

# Lepton Transmutation from a Rotating Mass Matrix

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+ Chen + Bordes hep-ph/0006338  
+ Chen + Bordes + Fairbairn hep-ph/0007004

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Rotating mass matrix

= mass matrix undergoes unitary transformations  
through scale changes

## Standard Model (SM)

$$\frac{dL}{dt} = \frac{3}{128\pi^2} \frac{1}{246^2} \underbrace{(ULU^\dagger)}_N \underbrace{(ULU^\dagger)^\dagger}_{N^\dagger}$$

(linearized rotating part)

where  $U$  is non-diagonal MNS mixing matrix.

## Dualized Standard Model (DSM)

$$m = m_T \begin{pmatrix} x \\ y \\ z \end{pmatrix} (x, y, z)$$

$$\frac{d}{dt} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \frac{5}{32\pi^2} \rho^2 \begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix}$$

- ICHEP 98
- +Chau, PRD 57 (1998) 2507, hep-ph/9701120 .....  
+Bordest + Chau + Faridani hep-ph/0007004

## DSM references

- Chen + Tsou, hep-th/9701120, PRD 57 (1998) 2077
- Chen + Tsou, hep-th/9702117, PRD 56 (1997) 3646
- Bordes + Chen + Faudot + Pfeudler + Tsou  
hep-ph/9707031, Astropart. Phys. 8 (1998) 135
- Bordes + Chen + Faudot + Pfeudler + Tsou  
hep-ph/9712276, PRD 58 (1998) 013004
- Bordes + Chen + Pfaudler + Tsou  
hep-ph/9802420, PRD 58 (1998) 053003
- Bordes + Chen + Pfaudler + Tsou  
hep-ph/9802436, PRD 58 (1998) 053006
- Bordes + Chen + Faudot + Pfaudler + Tsou  
hep-ph/9807277, PRD 60 (1999) 013005
- Bordes + Chen + Tsou, hep-ph/9901440, Eur. Phys. J. C10 (1999) 63
- Bordes + Chen + Gallego + Tsou  
hep-ph/9909321, PRD 61 (2000) 00077702
- Bordes + Chen + Tsou hep-ph/0006338
- Bordes + Chen + Faudot + Tsou hep-ph/0007004

## Mass matrix rotation

SM depends on mixing matrix  $U$

E.g. take  $U$  bimaximal

(GeV per decade change in energy)

$\langle \mu | \tau \rangle$  changes by  $\sim 5.5 \times 10^{-3}$

$\langle e | \tau \rangle$  changes by  $\sim 1.8 \times 10^{-7}$

$\langle e | \mu \rangle$  changes by  $\sim 1.1 \times 10^{-8}$

DSM explicit calculations

+ Brooks + Chan hep-ph/9901440  
Eur. Phys. J. C10 (1999) 63

~~free~~  
3 parameters determined by fitting experimental

mass & mixing parameters

( $\rightsquigarrow$  sensible predictions for remaining parameters)

$\rightsquigarrow$  present calculations entirely parameter-free

<i>Quantity</i>	<i>ExperimentalRange</i>	<i>PredictedCentralValue</i>	<i>PredictedRange</i>
$ V_{ud} $	0.9745 – 0.9760	0.9753	0.9745 – 0.9762
$ V_{us} $	0.217 – 0.224	(0.2207)	<i>input</i>
$ V_{ub} $	0.0018 – 0.0045	0.0045	0.0043 – 0.0046
$ V_{cd} $	0.217 – 0.224	(0.2204)	<i>input</i>
$ V_{cs} $	0.9737 – 0.9753	0.9745	0.9733 – 0.9756
$ V_{cb} $	0.036 – 0.042	0.0426	0.0354 – 0.0508
$ V_{td} $	0.004 – 0.013	0.0138	0.0120 – 0.0157
$ V_{ts} $	0.035 – 0.042	0.0406	0.0336 – 0.0486
$ V_{tb} $	0.9991 – 0.9994	0.9991	0.9988 – 0.9994
$ V_{ub}/V_{cb} $	$0.08 \pm 0.02$	0.1049	0.0859 – 0.1266
$ V_{td}/V_{ts} $	$< 0.27$	0.3391	0.3149 – 0.3668
$ V_{tb}^* V_{td} $	$0.0084 \pm 0.0018$	0.0138	0.0120 – 0.0156
$ U_{\mu 3} $	0.56 – 0.83	0.6658	0.6528 – 0.6770
$ U_{e 3} $	0.00 – 0.15	0.0678	0.0632 – 0.0730
$ U_{e 2} $	0.4 – 0.7	0.2266	0.2042 – 0.2531

Table 1: Predicted CKM matrix elements for both quarks and leptons

## Transmational decays

- $Z^0 \rightarrow \tau^- \mu^+$

$$4 \times 10^{-8}$$

$$4 \times 10^{-10}$$

$$1.2 \times 10^{-5}$$

- $\pi^0 \rightarrow \mu^- e^+$

$$3 \times 10^{-9}$$

far below

$$1.7 \times 10^{-8}$$

- $\psi \rightarrow \mu^+ \tau^-$

$$6 \times 10^{-6}$$

$$1 \times 10^{-8}$$

not given

- $\mu^- \rightarrow e^- \gamma$

$$0$$

?

$$4.9 \times 10^{-11}$$

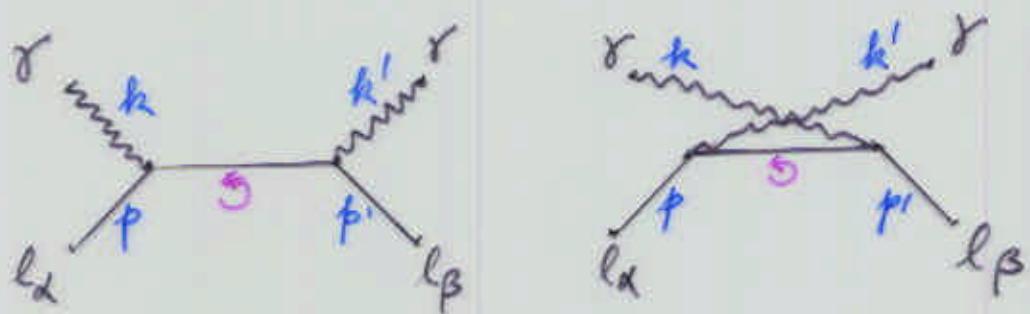
DSM

(SM)

experimental bound

## Photo-transmutation

$$\gamma + l_\alpha \rightarrow \gamma + l_\beta, \quad l_\alpha \neq l_\beta$$



## Lepton states

- must diagonalize the mass matrix
- eigenvectors depend on scale
- no canonical recipe



## Fixed scale diagonalization

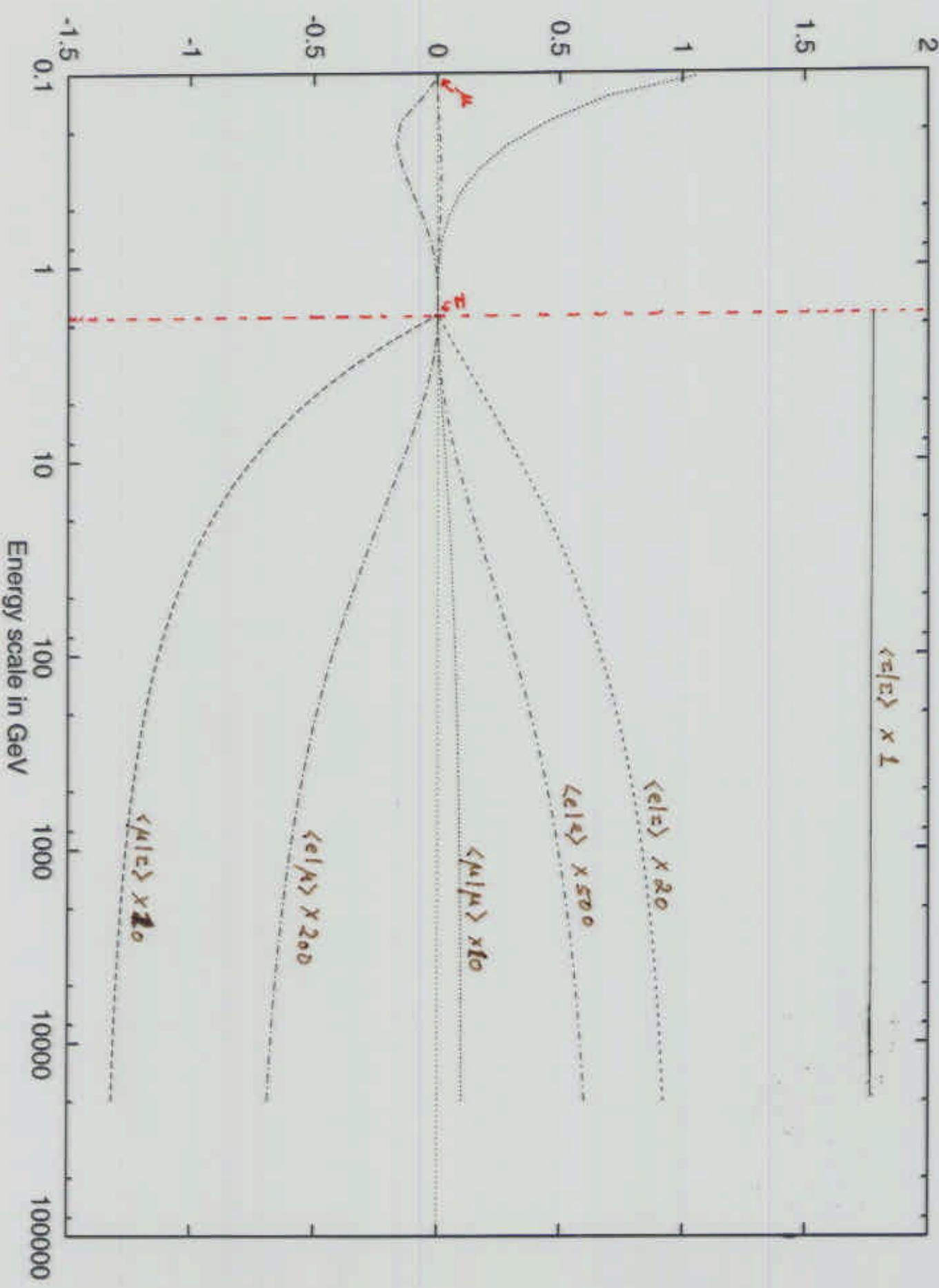
- state vectors fixed from a chosen scale
- applicable to SM

\* mass matrix diagonal only at chosen scale

## Step-by-step diagonalization

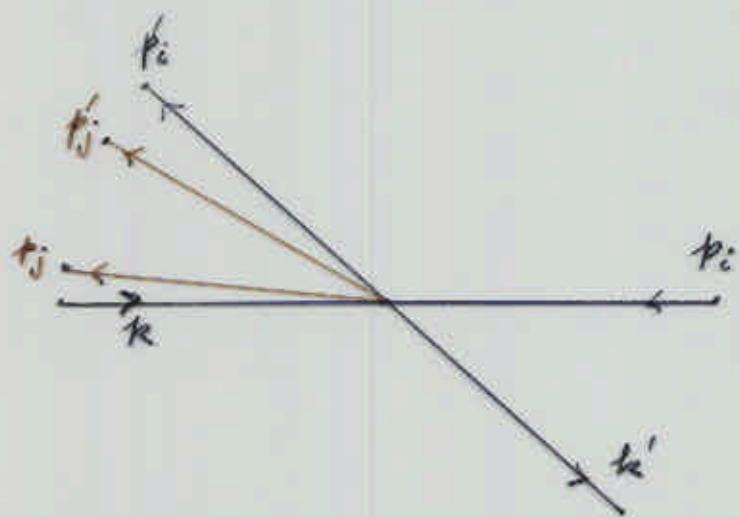
- a working criterion
  - lepton state vectors always orthogonal
  - rotation matrix always unitary
- must be used in DSM
- 3 steps:
  1. run  $m$  to scale where  $\mu = m_3(\mu)$
  2. corresponding e-vector is state vector  $v_3$
  3. do same with  $2 \times 2$  remaining submatrix

\* mass matrix diagonal at scales  $m_e, m_\mu, m_\tau$



## DSM calculations

- kinematics: unfamiliar
  - $l_\alpha$  and  $l_\beta$  lin. comb. of  $\tau, \mu, e$  states
  - how are momenta related?
  - $s, t$  as variables (*same for all channels in a given process*)
- amplitudes
  - cannot use standard  $\gamma$  traces formulae
  - individual spin, polarization
  - sum by hand



c.m. frame of channel  $i$

$$p^2 = p'^2 = m^2$$

## Comments on numerical results

### DSM

- $\gamma + e \rightarrow \gamma + \mu$        $\gamma + e \rightarrow \gamma + \tau$   
 $\gamma + \mu \xrightarrow{\text{if}} \gamma + e$        $\gamma + \mu \rightarrow \gamma + \tau$   
 (above = threshold)
- $\frac{d\sigma}{d\Omega}$  (not  $\frac{d\sigma}{du}$ )  $\rightarrow$  X-section  $\downarrow$  as  $s \uparrow$
- $s+t \sim -u$
- rotation matrix  $\rightarrow$   
 $\gamma \mu \rightarrow \gamma \tau > \gamma e \rightarrow \gamma \tau > \gamma e \rightarrow \gamma \mu$

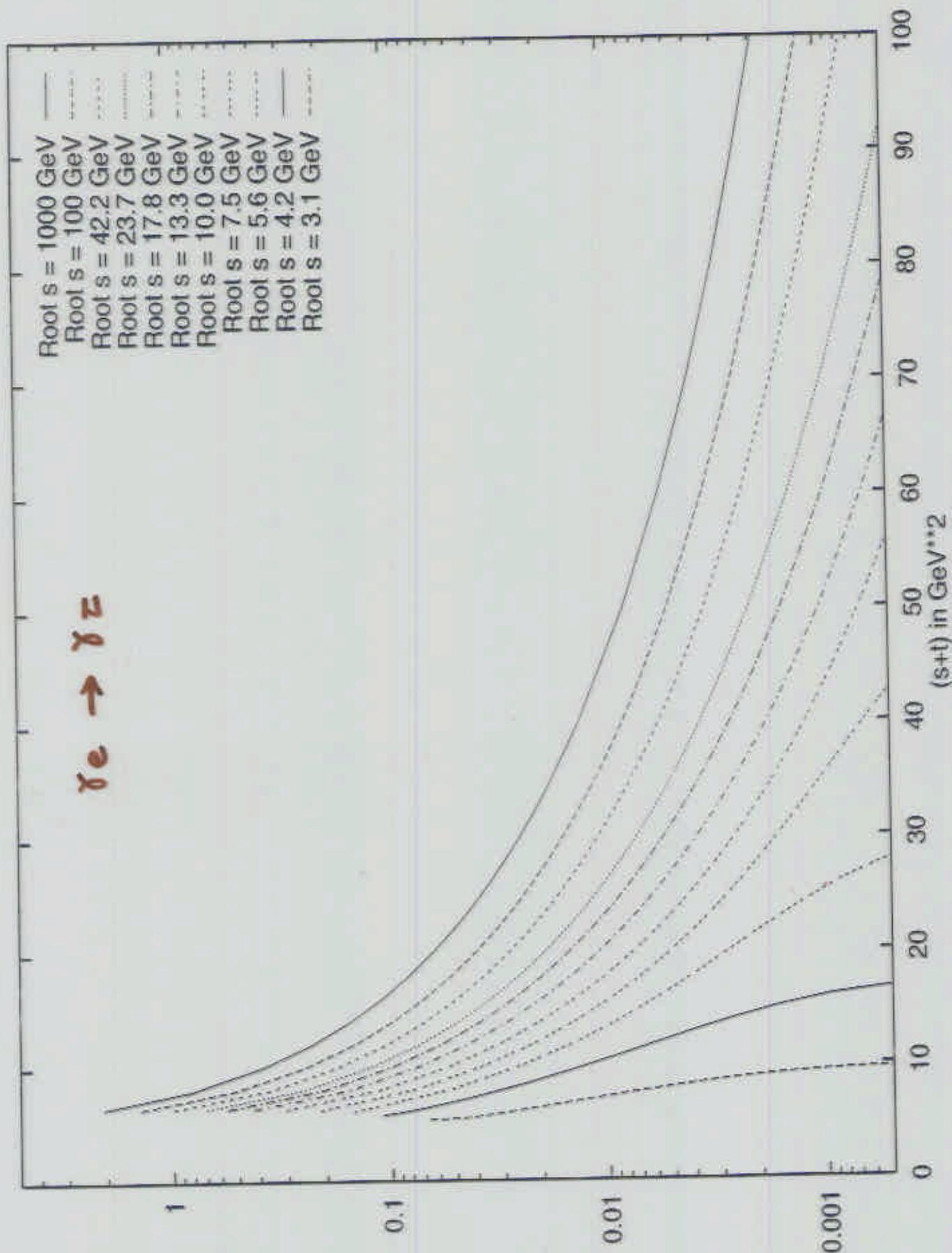
### SM with FSD

If
 

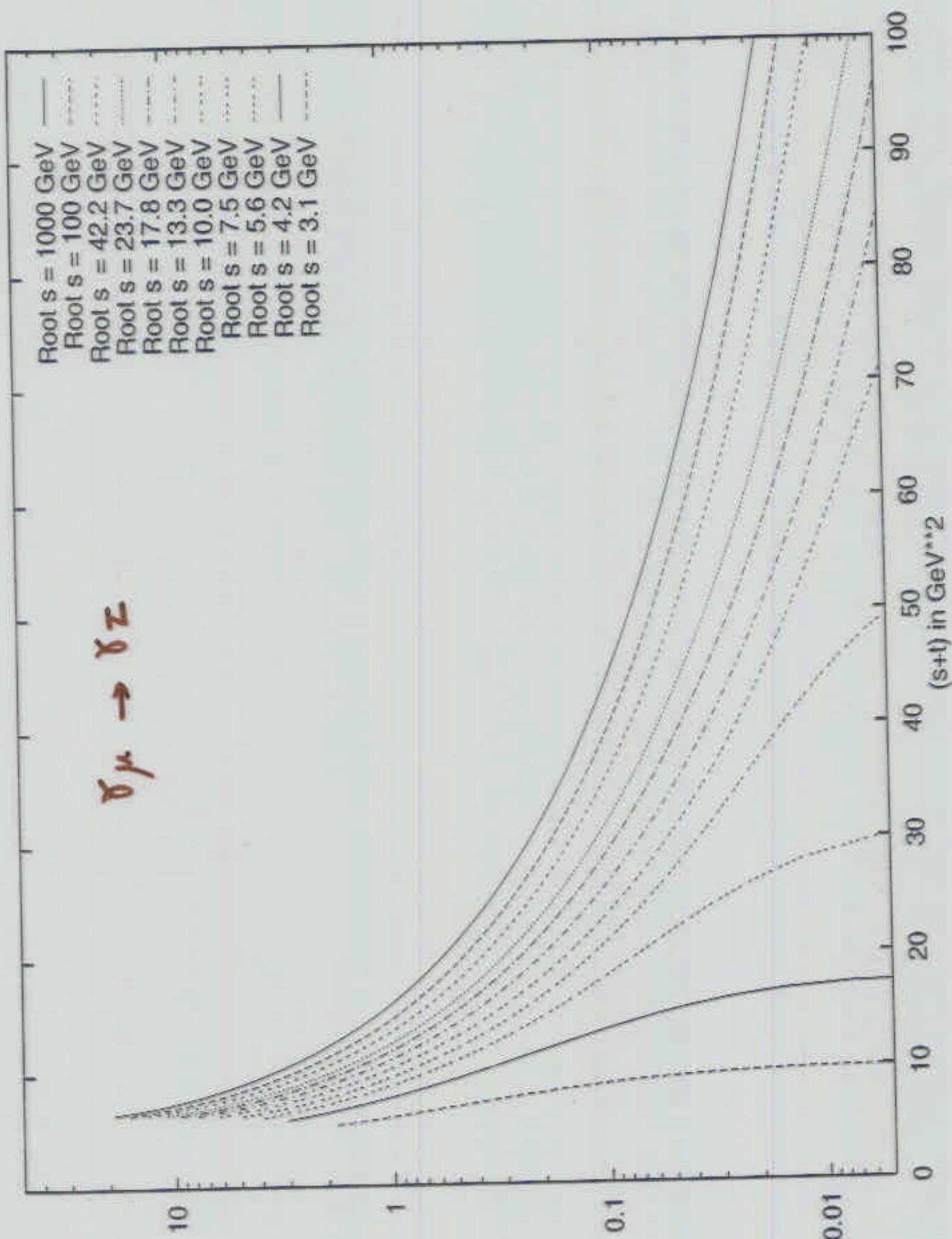
- hierarchical masses  $m_3 \gg m_2 \gg m_1$
- above = threshold

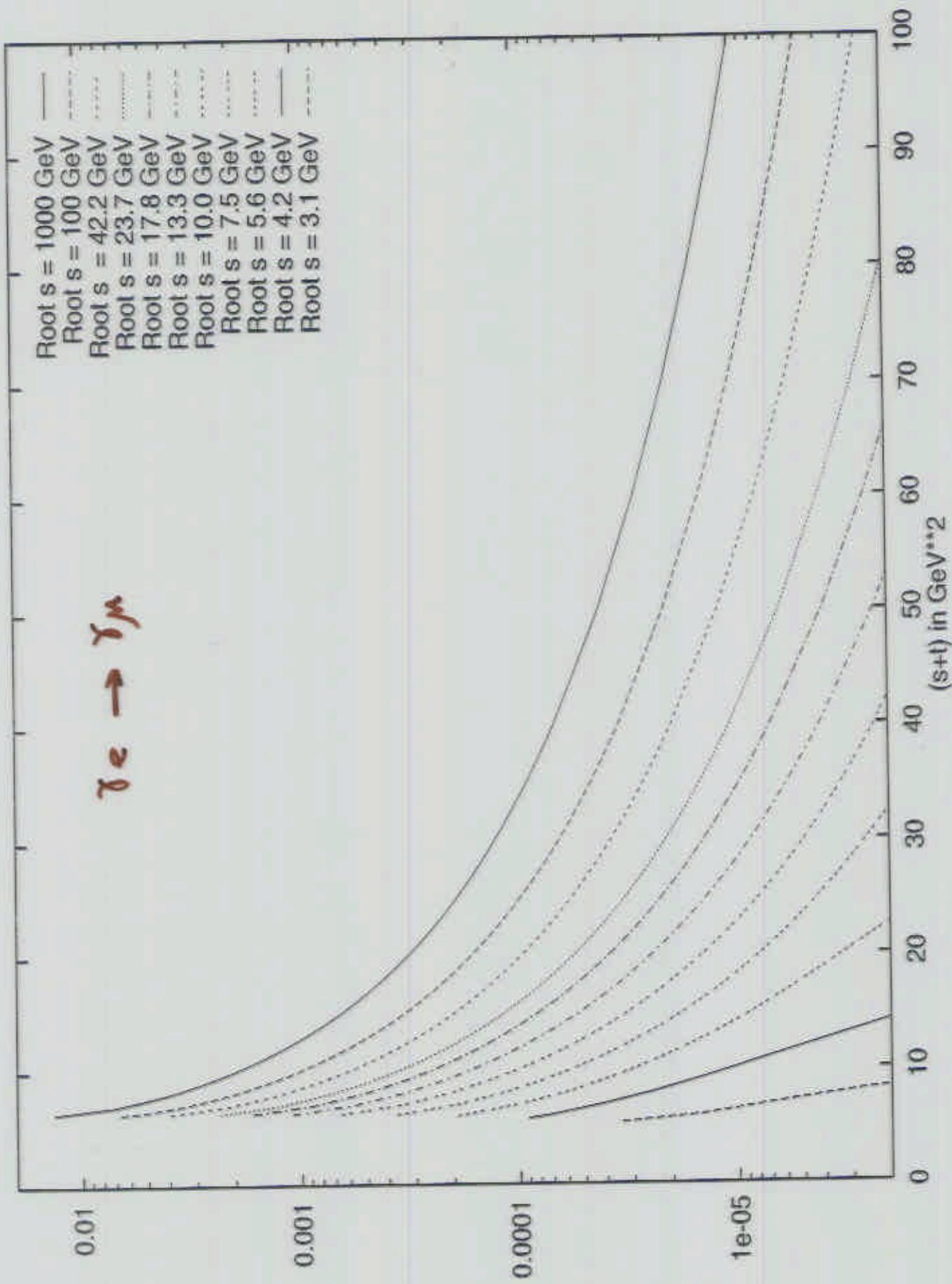
 $\rightarrow$  results app. given by scaling with relevant rotation matrix elements

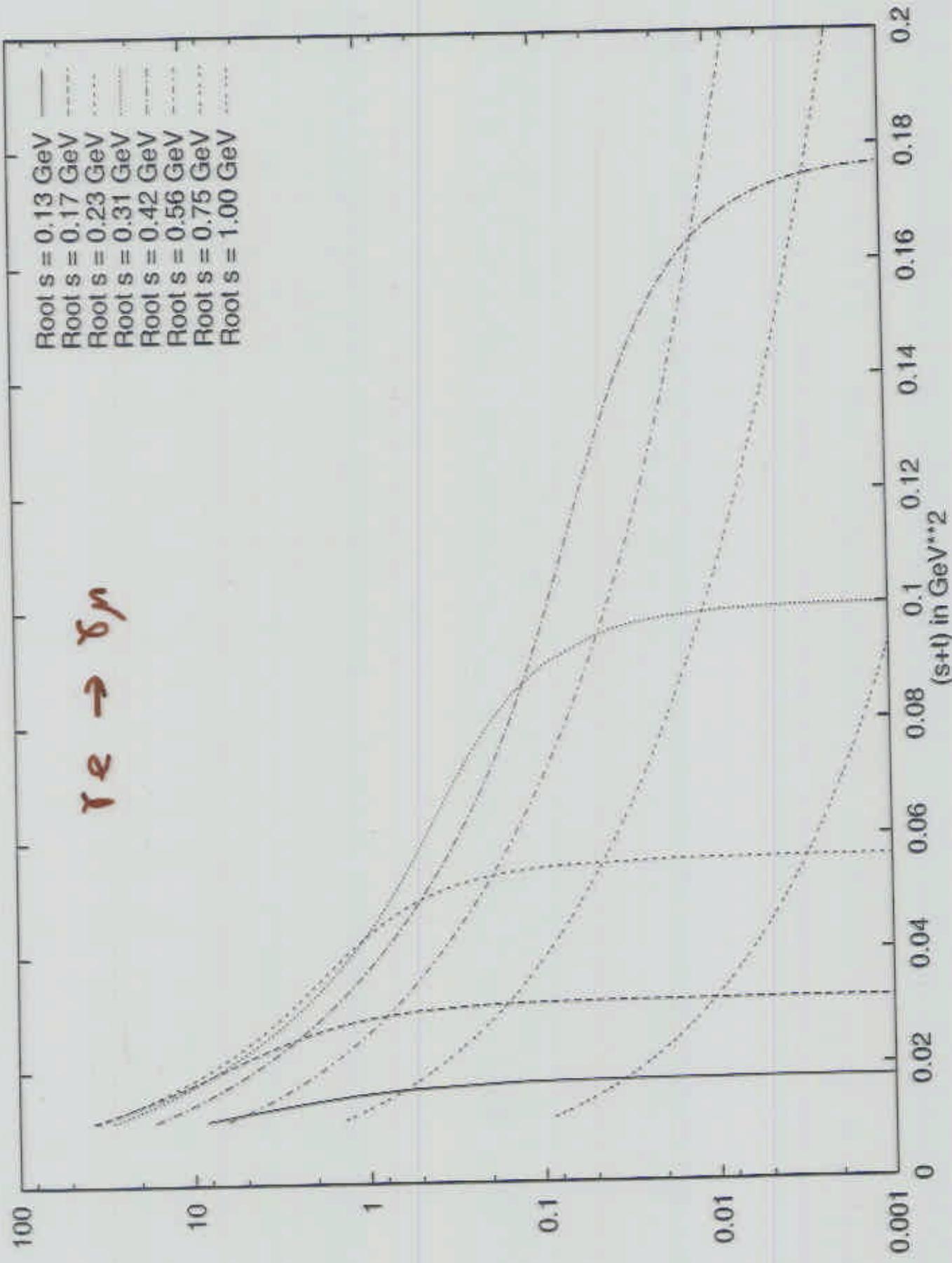
e.g.  $\gamma \mu \rightarrow \gamma \tau$  at  $\sqrt{s} = 17.8 \text{ GeV}$   
 2-3 orders smaller

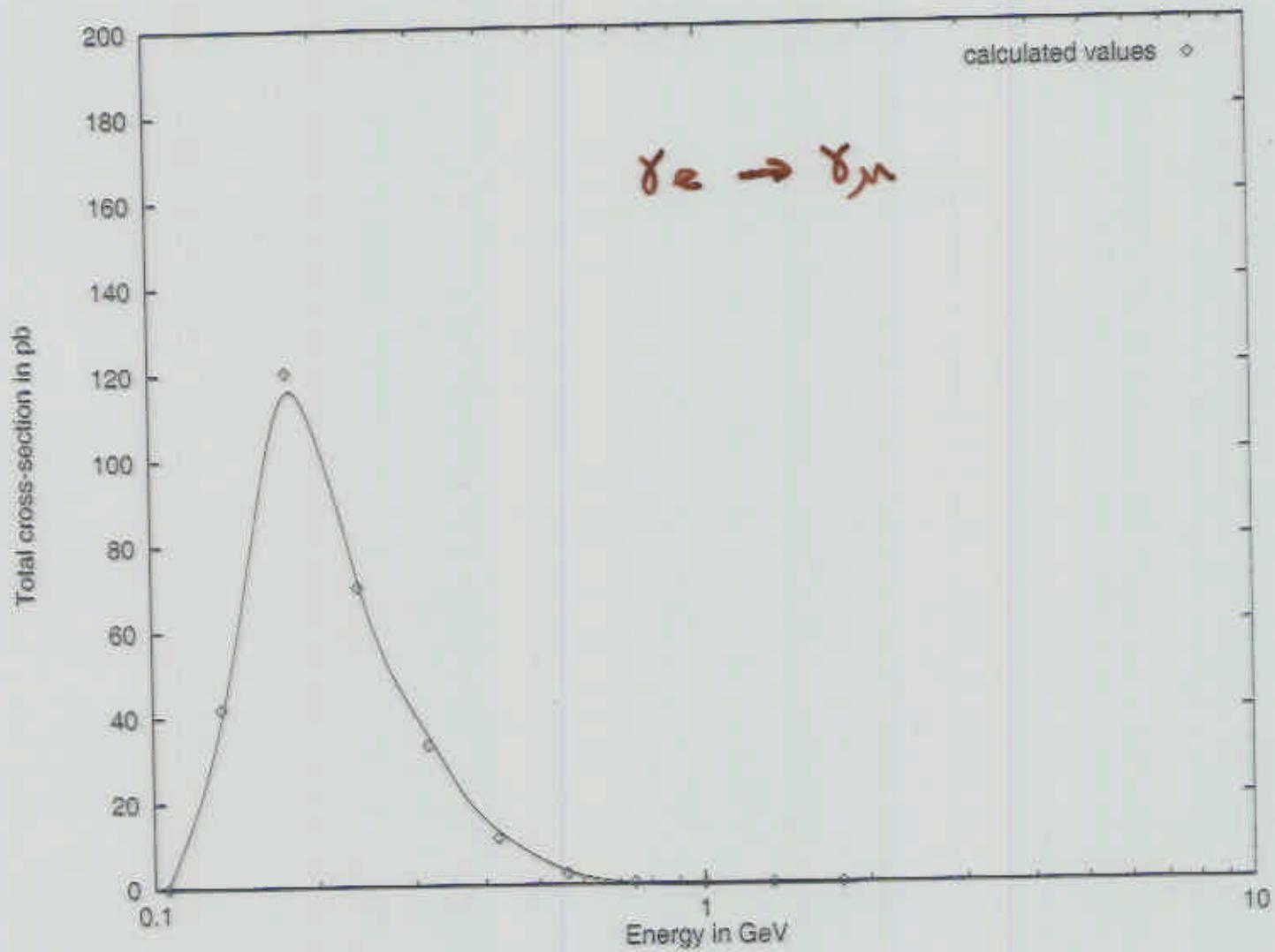


14 Differential cross-section per sr ad in pb









## Possible tests (near future?)

- may use virtual  $\gamma$  from  $e^+e^-$  colliders
- above  $\tau$  threshold, more profitable to look for  $\tau$   
(study underway) LEP or BEPC ?
- at low energy, more profitable to look for  $e \rightarrow \mu$   
transmutation,  $\sim$  cm energy 200 MeV  
(DSM max peak of  $\sim 100$  pb)  
BEPC ?

(need 40 GeV  $\gamma$ 's !)

## Conclusions

- Necessary consequence
- SM calculations
  - in general smaller than DSM
  - some uncertainties
- DSM calculations
  - parameter-free
  - working hypothesis with internal consistency
  - no violations with data so far
  - experimental tests
    - \*  $e \rightarrow \tau$
    - \*  $e \rightarrow \mu$  (below  $\tau$ )
  - other transmutational processes:  
e.g.  $e^+ e^- \rightarrow e^+ \mu^-$ , *decays*
- Exciting new physics to be explored

