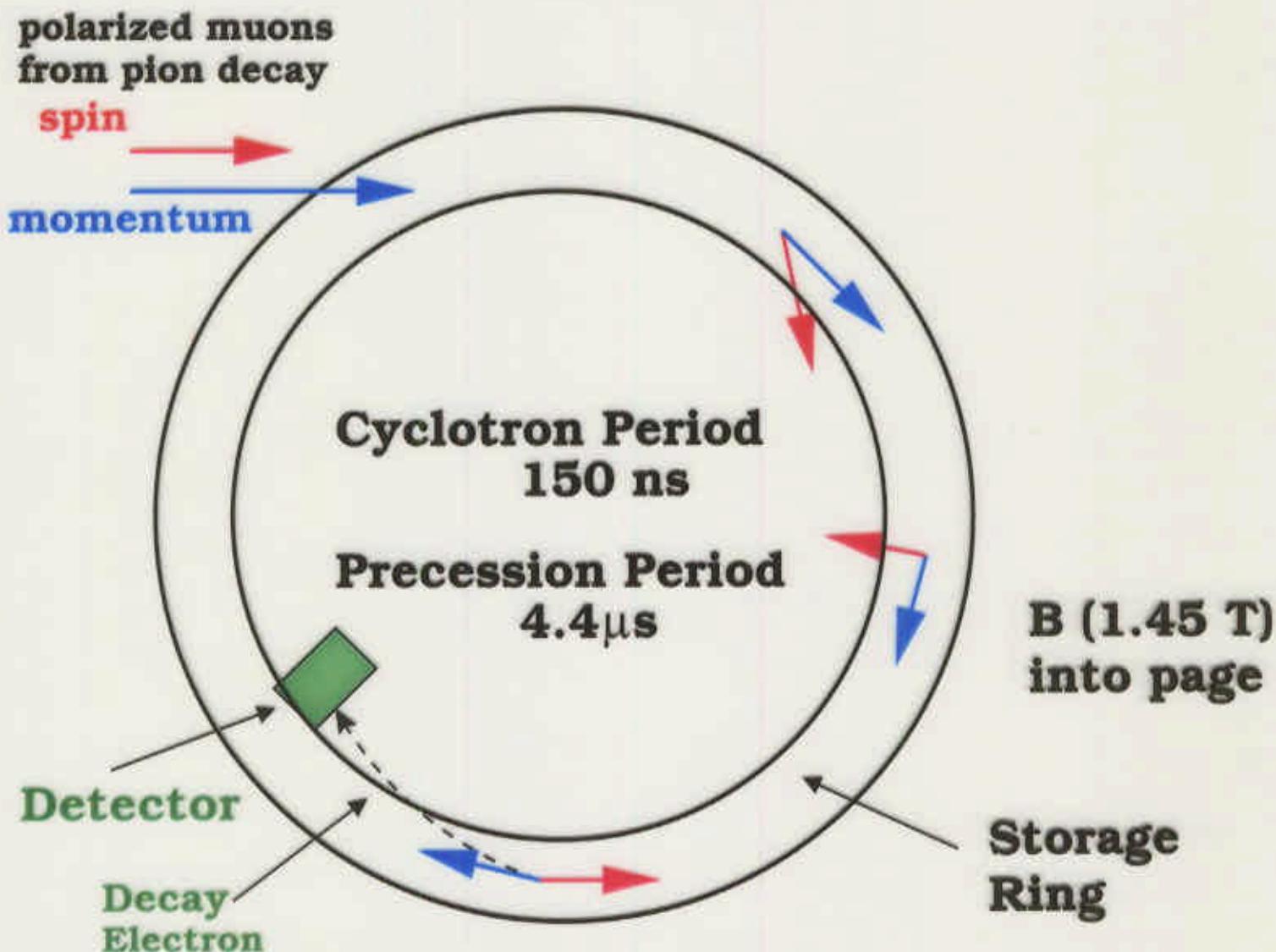


a_μ is a particularly sensitive test for SUSY models with large $\tan \beta$. In such models

$$\begin{aligned} a_\mu(\text{SUSY}) &\approx \frac{\alpha}{8\pi \sin^2 \theta_W} \frac{m_\mu^2}{\tilde{m}^2} \tan \beta \\ &\approx 140 \times 10^{-11} \left(\frac{100 \text{ GeV}}{\tilde{m}} \right)^2 \tan \beta \end{aligned}$$

: nominal electroweak effect scaled by $\tan \beta$ and relative mass squared

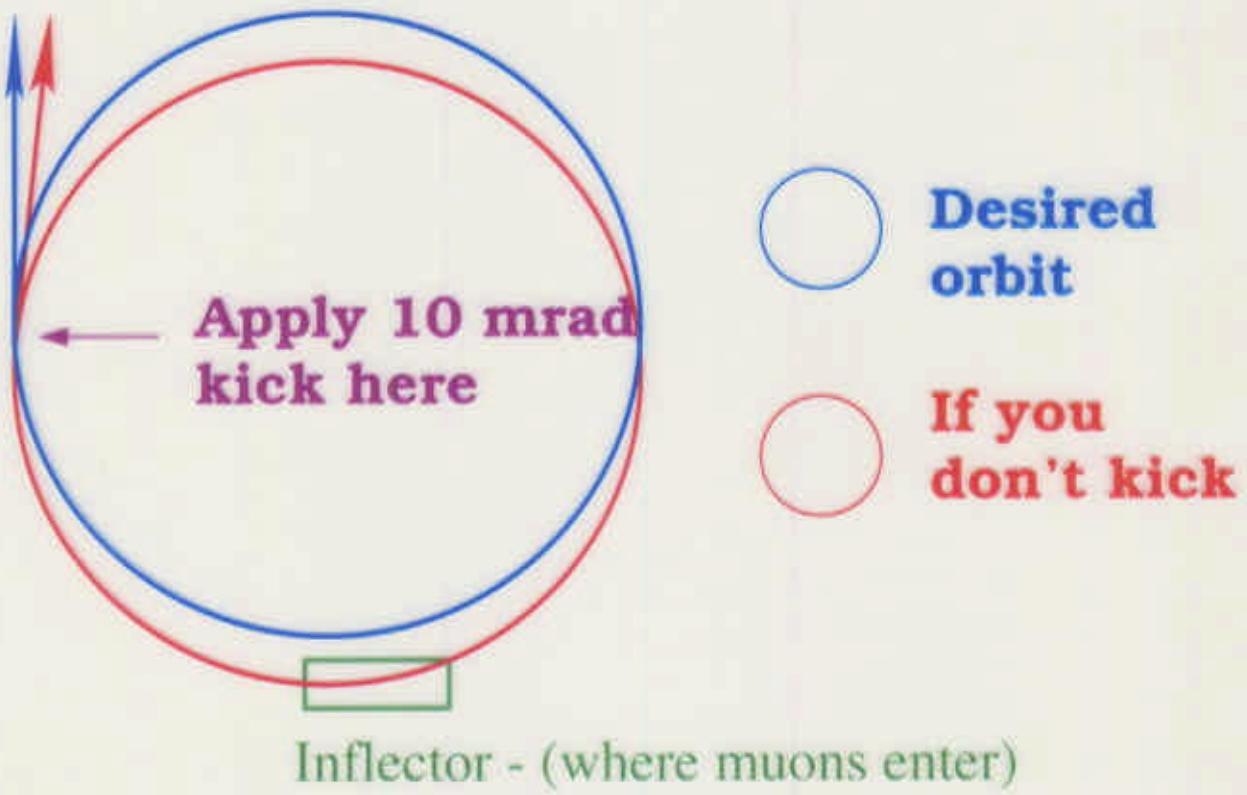
Muon Spin Precession in a Circular Orbit (exaggerated 30x)



ω_a is the time rate of change, in the lab, of the angle between the spin and momentum vectors.

{ Cyclotron motion
Larmor precession
Thomas precession

$$\omega_a = \frac{eB}{m}$$



- 1) More stored muons than pion injection**
- 2) Much less injection-related background**

The Magic Gamma

With a focusing electric field, the equation for spin rotation becomes

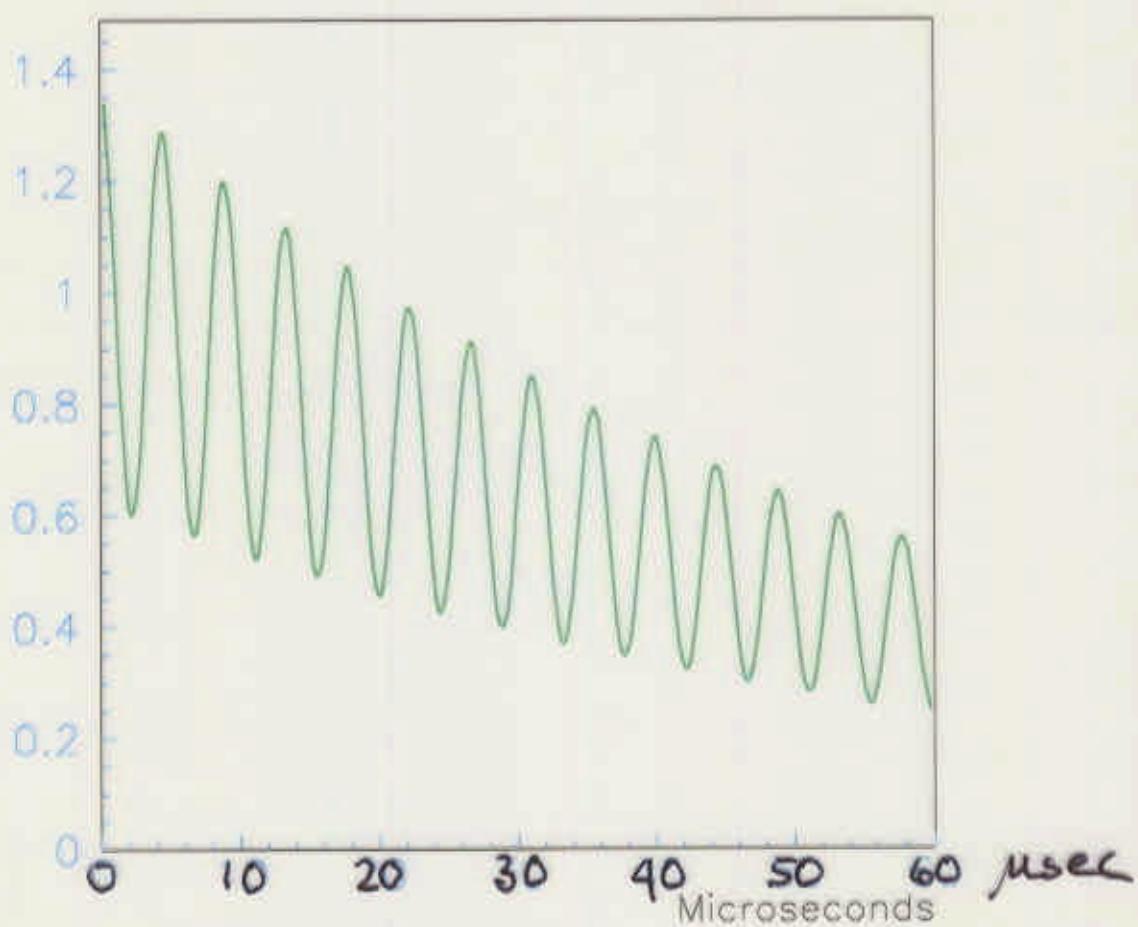
$$\vec{\omega}_a = \frac{e}{mc} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

For the **magic γ**

$$\gamma^2 = 1 + 1/a_\mu \quad E \approx 3.1 \text{ GeV}$$

the **second term** does not affect ω_a .

g-2 time spectrum



$$N(t) = N_0 e^{-t/\tau} \left[1 + A \cos(\omega_a t + \phi) \right]$$

where

- τ : dilated muon lifetime $\approx 64.4 \mu\text{sec}$
- ω_a : g-2 precession frequency $\approx 1.44 \text{ MHz}$
- A : asymmetry parameter

The statistical significance of the measurement goes as $(N_0 A^2)^{\frac{1}{2}}$

Magnetic Field

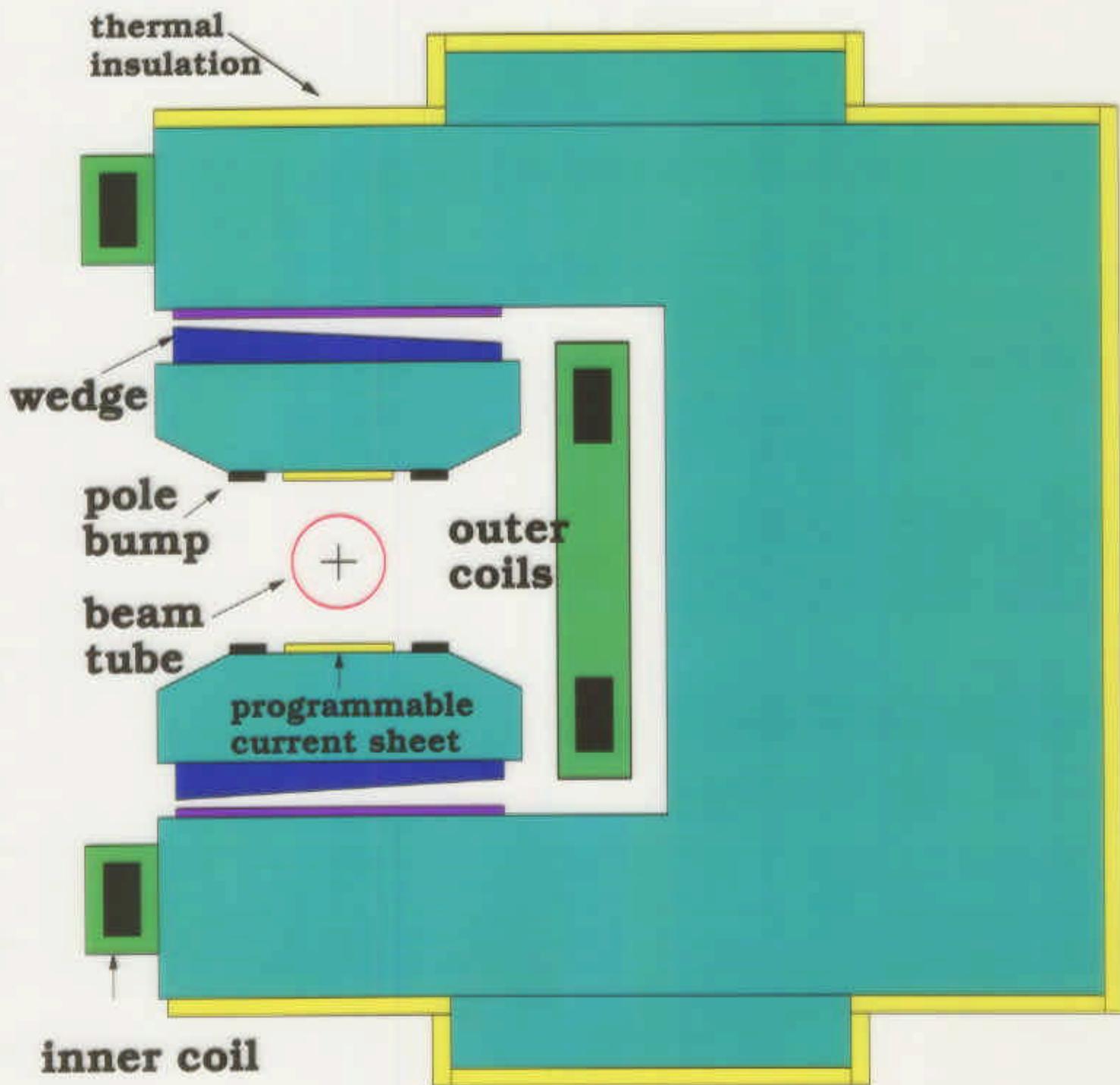
Error goal : 0.1 ppm

- => Map field periodically with NMR probes on trolley
- => Track B with 366 fixed NMR probes
- => Calibrate measurement probes to standard probe
- => Weight B-field by muon distribution

$$\omega_a = a_\mu \frac{eB}{m}$$

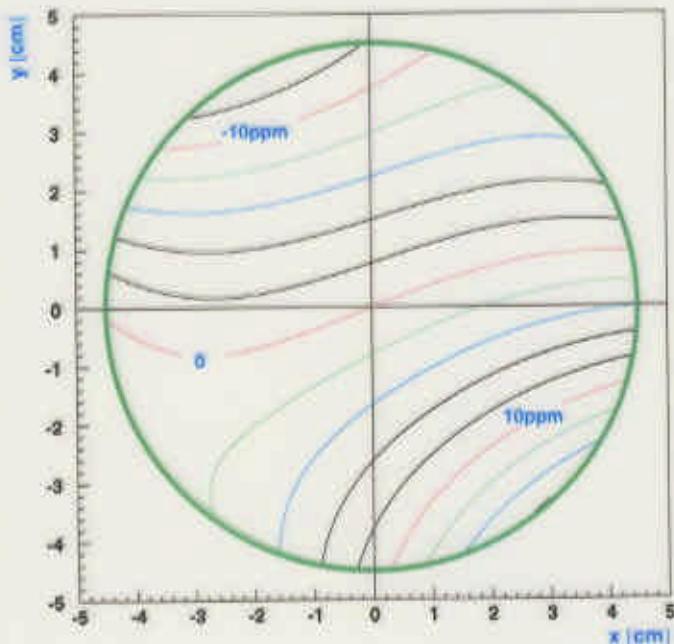
geometric averaged over
average muons

Year	ΔB (ppm)	$\Delta \langle B \rangle$ (ppm)
1997	25	0.9
1998	4	0.5
1999	4	0.4 (est.)
2000	<2	

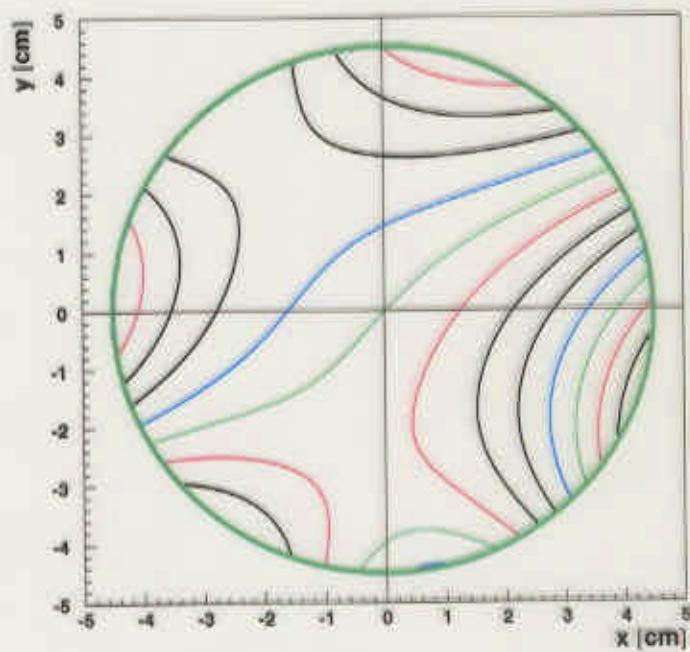


g-2 Magnet in Cross Section

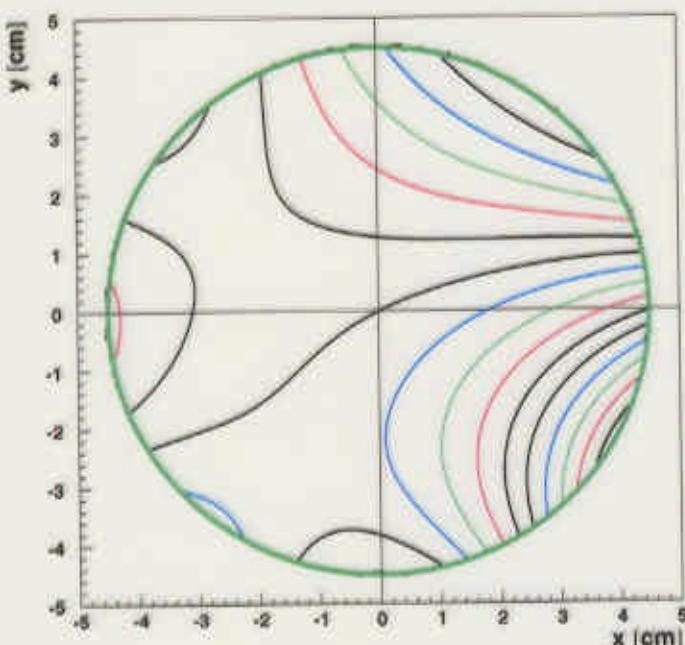
Magnetic Field Uniformity (Azimuthal Average, 1 ppm contours, except '97)



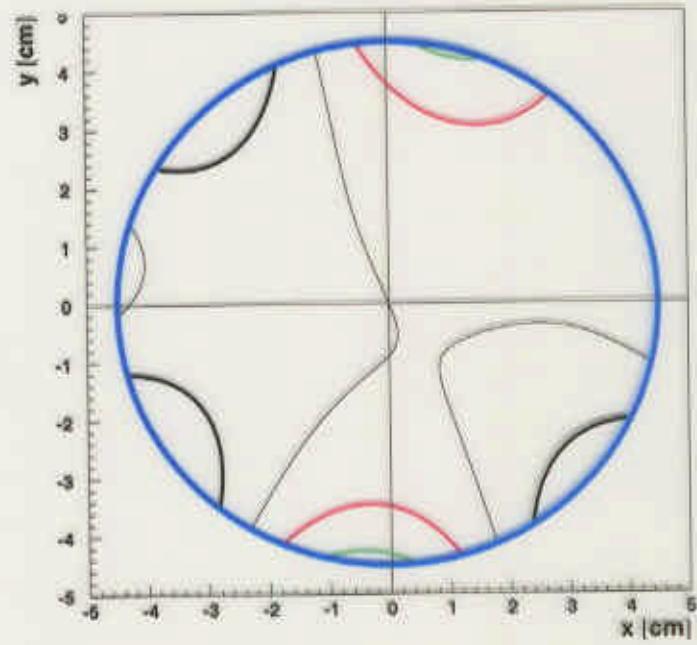
1997 run



1998 run

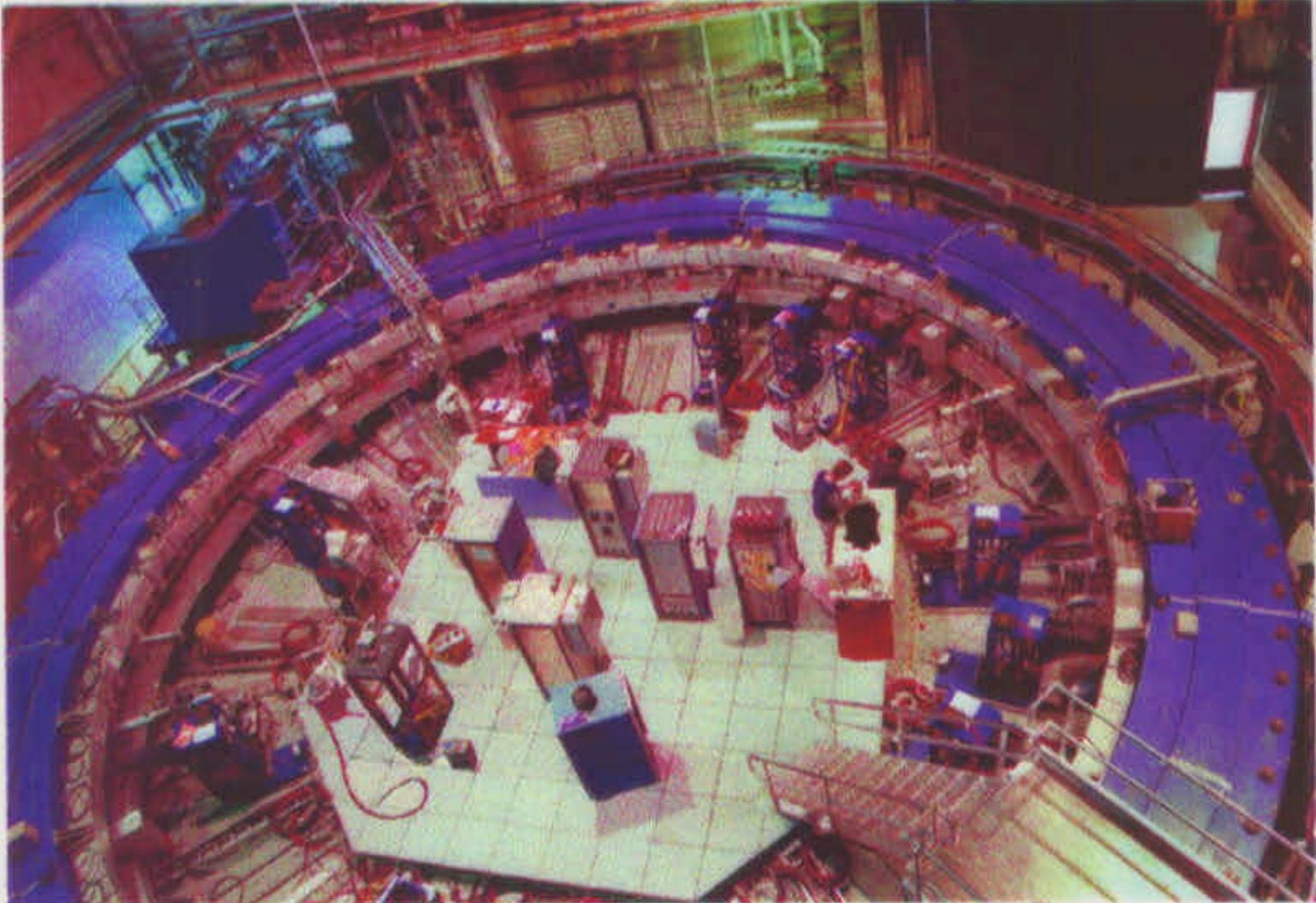


1999 run



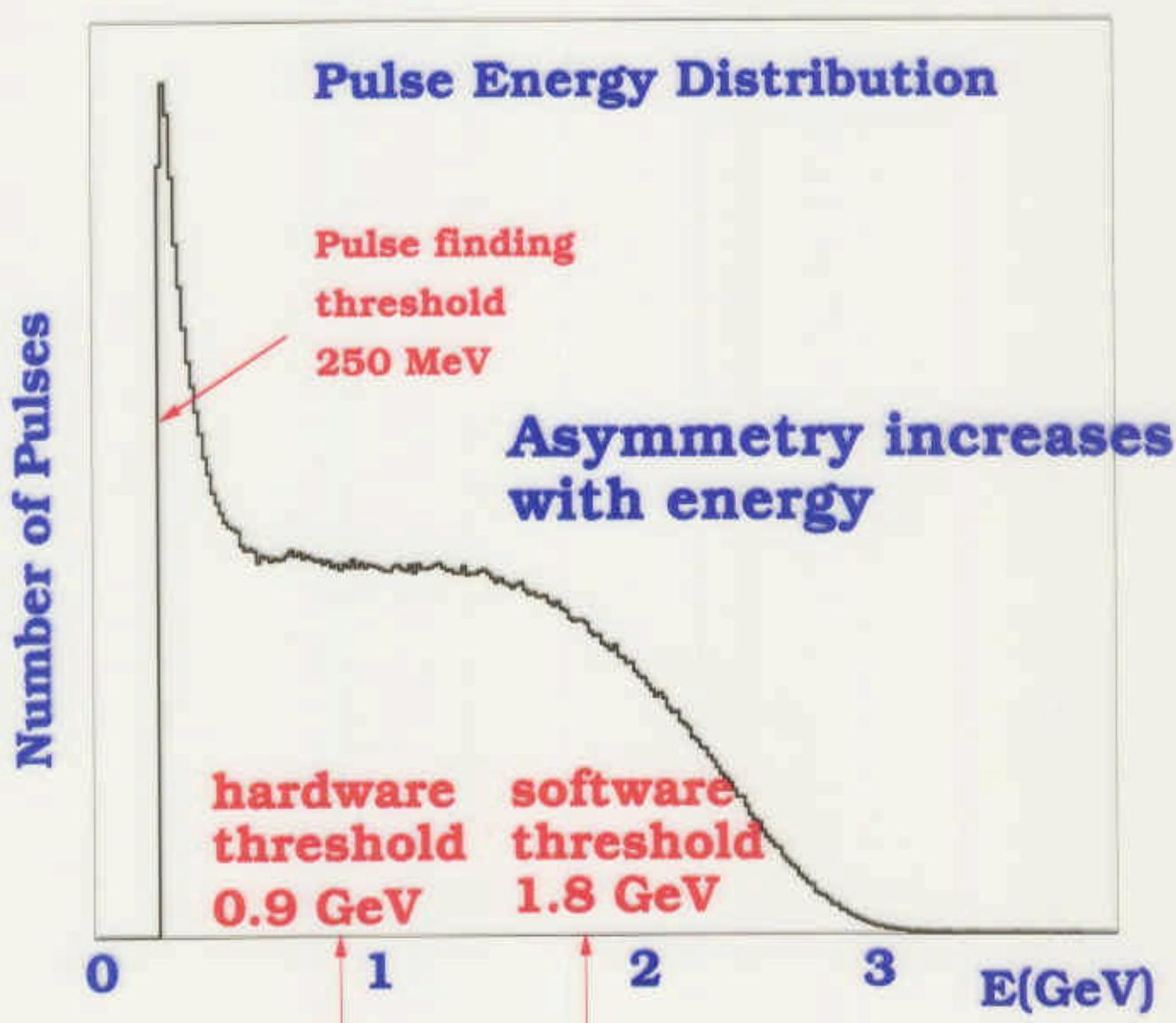
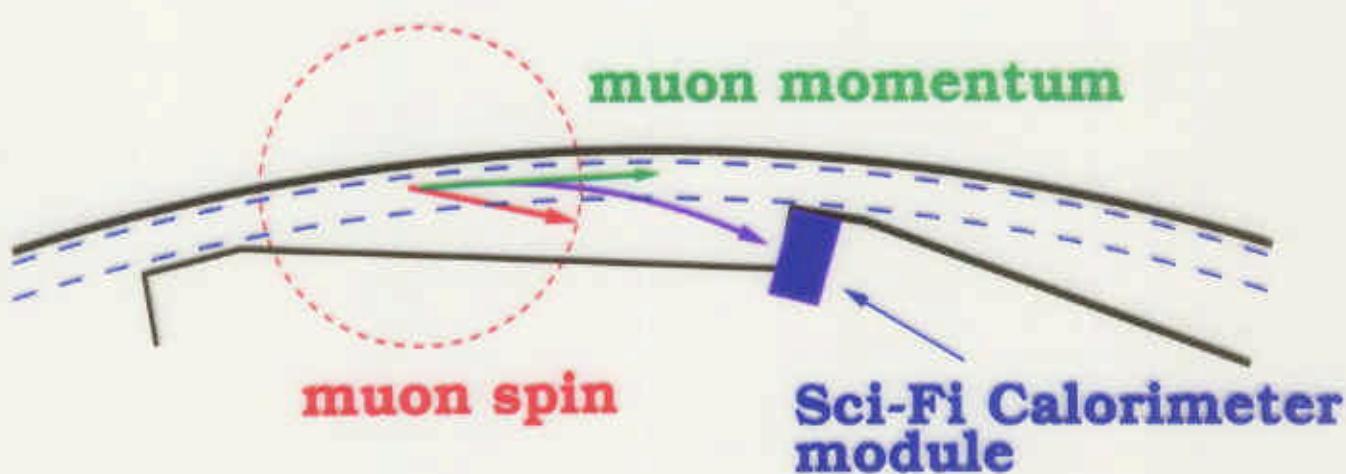
2000 run

Brookhaven E821 Muon Storage Ring

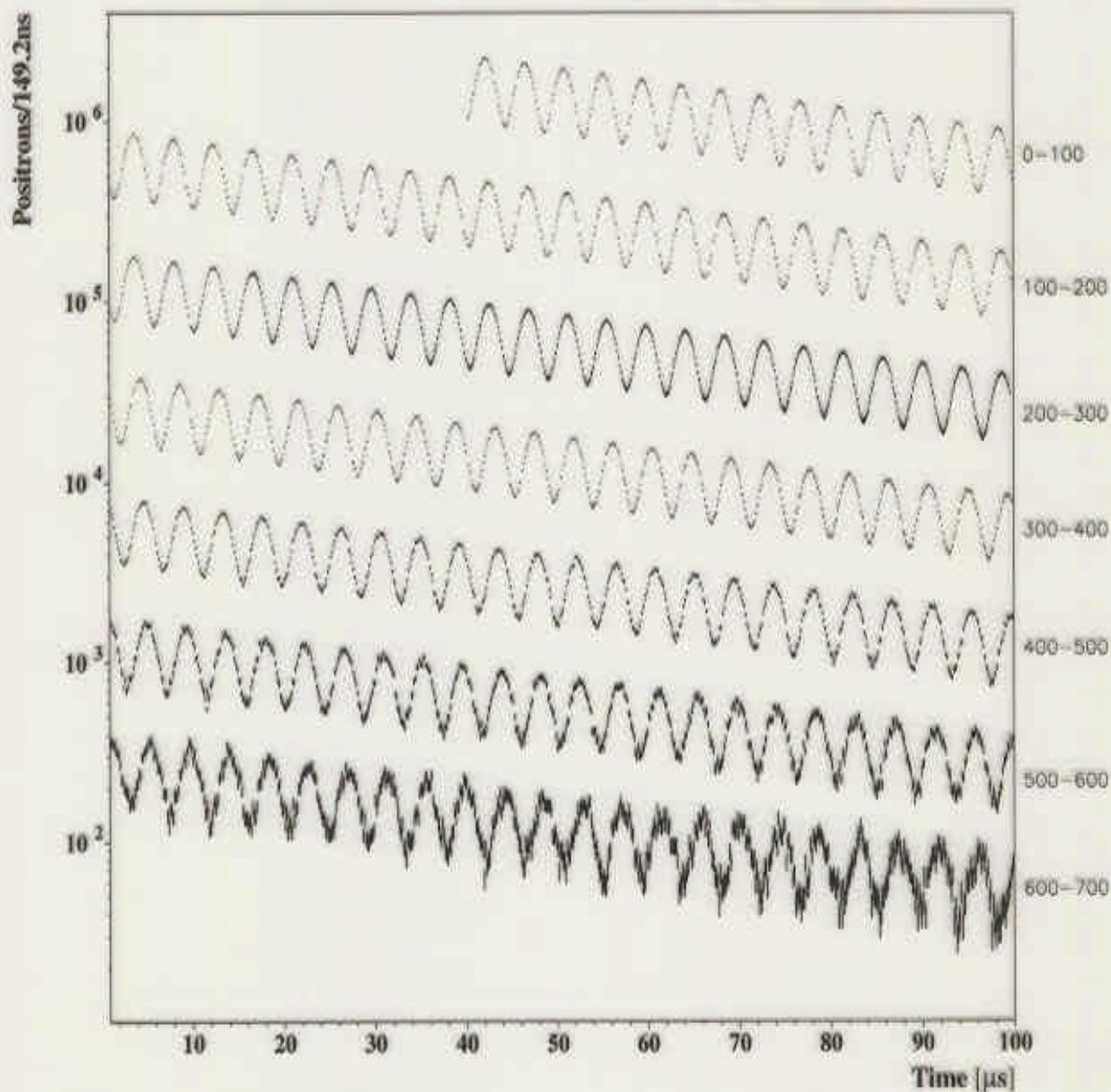


<u>Parameter</u>	<u>Value</u>	<u>Comments</u>
(g-2) Frequency	$f_a \sim 0.23 \times 10^6 / \text{s}$	$\omega_a = 2\pi f_a$ $\tau_a = 4.37 \mu\text{s}$
Muon Lifetime	$\gamma\tau = 64.4 \mu\text{s}$	
Muon kinematics	$p_\mu = 3.094 \text{ GeV/c}$	
Cyclotron Period	$\gamma_\mu = 29.3$	
Central Radius	$\tau_{cyc} = 149 \text{ ns}$	
Magnetic Field	$\rho = 7112 \text{ mm}$	(280'')
Storage Aperture	$B = 1.451 \text{ T}$	
In one lifetime:	9.0 cm circle	
	432 revolutions around ring	
	14.7 (g-2) periods	

The Anomalous Precession



A Sample of 1999 data

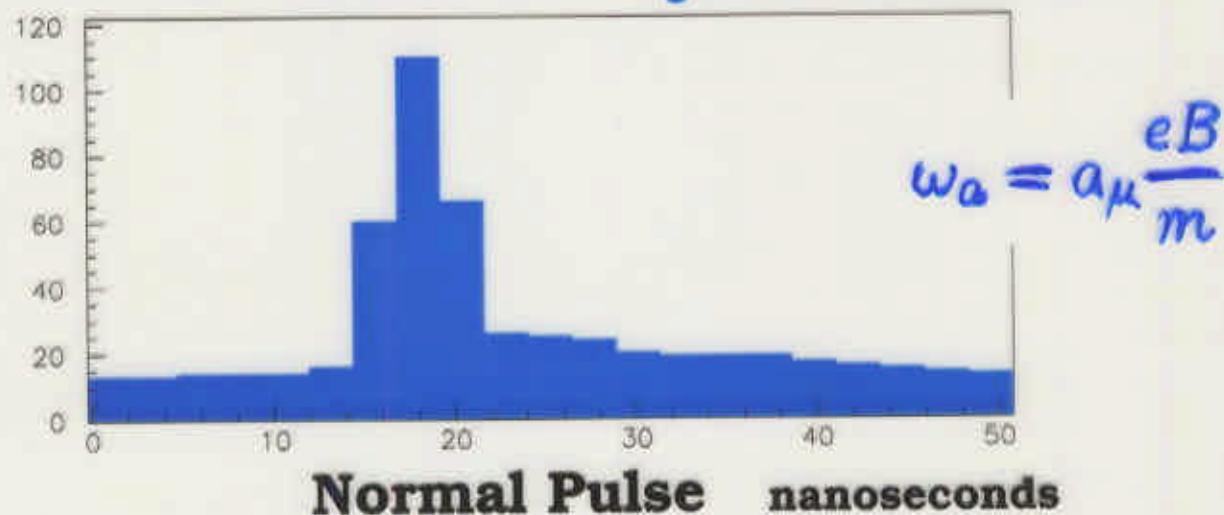


~ 750 Million Positrons

$$\text{Fit to } N(t) = \underline{N_0} e^{-t/\tau} (1 + \underline{A} \cos(\underline{\omega t} + \underline{\phi}))$$

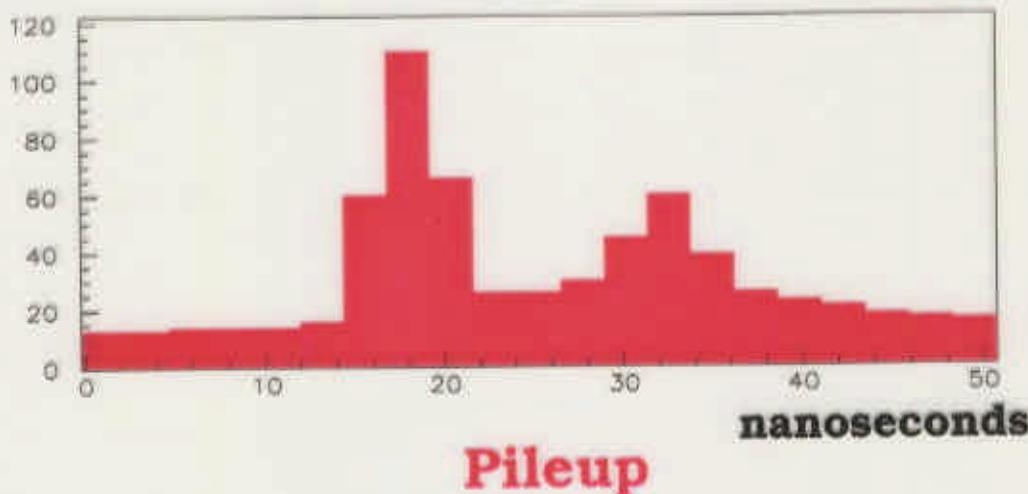
Wa error goal : 0.1 ppm

Detector Systematics



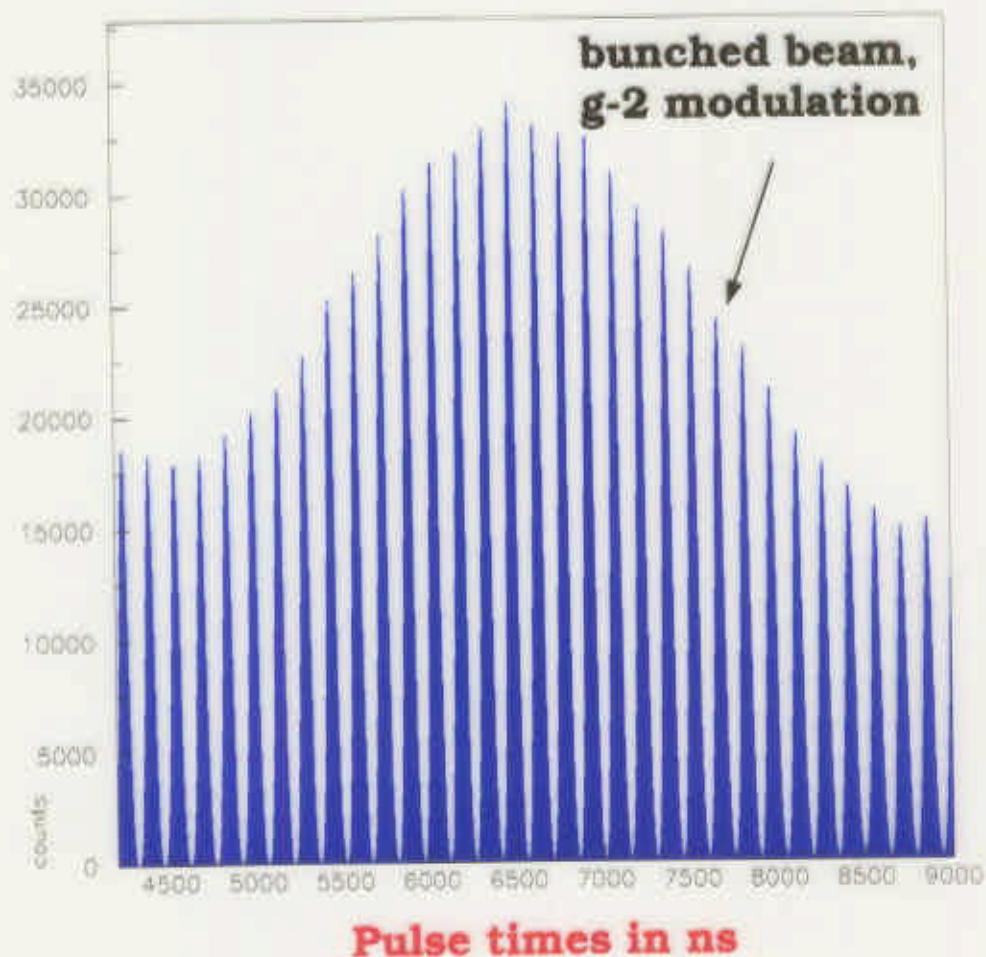
- average time pickoff stable to 20 ps
- average gain stable to 0.2%

over the first 200 μ seconds of data taking cycle



- small pulses disappear behind large ones
 - two smaller pulses combine to form a larger one
- => correction required, dominant systematic error in 1998 (0.6 ppm)

Beam Dynamics

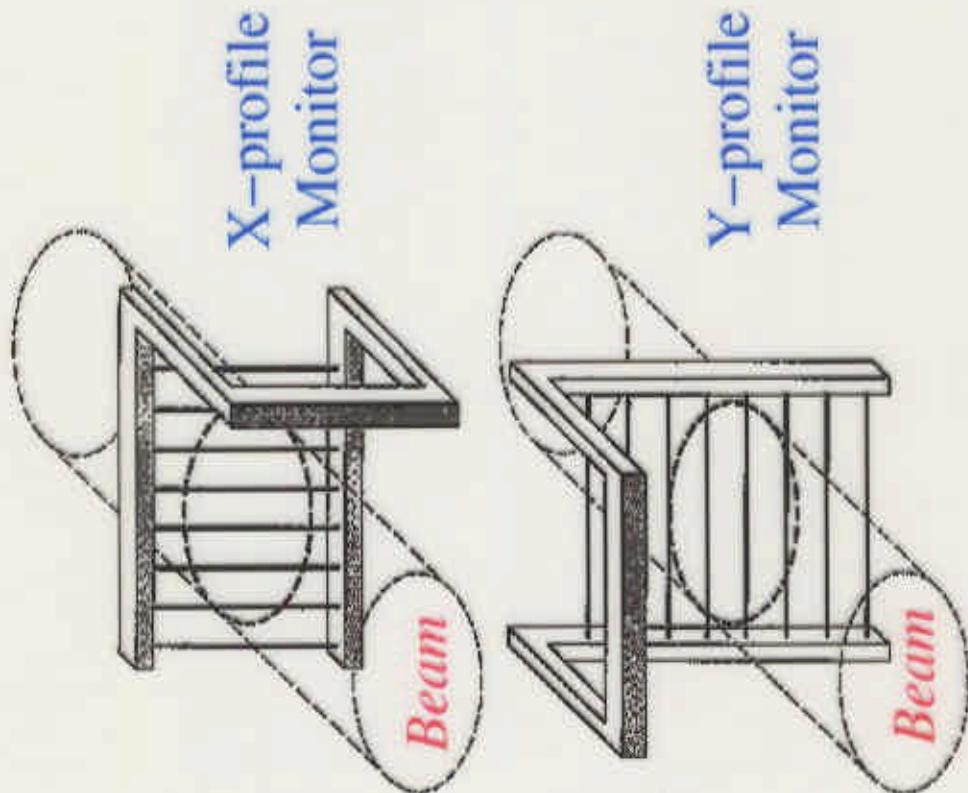


Bunching of beam at early times and debunching

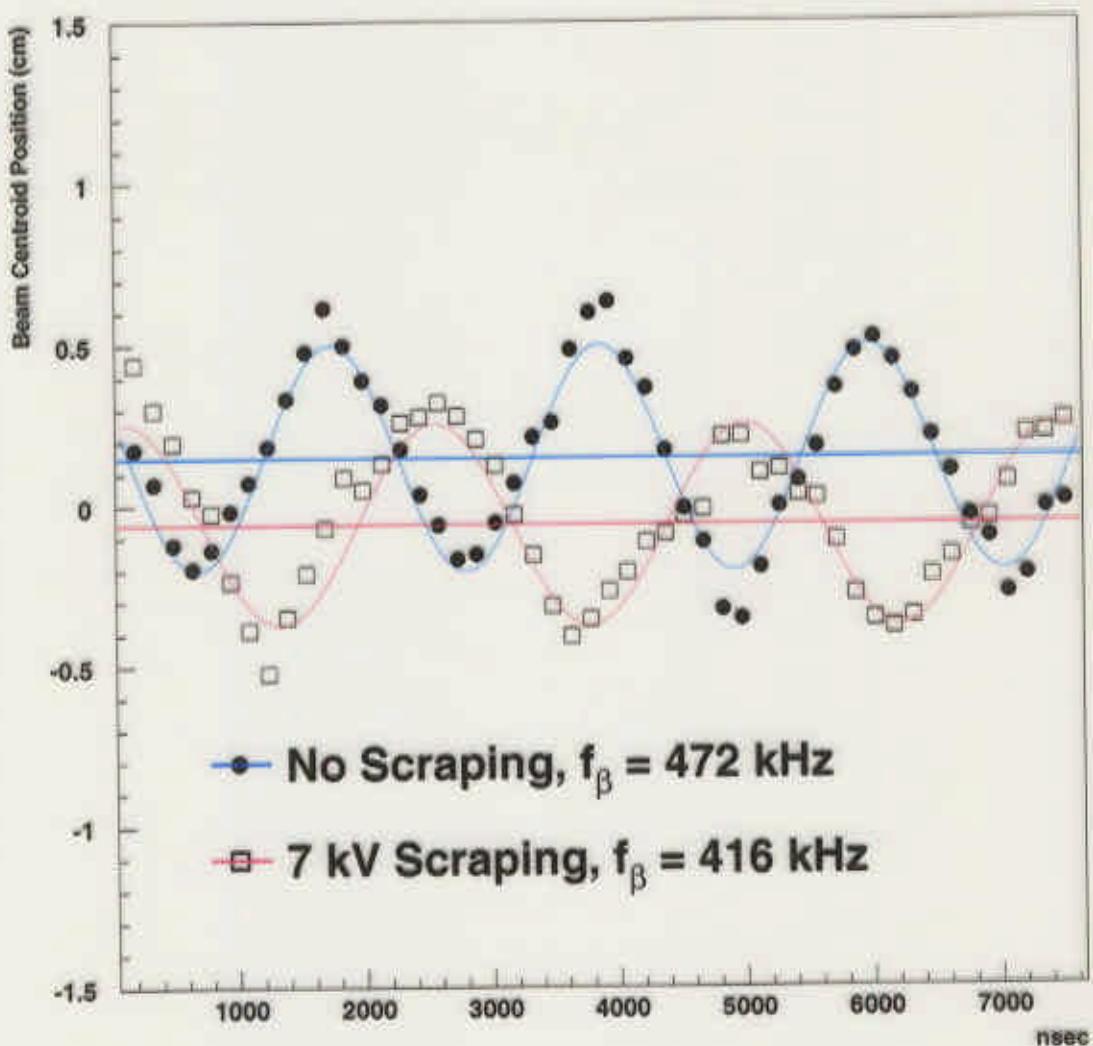
- 1) are used to determine momentum distribution of stored muons
- 2) must be accounted for in fitting the anomalous precession frequency

Scintillating Fiber Beam Monitor

- Measure radial and vertical profiles of muon beam on a turn-by-turn basis
- Two locations in the storage ring: 180° and 270° from injection point
- 7 fibers, 0.5 mm thick, 13 mm spacing
- Destructive measurement \Rightarrow remotely controlled pneumatic operation for insertion into beam



Coherent Betatron Oscillations



- Average radial beam position oscillates with an amplitude of $\sim 0.4 \text{ mm cm}$
- Oscillation frequency $\sim 2 \omega_a$
- Variation in detector acceptance vs. radius => small modulation in count rate

Result From 1998 Running

$$a_{\mu^+} (\mu_{\text{inj}}) = 116\ 591\ 91\ (59) \times 10^{-10} \ (\pm 5 \text{ ppm})$$

Errors statistically dominated

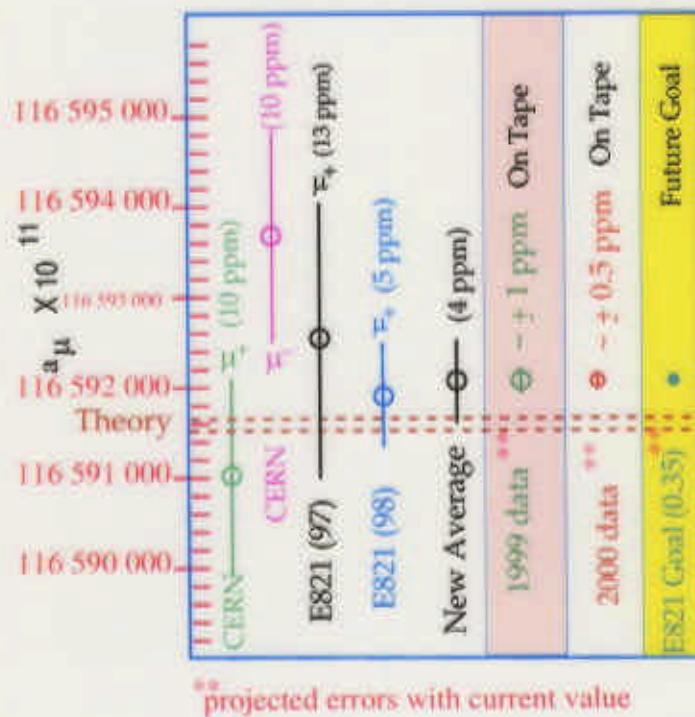
Experiment	$a_\mu \times 10^{10}$
CERN ¹ μ^+	116 591 00 (110) (9.4 ppm)
CERN ¹ μ^-	116 593 65 (120) (10 ppm)
E821 ² $\mu^+ \pi_{\text{inj}}$	116 592 51 (152) (13 ppm)
E821 $\mu^+ \mu_{\text{inj}}$	116 591 91 (59) (5 ppm)
New Average $\chi^2/\nu = 2.7/3$	116 592 05 (45) (3.9 ppm)
Theory ³	116 591 62 (8) (0.66 ppm)

¹J. Bailey et al., Nucl. Phys. B150, 1 (1979) and the PDG

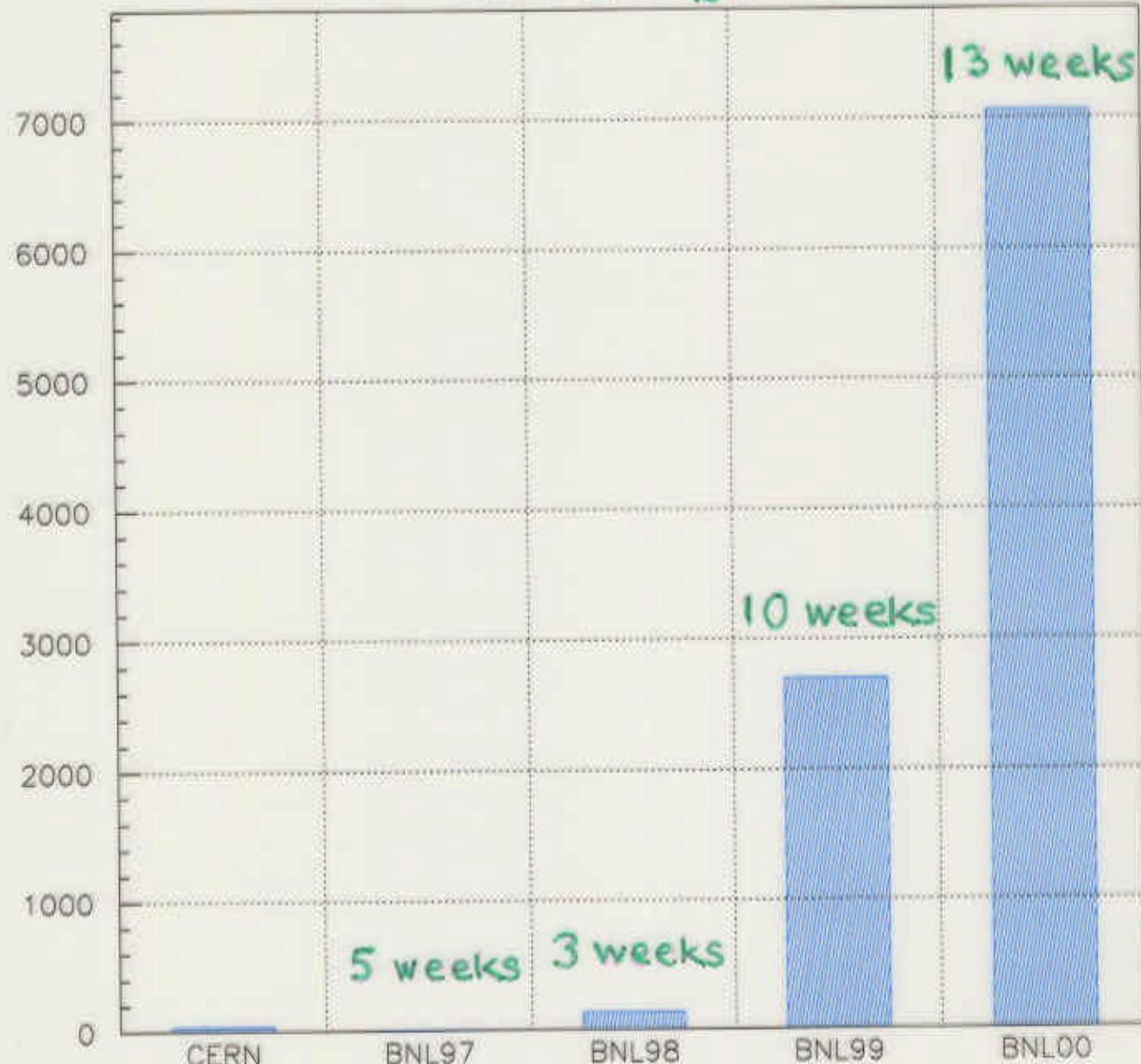
²R.M. Carey, et al., Phys. Rev. Lett. 82, 1632 (1999)

³V.W. Hughes and T. Kinoshita, Rev. Mod. Phys. 71, S133 (1999).

$$\text{Experiment} - \text{Theory} = (43 \pm 45) \times 10^{-10}$$



Millions of High Energy Positrons
and running time



Analysis time 50 weeks 40 weeks 25 weeks
(so far!)

Also: 3/4 Wa analyses complete and consistent
99 1/4 due soon

49
RUN

2 3 field analyses - a week away

Conclusions

- 1) Our newly submitted, 5ppm measurement of the muon anomalous magnetic moment is consistent with previous results and with the standard model.**
- 2) The analysis of our 1999 data will be complete early this fall. A 1.5 ppm error (statistical) is expected. Production of the 2000 data has already begun. Together, the 1999 and 2000 data sets will provide a statistical precision of about 0.6 ppm.**
- 3) Our next run, with negative muons, is scheduled to start in February, 2001.**
- 4) Steady progress on the hadronic correction continues thanks to the efforts at BES, CMD2, SND, ALEPH and CLEO. More work is needed to resolve the differences between tau decay and e+e- data at low energy.**