

**Some Recent Results
from the Complete Theory of
Supersymmetry without R-parity**

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Supersymmetry without R-parity IS the Generic Supersymmetric SM

- minimal superfield spectrum
- SM (gauge) symmetries

as Vs R-parity Violations

R-parity Violating Parameters

- trilinear (superpotential) : λ_{ijk} , λ'_{ijk} , λ''_{ijk}
- bilinear (superpotential) : μ_i
- trilinear & bilinear (soft SUSY breaking) :
- scalar mass mixing (soft SUSY breaking) :

★ “sneutrino VEVs”

⇒ the Complete Theory

A Purely Phenomenological Approach :-

- a formulation that relies on *no a priori* assumption
- study admissible phenomenology
- check experimental constraints on the various parameters
- need optimal set of independent parameters
 - to simplify analysis
 - to remove ambiguity
- **SINGLE-VEV parametrization**
 - such an optimal choice of flavor bases
 - with RPV effects on tree-level mass matrices for all states (scalars and fermions) maintaining the simplest structure

Supersymmetrizing the SM Matter Fields

— minimal list of superfields :-

- holomorphy of superpotential requires
(at least) two independent Higgs doublets

	<i>fermion</i>	<i>scalar</i>
$(3, 2)_{1/3}$	$3 \ Q_i \rightarrow$	
$(\bar{3}, 1)_{-4/3}$	$3 \ U_i^c \rightarrow$	
$(\bar{3}, 1)_{2/3}$	$3 \ D_i^c \rightarrow$	
$(1, 2)_1$		$\leftarrow H_u$
$(1, 2)_{-1}$	$3 \ L_i \rightarrow$	$\leftarrow H_d$
$(1, 1)_2$	$3 \ E_i^c \rightarrow$	

3 \hat{Q}_i

3 \hat{U}_i^c

3 \hat{D}_i^c

\hat{H}_u

4 \hat{L}_α

3 \hat{E}_i^c

* extra fermion (higgsino) doublet needed for
gauge anomaly cancellation*

WHAT IS R-PARITY ?

- (SM) particles — even
- superparticles — odd

$$\mathcal{R} = (-1)^{3B + L + 2S}$$

- B - baryon number
- L - lepton number
- S - spin (of component)

As superfields :-

- $\hat{Q}_i, \hat{U}_i^c, \hat{D}_i^c, \hat{L}_i, \hat{E}_i^c$ — odd
- \hat{H}_u, \hat{H}_d — even

* \hat{L}_i and \hat{H}_d NOT the same quantum numbers *

R-parity conserving MSSM :

- superparticles have a *categorically different* quantum number
- NO NEUTRINO MASSES !!

Life without R-parity :-

- B violation and L violation

$$W = \varepsilon_{ab} [\mu_\alpha \hat{H}_u^a \hat{L}_\alpha^b + h_{ik}^u \hat{Q}_i^a \hat{H}_u^b \hat{U}_k^c + \lambda'_{\alpha j k} \hat{L}_\alpha^a \hat{Q}_j^b \hat{D}_k^c \\ + \lambda''_{\alpha \beta k} \hat{L}_\alpha^a \hat{L}_\beta^b \hat{E}_k^c] + \lambda'''_{ijk} \hat{U}_i^c \hat{D}_j^c \hat{D}_k^c$$

- proton \(\langle>\)/
- neutrinos \(\langle^0\rangle/\ \langle^o\rangle/\ \langle^0\rangle/\)



listen to the neutrinos

+

impose **B** (*or baryon parity*)

\(\langle>\)/ → ... → \(\langle^0\rangle/\)

Parametrization — choice of flavor bases :-

e.g. two 3×3 quark Yukawas \rightarrow 10 parameters

- $h_{ik}^u = \frac{\sqrt{2}}{v_u} V_{CKM}^\dagger \text{diag}\{m_u, m_c, m_t\}$
- $h_{jk}^d = \frac{\sqrt{2}}{v_d} \text{diag}\{m_d, m_s, m_b\}$

SINGLE-VEV parametrization

for SUSY w/o R-parity :-

- **4 \hat{L} flavors \rightarrow SINGLE VEV** ($v_0 \equiv v_d$)
 - no $\lambda, \lambda', \lambda''$ in fermion mass matrices
 - h_{ik}^u and $h_{jk}^d (\equiv \lambda'_{0jk})$ as above
- **+ 3 \hat{E}^C $\rightarrow h_{jk}^e = \frac{\sqrt{2}}{v_0} \text{diag}\{m_1, m_2, m_3\}$**
 - but the three m_i 's correspond to the physical charged lepton masses *only* when $\mu_i = 0$

(Color-singlet) Charged Fermion Sector :-

$$\mathcal{M}_C = \begin{pmatrix} M_2 & \frac{g_2 v_0}{\sqrt{2}} & 0 & 0 & 0 \\ \frac{g_2 v_u}{\sqrt{2}} & \mu_0 & \mu_1 & \mu_2 & \mu_3 \\ 0 & 0 & m_1 & 0 & 0 \\ 0 & 0 & 0 & m_2 & 0 \\ 0 & 0 & 0 & 0 & m_3 \end{pmatrix}$$

INSTEAD OF

$$\begin{pmatrix} M_2 & \frac{g_2 v_0}{\sqrt{2}} & \frac{g_2 v_1}{\sqrt{2}} & \frac{g_2 v_2}{\sqrt{2}} & \frac{g_2 v_3}{\sqrt{2}} \\ \frac{g_2 v_u}{\sqrt{2}} & \mu_0 & \mu_1 & \mu_2 & \mu_3 \\ 0 & 2\lambda_{\alpha 01} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 11} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 02} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 13} \frac{v_\alpha}{\sqrt{2}} \\ 0 & 2\lambda_{\alpha 02} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 21} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 22} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 23} \frac{v_\alpha}{\sqrt{2}} \\ 0 & 2\lambda_{\alpha 03} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 31} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 32} \frac{v_\alpha}{\sqrt{2}} & 2\lambda_{\alpha 33} \frac{v_\alpha}{\sqrt{2}} \end{pmatrix}$$

- ★ μ_i 's cannot be set to zero in general ★
- m_i 's have to be determined by imposing the correct ℓ_i masses for the mass eigenstates

Neutral Fermion Sector :-

$$\mathcal{M}_N = \begin{pmatrix} M_1 & 0 & \frac{g_1 v_u}{2} & -\frac{g_1 v_0}{2} & 0 & 0 & 0 \\ 0 & M_2 & -\frac{g_2 v_u}{2} & \frac{g_2 v_0}{2} & 0 & 0 & 0 \\ \frac{g_1 v_u}{2} & -\frac{g_2 v_u}{2} & 0 & -\mu_0 & -\mu_1 & -\mu_2 & -\mu_3 \\ -\frac{g_1 v_0}{2} & \frac{g_2 v_0}{2} & -\mu_0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\mu_1 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\mu_2 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\mu_3 & 0 & 0 & 0 & 0 \end{pmatrix}$$

- one massive neutrino state :

$$|\nu_5\rangle = \frac{\mu_1}{\mu_5} |\psi_{L_1}^1\rangle + \frac{\mu_2}{\mu_5} |\psi_{L_2}^1\rangle + \frac{\mu_3}{\mu_5} |\psi_{L_3}^1\rangle$$

$$\mu_5 = \sqrt{\mu_1^2 + \mu_2^2 + \mu_3^2}$$

- it is an admixture of the " ν_e, ν_μ, ν_τ "
- sub-eV (oscillation) masses \rightarrow very small μ_i
our basis gives e, μ and τ
- Super-K atmospheric result
 \implies **maximal mixing**
 Vs usual hierarchical flavor structure

Constraints from Leptonic Phenomenology

Quantity	μ_i combo. constrained	Experimental bounds
Z^0-coupling:		
• $U_{br}^{e\mu}$ ($e-\mu$ universality)	$\mu_1^2 - \mu_2^2$	$(0.596 \pm 4.37) \times 10^{-3}$
• $U_{br}^{e\tau}$ ($e-\tau$ universality)	$\mu_1^2 - \mu_3^2$	$(0.955 \pm 4.98) \times 10^{-3}$
• $U_{br}^{\mu\tau}$ ($\mu-\tau$ universality)	$\mu_2^2 - \mu_3^2$	$(1.55 \pm 5.60) \times 10^{-3}$
• $\Delta A_{e\mu}$ ($e-\mu$ L-R asymmetry)	$\mu_1^2 - \mu_2^2 + \text{Rt. contrib.}$	$(0.346 \pm 2.54) \times 10^{-2}$
• $\Delta A_{e\tau}$ ($e-\tau$ L-R asymmetry)	$\mu_1^2 - \mu_2^2 + \text{Rt. contrib.}$	0.0043 ± 0.104
• $\Delta A_{\tau\mu}$ ($\tau-\mu$ L-R asymmetry)	$\mu_1^2 - \mu_2^2 + \text{Rt. contrib.}$	0.082 ± 0.25
• $Br(Z^0 \rightarrow e^\pm \mu^\mp)$	$ \mu_1 \mu_2 $	$< 1.7 \times 10^{-6}$
• $Br(Z^0 \rightarrow e^\pm \tau^\mp)$	$ \mu_1 \mu_3 $	$< 9.8 \times 10^{-6}$
• $Br(Z^0 \rightarrow \mu^\pm \tau^\mp)$	$ \mu_2 \mu_3 $	$< 1.2 \times 10^{-5}$
• $Br(\mu^- \rightarrow e^- e^+ e^-)$	$ \mu_1 \mu_2 $	$< 1.0 \times 10^{-12}$
• $Br(\tau^- \rightarrow e^- e^+ e^-)$	$ \mu_1 \mu_2 $	$< 2.9 \times 10^{-8}$
• $Br(\tau^- \rightarrow \mu^- e^+ e^-)$	$ \mu_2 \mu_3 $	$< 1.7 \times 10^{-8}$
• $Br(\tau^- \rightarrow \mu^+ e^- e^-)$	$ \mu_1^2 \mu_2 \mu_3 $	$< 1.5 \times 10^{-8}$
• $Br(\tau^- \rightarrow e^- \mu^+ \mu^-)$	$ \mu_1 \mu_3 $	$< 1.8 \times 10^{-9}$
• $Br(\tau^- \rightarrow e^+ \mu^- \mu^-)$	$ \mu_1 \mu_2^2 \mu_3 $	$< 1.5 \times 10^{-8}$
• $Br(\tau^- \rightarrow \mu^- \mu^+ \mu^-)$	$ \mu_2 \mu_3 $	$< 1.9 \times 10^{-8}$
• $Br(Z^0 \rightarrow \chi^\pm \ell^\mp)$	μ_5	$< 1.0 \times 10^{-5}$
• $Br(Z^0 \rightarrow \chi^\pm \chi^\mp)$	μ_5	$< 1.0 \times 10^{-5}$
• $Br(Z^0 \rightarrow \chi_i^0 \chi_j^0, \chi_j^0 \nu); j \neq 1$	μ_5	$< 1.0 \times 10^{-5}$
• Γ_s (total Z^0 -width)	μ_5	$2.4948 \pm .0075 \text{ GeV}$
• Γ_s^{expt} (*)	μ_5	$500.1 \pm 5.4 \text{ MeV}$
W^\pm-coupling:		
• $\bar{\Gamma}^{\mu e}$ ($\mu \rightarrow e \nu \nu$)	m_{ν_3} / μ_i ratio	0.983 ± 0.111
• $\bar{\Gamma}^{\tau e}$ ($\tau \rightarrow e \nu \nu$)	m_{ν_3} / μ_i ratio	0.979 ± 0.111
• $\bar{\Gamma}^{\tau \mu}$ ($\tau \rightarrow \mu \nu \nu$)	m_{ν_3} / μ_i ratio	0.954 ± 0.108
• $R_{\pi\mu}^{ee}$ (π decays)	$m_{\nu_3} / \frac{\mu_1}{\mu_5}$ and $\frac{\mu_2}{\mu_5}$	$(1.230 \pm 0.012) \times 10^{-4}$
• $R_{\tau\mu}^{ee}$ (τ decays)	m_{ν_3} / μ_i ratio	1.0265 ± 0.0222
• $R_{\tau e}^{\mu e}$ (decays to e 's)	m_{ν_3} / μ_i ratio	1.0038 ± 0.0219
• $m_{\nu_3} \tilde{B}_{e\nu_3}^L ^2$ [$(\beta\beta)_{0\nu}$]	$m_{\nu_3} / \frac{\mu_1}{\mu_5}$	$< 0.46 \text{ eV}$ (only for $m_{\nu_3} < 10 \text{ MeV}$)
• BEBC expt.	$m_{\nu_3} / \frac{\mu_1}{\mu_5}$ and $\frac{\mu_2}{\mu_5}$	
mass constraints:		
• ν_3 mass	μ_5	$< 18.2 \text{ MeV}$ if $\nu_3 = \nu_\tau$
• χ^\pm mass	μ_5	$< 149 \text{ MeV}$ if $\nu_3 \neq \nu_\tau$
		$> 70 \text{ GeV}$

Studies on Various Phenomenological Issues :-

- unconventional Z^0 and W^\pm couplings
 - leptonic **universality violations**
 - lepton number violating **rare decays**

used to give overall constraint on μ_i 's
 (with Bisset, Macesanu, and Orr)

(NEUTRINO OSCILLATIONS :)

- bilinear (μ_i 's) or trilinear (λ and λ') only
 - implications on flavor structure
 - bilinear and trilinear together
 - give new contributions (SUSY Zee diagram)
(with Cheung)
 - full neutrino mass contributions up to 1-loop

 - new contribution to LR-mixing squark and slepton masses (bilinear and trilinear together)
 - neutron and electron EDM at 1-loop
 - $B \rightarrow s\gamma, \mu \rightarrow e\gamma, \dots$
(with Keum)
 - direct CP violation in B-decay
(with Tseng)
 - scalar sector
 - charginos,

Complete Soft SUSY Breaking Terms :-

$$\begin{aligned}
 V_{\text{soft}} = & \epsilon_{ab} \left[B_0 H_u^a H_d^b + A_{ij}^U \tilde{Q}_i^a H_u^b \tilde{U}_j^C + A_{ij}^D H_d^a \tilde{Q}_i^b \tilde{D}_j^C \right. \\
 & + A_{ij}^E H_d^a \tilde{L}_i^b \tilde{E}_j^C + B_i H_u^a \tilde{L}_i^b + A_{ijk}^{\lambda'} \tilde{L}_i^a \tilde{Q}_j^b \tilde{D}_k^C \\
 & + A_{ijk}^{\lambda} \tilde{L}_i^a \tilde{L}_j^b \tilde{E}_k^C \Big] + A_{ijk}^{\lambda''} \tilde{U}_i^C \tilde{D}_j^C \tilde{D}_k^C \\
 & + \tilde{Q}^\dagger \tilde{m}_Q^2 \tilde{Q} + \tilde{U}^\dagger \tilde{m}_U^2 \tilde{U} + \tilde{D}^\dagger \tilde{m}_D^2 \tilde{D} \\
 & + \tilde{L}^\dagger \tilde{m}_L^2 \tilde{L} + \tilde{E}^\dagger \tilde{m}_E^2 \tilde{E} + \tilde{m}_{H_u}^2 |H_u|^2 \\
 & + \frac{M_1}{2} \tilde{B} \tilde{B} + \frac{M_2}{2} \tilde{W} \tilde{W} + \frac{M_3}{2} \tilde{g} \tilde{g}
 \end{aligned}$$

Note that $\tilde{m}_{L_{00}}^2 \rightarrow \tilde{m}_{H_d}^2$ ($H_d \equiv L_0$)

Squark mass — new (RPV) contribution

$$\mathcal{M}_D^2 = \begin{pmatrix} \mathcal{M}_{LL}^2 & \mathcal{M}_{RL}^{2\dagger} \\ \mathcal{M}_{RL}^2 & \mathcal{M}_{RR}^2 \end{pmatrix}$$

where

$$(\mathcal{M}_{RL}^2)^T = A^D \frac{v_0}{\sqrt{2}} - m_D \mu_0^* \tan\beta - (\mu_i^* \lambda'_{ijk}) \frac{v_u}{\sqrt{2}}$$

$(\mu_i^* \lambda'_{ijk})$ is interesting

- 3×3 matrix $()_{jk}$ with elements listed
- **SUSY conserving R-parity violating contributions**
- **no natural mechanism for suppression of off-diagonal part**

Vs e.g.

$$A^D \frac{v_0}{\sqrt{2}} = A_d m_D + \delta A^D \frac{v_0}{\sqrt{2}}$$

— soft SUSY breaking part (proportionality)

\mathcal{M}_{RL}^2 contributes to FCNC

e.g. $b \rightarrow s\gamma$

also neutron EDM, neutrino masses

Similarly, we have $(\mu_i^* \lambda_{ijk})$ for charged leptons

e.g. **Neutron EDM** $[(d_n)^{\text{exp}} < 6.3 \cdot 10^{-26} e \cdot \text{cm}]$:-

— gluino diagram

$$\left(\frac{d_d}{e} \right)_{\tilde{g}} = -\frac{2\alpha_s}{3\pi} \frac{M_{\tilde{g}}}{M_{\tilde{d}}^2} Q_{\tilde{d}} \text{Im}(\delta_{11}^D) F\left(\frac{M_{\tilde{g}}^2}{M_{\tilde{d}}^2} \right)$$

$$\begin{aligned} \delta_{11}^D M_{\tilde{d}}^2 &= [A_d - \mu_0^* \tan\beta] m_d + \frac{\sqrt{2} M_W \cos\beta}{g_2} \delta A_{11}^D \\ &\quad - \frac{\sqrt{2} M_W \sin\beta}{g_2} (\mu_i^* \chi'_{i11}) \end{aligned}$$

- neutrino mass bound (super-K)

- χ_{311} (also $\tau \rightarrow \pi\nu$) $\lesssim 0.05 \sim 0.1$
- $\mu_i \cos\beta \lesssim 10^{-4} \text{ GeV}$

EDM : $M_{\tilde{d}} = 100 \text{ GeV}$ and $M_{\tilde{g}} = 300 \text{ GeV}$ gives

$$\text{Im}(\mu_i^* \chi'_{i11}) \lesssim 10^{-6} \text{ GeV}$$

- ★ RPV contribution could be larger than MSSM part

- ★ new bound interesting

Slepton-Higgs Masses :-

Charged particles — 4 + 3 + 1 matrix :

$$\mathcal{M}_E^2 = \begin{pmatrix} \widetilde{\mathcal{M}}_{LL}^2 & \widetilde{\mathcal{M}}_{RL}^{2\dagger} & \widetilde{\mathcal{M}}_{LH}^2 \\ \widetilde{\mathcal{M}}_{RL}^2 & \widetilde{\mathcal{M}}_{RR}^2 & \widetilde{\mathcal{M}}_{RH}^2 \\ \widetilde{\mathcal{M}}_{LH}^{2\dagger} & \widetilde{\mathcal{M}}_{RH}^{2\dagger} & \widetilde{\mathcal{M}}_{Hu}^2 \end{pmatrix},$$

where

$$\begin{aligned} \widetilde{\mathcal{M}}_{LL}^2 &= \tilde{m}_L^2 + m_L^\dagger m_L + (\mu_\alpha^* \mu_\beta) + M_Z^2 \cos 2\beta \left[-\frac{1}{2} + \sin^2 \theta_W \right] \\ &\quad + \begin{pmatrix} M_Z^2 \cos^2 \beta [1 - \sin^2 \theta_W] & 0_{1 \times 3} \\ 0_{3 \times 1} & 0_{3 \times 3} \end{pmatrix}, \\ \widetilde{\mathcal{M}}_{RR}^2 &= \tilde{m}_E^2 + m_E^\dagger m_E + M_Z^2 \cos 2\beta [-\sin^2 \theta_W], \\ \widetilde{\mathcal{M}}_{Hu}^2 &= \tilde{m}_{Hu}^2 + \mu_\alpha^* \mu_\alpha + M_Z^2 \cos 2\beta \left[\frac{1}{2} - \sin^2 \theta_W \right] \\ &\quad + M_Z^2 \sin^2 \beta [1 - \sin^2 \theta_W]. \end{aligned}$$

- \tilde{m}_L^2 is a 4×4 matrix with \tilde{m}_{L0i}^2 being RPV
- $\mu_\alpha^* \mu_\beta$ contains RPV flavor mixings, e.g. $\mu_i^* \mu_j$

$$\begin{aligned}
 (\widetilde{\mathcal{M}}_{RL}^2)^T &= \begin{pmatrix} 0 \\ A^E \end{pmatrix} \frac{v_0}{\sqrt{2}} - (\mu_\alpha^* \lambda_{\alpha\beta k}) \frac{v_u}{\sqrt{2}} \\
 &= [A_e - \mu_0^* \tan\beta] \begin{pmatrix} 0 \\ m_E \end{pmatrix} + \frac{v_0}{\sqrt{2}} \begin{pmatrix} 0 \\ \delta A^E \end{pmatrix} \\
 &\quad - \begin{pmatrix} -\mu_k^* m_k \tan\beta \\ \frac{\sqrt{2} M_W \sin\beta}{g_2} (\mu_i^* \lambda_{ijk}) \end{pmatrix}, \\
 \widetilde{\mathcal{M}}_{RH}^2 &= -(\mu_i^* \lambda_{iok}) \frac{v_0}{\sqrt{2}} = (\mu_k^* m_k) \quad (\text{no sum over } k), \\
 \widetilde{\mathcal{M}}_{LH}^2 &= \begin{pmatrix} B_0^* \\ (B_k^*) \end{pmatrix} + \begin{pmatrix} \frac{1}{2} M_Z^2 \sin 2\beta [1 - \sin^2 \theta_W] \\ 0_{3 \times 1} \end{pmatrix}.
 \end{aligned}$$

- $m_t = \text{diag}\{0, m_E\} = \text{diag}\{0, m_4, m_2, m_3\}$
- 4 × 3 matrix $(\mu_i^* \lambda_{i\beta k})$
 - first row : $\tilde{l}_R^c \tilde{h}_d$ mass

plays a role in SUSY Zee model where a right-handed slepton becomes the Zee scalar

$$\mathcal{M}_S^2 =$$

$$\begin{pmatrix} \tilde{m}_L^2 + (\mu_\alpha^* \mu_\beta) + \frac{M_Z^2 \cos 2\beta}{2} & -(B_\alpha^*) \\ -(B_\alpha) & \tilde{m}_{H_u}^2 + \mu_\alpha^* \mu_\alpha - \frac{M_Z^2 \cos 2\beta}{2} \end{pmatrix}$$

$$+ \frac{1}{2} M_Z^2 \begin{pmatrix} \cos^2 \beta & 0_{1 \times 3} & -\cos \beta \sin \beta \\ 0_{3 \times 1} & 0_{3 \times 3} & 0_{3 \times 1} \\ -\cos \beta \sin \beta & 0_{1 \times 3} & \sin^2 \beta \end{pmatrix}$$

+

Majorana-like mass terms for Higgses :

$$\frac{1}{4} M_Z^2 \cos^2 \beta h_d^0 h_d^0 - \frac{1}{2} M_Z^2 \cos \beta \sin \beta h_u^{0\dagger} h_d^0 + \frac{1}{4} M_Z^2 \sin^2 \beta h_u^0 h_u^0$$

$+ h.c.$

- B_i 's lead to (seesaw type) Majorana-like mass terms for “sneutrinos”

→ gauge loop neutrino mass

Haber/Grossman

→ RPV contribution to quark-scalar (Higgs)
loop of EDM, FCNC

under study