

Reconstructing
Supersymmetric Theories
at High Energy Scales

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- mSUGRA, GMSB
- Procedure
- Numerical Results
- Summary

G. Blair, W. Porod, P. Zerwas, hep-ph/0007107

Supersymmetry breaking

mSUGRA*

Supergravity coupled with a GUT theory.

- gauge unification at GUT scale
- Universal input Parameters (at GUT scale):
 $M_0, M_{1/2}, A_0, \tan \beta, \text{sign}(\mu)$

GMSB†

Transfer of SUSY breaking via gauge interactions.

- Messenger scale: $M_m = \lambda S$
- $\Lambda = F/S$ where $\langle X \rangle = S + F\theta\theta$
 $M_{1/2} \rightarrow g(x)\alpha_i\Lambda, M_0^2 \rightarrow f(X)\sum C_i\alpha_i^2\Lambda^2,$
 $x = \Lambda/M, f(x), g(x) = (n_5 + n_{10})O(1)$
- $A_0, \tan(\beta), \text{sign}(\mu)$

*H.P.Nilles, Phys.Rep. 110, 1 (1984)

†G.F.Guidice and R.Rattazzi, Phys.Rep. 322, 419 (1999)

Parameters

- The unbroken MSSM

1. μ : mixing parameter for the Higgs Superfields
2. Y_u, Y_d, Y_e : Yukawa couplings of Matter Superfields with Higgs Superfields
3. g_1, g_2, g_3 : gauge couplings

- Soft Susy Breaking Terms

1. gaugino masses: $M_a \lambda_a \lambda_a + h.c.$
($a = U(1), SU(2), SU(3)$)
2. scalar masses: $M_{\tilde{Q}ij}^2 \tilde{q}_{Lj}^* \tilde{q}_{Li}, M_{\tilde{U}ij}^2 \tilde{u}_{Rj}^* \tilde{u}_{Ri},$
 $M_{\tilde{D}ij}^2 \tilde{d}_{Rj}^* \tilde{d}_{Ri}, M_{\tilde{L}ij}^2 \tilde{l}_{Lj}^* \tilde{l}_{Li}, M_{\tilde{E}ij}^2 \tilde{e}_{Rj}^* \tilde{e}_{Ri},$
 $M_{H1}^2 h_1^* h_1, M_{H2}^2 h_2^* h_2$
3. bilinear coupling: $-\epsilon_{jk} B\mu h_1^j h_2^k + h.c.$

4. trilinear couplings:

$$\epsilon_{jk}(h_1^j(\tilde{e}_R^* a_l \tilde{l}_L^k + \tilde{d}_R^* a_d \tilde{q}_L^k) - h_2^j \tilde{u}_R^* a_u \tilde{q}_L^k) + h.c.$$

Assumption

1) real Parameters

2) The generation mixing for sfermions is the same as for fermions:

$$M_{\tilde{f}ij}^2 = \delta_{ij} M_{\tilde{f}i}^2,$$

$$a_{f,ij} = \delta_{ij} A_{f,i} Y_{f,i}$$

⇒ Each of the three $(\tilde{l}, \tilde{u}, \tilde{d})$ generally 6×6 matrices can be decomposed into three 2×2 matrices

Procedure*

- Input at m_Z : $g_1, g_2, g_3, h_l, h_d, h_u, \tan \beta$ in \overline{DR} scheme
- Using 2-loop RGEs to get the above parameters at the high scale: M_{GUT} (in mSUGRA defined via $g_1 = g_2$) or M_m (in GMSB)
- Evaluating mass parameters down to electroweak scale using 2-loop RGEs[†], including threshold effects**
- radiative electroweak symmetry breaking

$$\Rightarrow |\mu|^2 = \frac{m_{H_2}^2 \sin^2 \beta - m_{H_1}^2 \cos^2 \beta}{\cos 2\beta} - \frac{m_Z^2}{2} + \text{rad.corr.}$$

*for details see e.g. Arason et al., Phys.Rev.D **46** 3945 (1992)

[†]S. Martin and M. Vaughn, Phys. Rev. **D50**, 2282 (1994); Y. Yamada, Phys. Rev. **D50**, 3537 (1994); I. Jack, D.R.T. Jones, Phys. Lett. **B333**, 372 (1994)

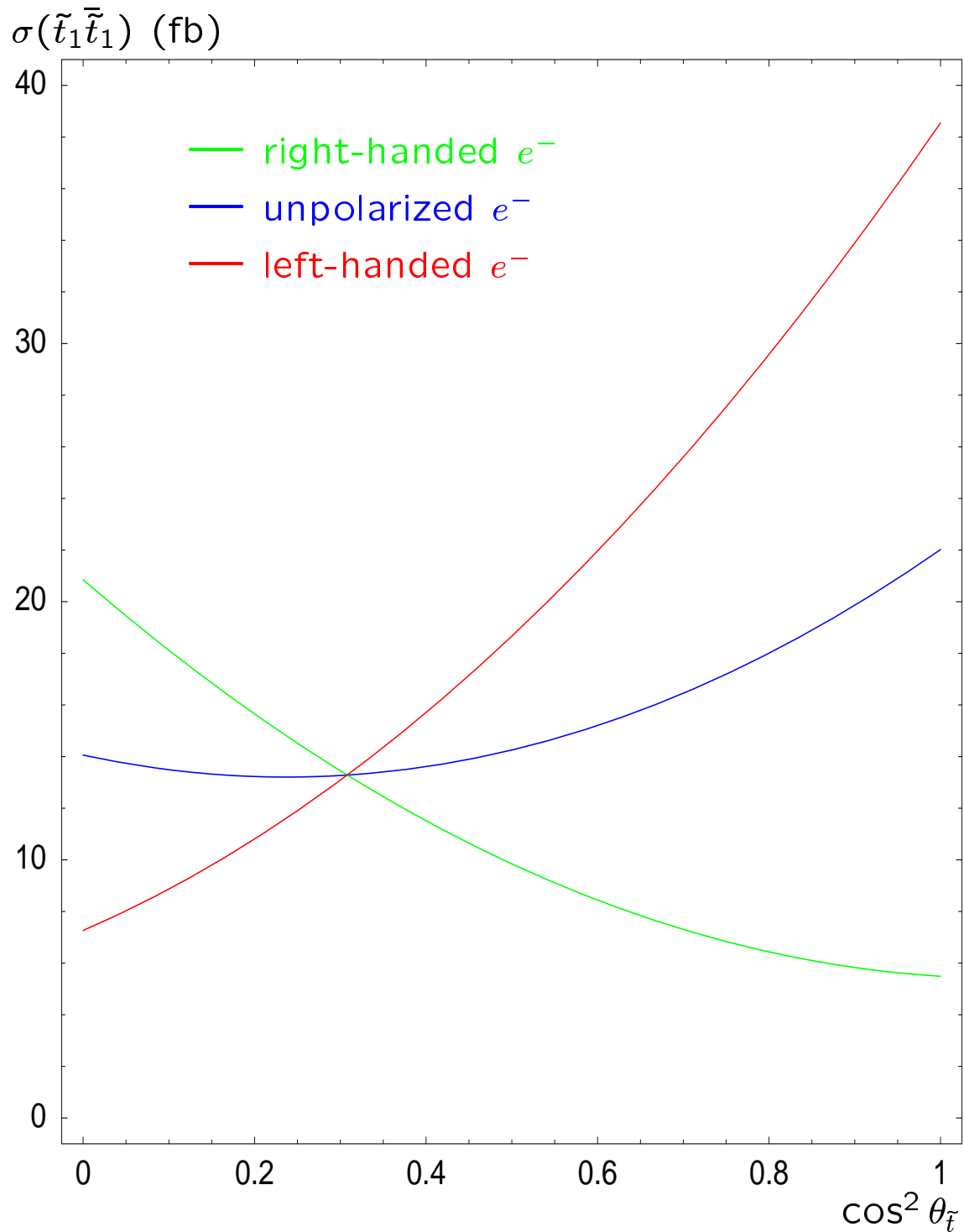
J. Bagger, K. Matchev, D. Pierce, and R. Zhang, Nucl. Phys. **B491, 3 (1997)

- Calculate SUSY masses at the electroweak scale. Attach experimental errors to the masses.
- Calculation of production cross sections for $\tilde{t}_{1,2}$, $\tilde{b}_{1,2}$, $\tilde{\tau}_{1,2}$ with polarized e^- and e^+ beams.
- Fit the masses and production cross sections within given experimental errors by varying the low energy parameters: M_{E_k} , M_{L_k} , M_{D_k} , M_{Q_k} , M_{U_k} , A_τ , A_b , A_t , M_{H_1} , M_{H_2} , M_i , $\tan \beta$, $k = 1, 3$, $i = 1, 2, 3$
- use again RGEs to get high scale parameters within the errors.

This is a pure bottom-up approach!

$$\sigma(e^+e^- \rightarrow \tilde{t}_1\bar{\tilde{t}}_1)$$

$m_{\tilde{t}_1} = 350$ GeV, $E = 1$ TeV
Polarization degree: 80%



Assumptions for the Fits*

1. $\mathcal{L} = 100 \text{ fb}^{-1}$ for each scanned point
2. $\mathcal{L} = 500 \text{ fb}^{-1}$ for each polarized cross-section measurement
3. $\Delta m_{\tilde{g}} = 10 \text{ GeV}$ from LHC[†]
4. Errors on masses for particles which decay predominantly to τ channels** are inflated conservatively
5. The errors $\Delta\sigma$ on the cross sections σ are statistical only: $\Delta\sigma = \sqrt{\frac{\sigma}{\mathcal{L}\epsilon}}$, where ϵ ($=20\%$) is the efficiency and \mathcal{L} the integrated luminosity
6. Measurement of squark masses at LC require $\sqrt{s} = 1 \text{ TeV}$ for mSUGRA and $\sqrt{s} = 1.5 \text{ TeV}$ for GMSB

*for details see e.g. G.A. Blair and U. Martyn, hep-ph/9910416

[†]ATLAS TDR, CERN/LHCC/99-15

M.M. Nojiri, K. Fujii, and T. Tsukamoto, Phys.Rev. **D54, 6756 (1996).

Particle	M(GeV) Mass	Δ M(GeV)	
		LHC	LHC+LC
h^0	109	0.2	0.05
A^0	191	3	1.5
χ_1^+	133	3	0.11
χ_1^0	72.6	3	0.15
$\tilde{\nu}_e$	233	3	0.1
\tilde{e}_1	217	3	0.15
$\tilde{\nu}_\tau$	214	3	0.8
$\tilde{\tau}_1$	154	3	0.7
\tilde{u}_1	466	10	3
\tilde{t}_1	377	10	3
\tilde{g}	470	10	10

Representative experimental mass errors used in the fits to the mass spectra. Starting point:

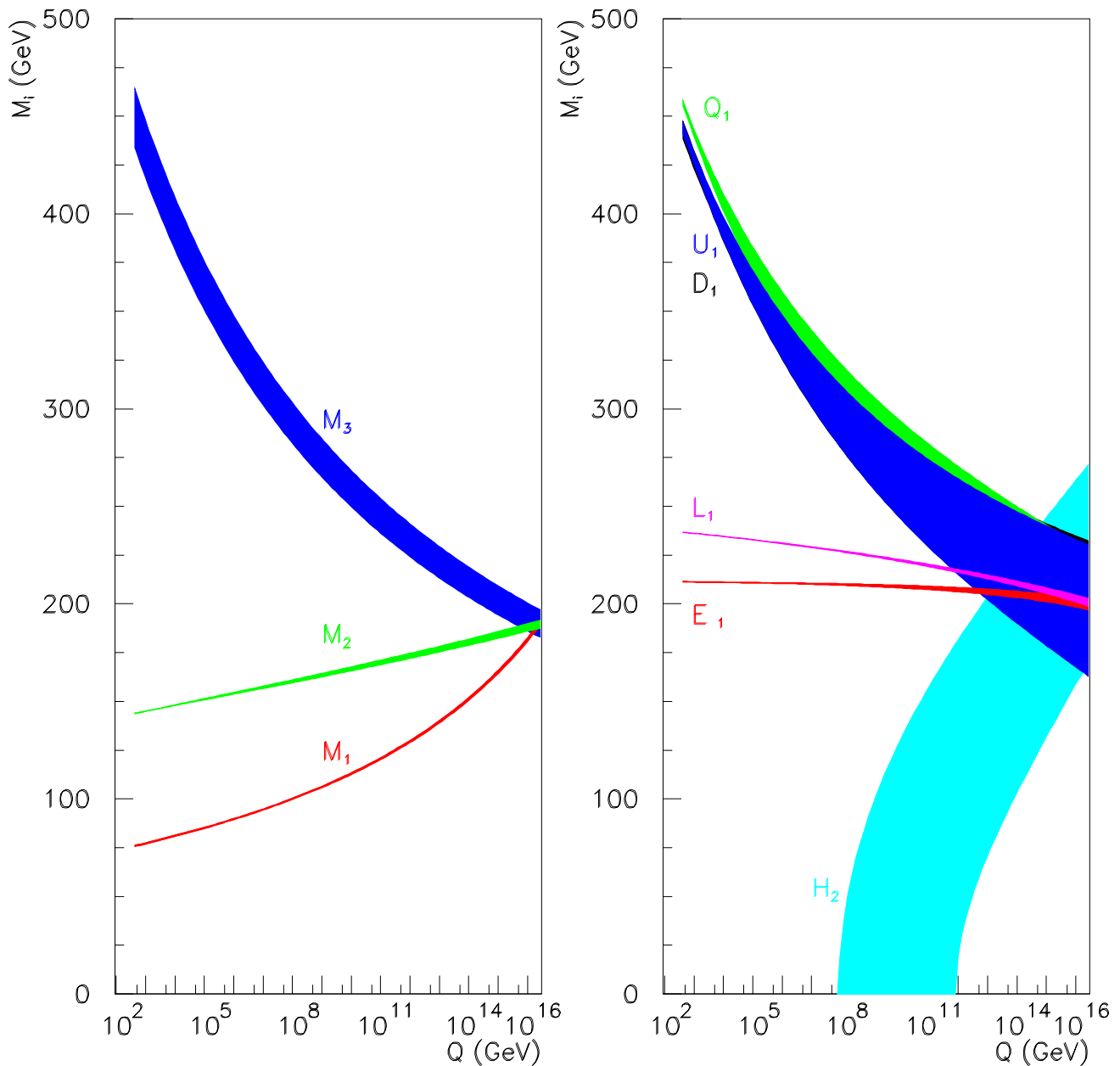
$M_0 = 200$ GeV, $M_{1/2} = 190$ GeV, $A_0 = 550$ GeV, $\tan \beta = 30$, and $\text{sign}(\mu) = (-)$.

	LHC		LC	
	exp. input	GUT value	exp. input	GUT value
M_1	75.6 ± 3.2	189.6 ± 7.6	75.6 ± 0.2	189.6 ± 0.7
M_2	143.6 ± 3.1	190.6 ± 3.8	143.6 ± 0.2	189.4 ± 0.9
M_3	452.3 ± 11.9	190.1 ± 5.7	452.3 ± 9	190.0 ± 4.2
M_{L_1}	236.8 ± 2.1	200.6 ± 6.9	236.8 ± 0.1	200.5 ± 0.9
M_{Q_1}	459.6 ± 7.4	200.7 ± 30.5	459.7 ± 0.6	200 ± 18
M_{L_3}	218.6 ± 2.8	199.5 ± 12.3	218.6 ± 0.6	196.5 ± 7.2
M_{Q_3}	392 ± 45	192 ± 251	391.2 ± 1.0	233 ± 46
M_{H_1}	132.4 ± 12	361 ± 324	132.4 ± 1.5	224 ± 90
$ M_{H_2} $	$(-)251.9 \pm 2.2$	279 ± 98	$(-)251.9 \pm 0.2$	211 ± 27
A_τ	101 ± 2590	210 ± 432	100 ± 92	319 ± 340
A_b	-125 ± 3920	806 ± 1292	-126 ± 286	129 ± 571
A_t	-186 ± 39	608 ± 169	-186.3 ± 3.2	505 ± 81

Representative mass parameters as determined at the electroweak scale and evolved to the GUT scale; the minus sign (-) in front of M_{H_2} refers to the negative value of $M_{H_2}^2$ at the electroweak scale; The errors quoted correspond to 1σ ; Starting point: $M_0 = 200$ GeV, $M_{1/2} = 190$ GeV, $A_0 = 550$ GeV, $\tan\beta = 30$, and $\text{sign}(\mu) = (-)$.

mSUGRA

$\tan \beta = 30$, $M_0 = 200$ GeV, $M_{1/2} = 190$ GeV,
 $A_0 = 550$, $\text{sign}(\mu) = -1$



The widths of the bands indicate the 95% CL.

Gaugino mass Parameters

$$M_1 \simeq 0.41M_{1/2}$$

$$M_2 \simeq 0.82M_{1/2}$$

$$M_3 \simeq 2.82M_{1/2}$$

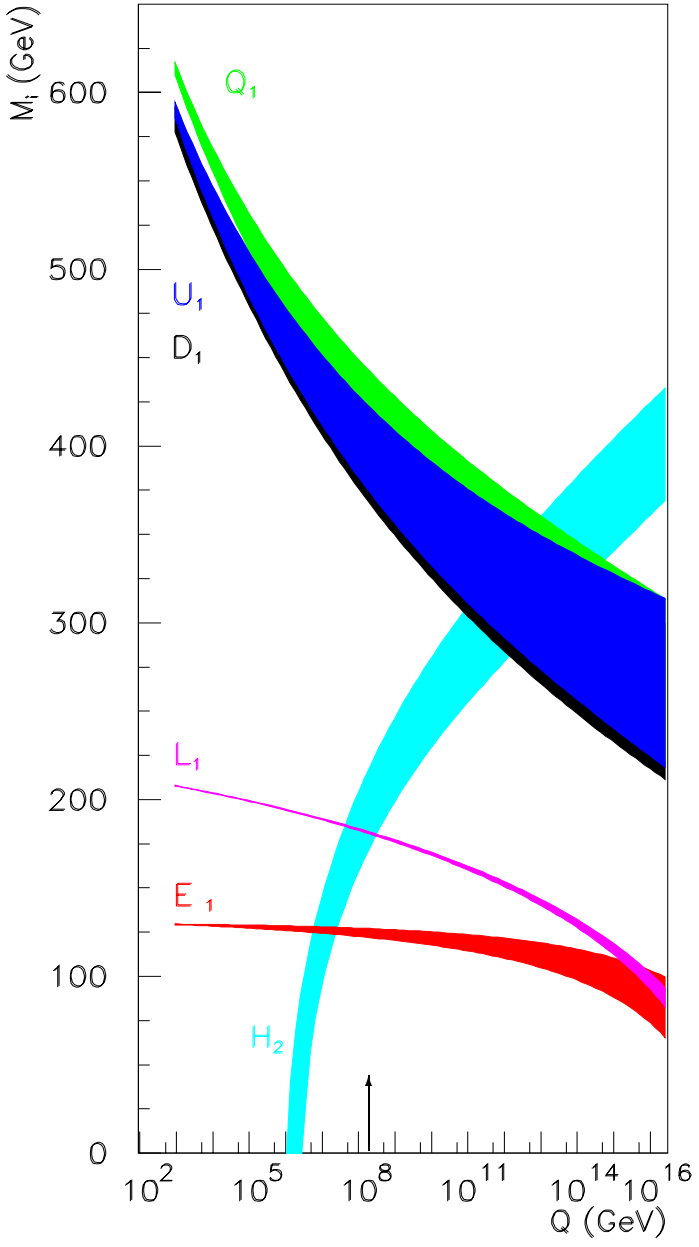
Sfermions + Higgs ($\tan\beta = 30$)

$$M^2 = aM_0^2 + bM_{1/2}^2 + cA_0^2 + dA_0M_{1/2}$$

	a	b	c	d
$M_{\tilde{E}_{1,2}}^2$	1	0.15		
$M_{\tilde{L}_{1,2}}^2$	1	0.52		
$M_{\tilde{U}_{1,2}}^2 \simeq M_{\tilde{D}_{1,2}}^2$	1	6.2		
$M_{\tilde{Q}_{1,2}}^2$	1	6.7		
$M_{\tilde{E}_3}^2$	0.94	0.14	-0.02	
$M_{\tilde{L}_3}^2$	0.97	0.52	-0.01	
$M_{\tilde{D}_3}^2$	0.78	5.7	-0.05	- 0.21
$M_{\tilde{U}_3}^2$	0.27	4.5	-0.07	-0.28
$M_{\tilde{Q}_3}^2$	0.53	5.6	-0.06	-0.25
$M_{\tilde{H}_1}^2$	0.65	-0.24	0.09	-0.32
$M_{\tilde{H}_2}^2$	-0.18	-2.2	0.08	-0.35

GMSB

$M_m = 2 \cdot 10^5$ TeV, $\Lambda = 28$ TeV, $N_5 = 3$,
 $\tan \beta = 30$, $A_0 = 0$, $\text{sign}(\mu) = -1$



The widths of the bands indicate the 95% CL.

Summary

- We have used the **bottom-up approach** for determining the high scale parameters assuming we know **masses and cross sections** within the **experimental errors**.
- The **model-independent reconstruction** of the fundamental supersymmetric theory **at the high scale**, the grand unification scale M_{GUT} in supergravity or the intermediate scale M_m in gauge mediated supersymmetry breaking, **appears feasible**.
- The **accuracy** is **significantly improved** if, in addition to the **LHC input** values, **high-precision LC values** are also included.