

B and D Meson Lifetime Measurements with Belle

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A ~~outline~~ ~~for~~ ~~the~~ ~~work~~
and should ~~be~~ ~~be~~ ~~used~~

- Outline
- Physics background.
- D lifetime measurements.
- » Reconstruction.
- » Lifetime fit.

- B lifetime measurements.

- » Reconstruction.
- » Lifetime fit.

- Summary



Physics Background



Lifetime Physics.

- Theoretical inputs to understand non-perturbative QCD in the heavy quark decay.
 - » Annihilation process, W-exchange
 - Theoretical challenge to explain $\tau(D_s)/\tau(D^0) \approx 1.21 \pm 0.02$

Mixing

- Difference of lifetime between flavor specific mode and CP mode gives mixing parameter, y_{CP} .

$$\begin{aligned} y_{CP} &= \frac{\Delta\Gamma}{\Gamma} = \frac{\Gamma(CP\text{even}) - \Gamma(CP\text{odd})}{\Gamma(CP\text{even}) + \Gamma(CP\text{odd})} \\ &= \frac{\tau(D^0 \rightarrow K^-\pi^+) - \tau(D^0 \rightarrow K^-K^+)}{\tau(D^0 \rightarrow K^-\pi^+) + \tau(D^0 \rightarrow K^-K^+)} - 1 \approx y \cos\phi + \frac{A_{mix}}{2} x \sin\phi \\ &= 1 - \frac{\tau(\bar{B}^0 \rightarrow D^{*+} \ell\nu, D\pi)}{\tau(\bar{B}^0 \rightarrow \psi K_S)} \approx y \cos 2\phi_1 \end{aligned}$$

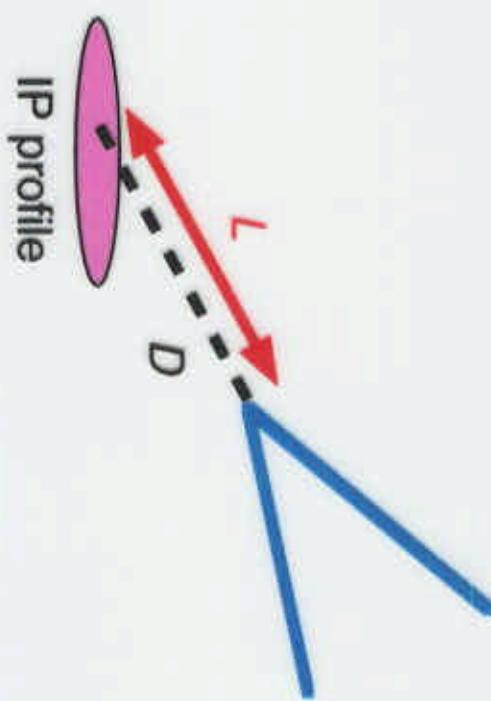
- Analysis is based on 2.75 fb⁻¹ (D lifetime analysis), 5.1 fb⁻¹ (B lifetime analysis).

All results are preliminary.

D Proper-time Reconstruction

Reconstruction.

- **Reconstruct specific D decay modes.**
 - » $D^0 \rightarrow K^-\pi^+$, K^-K^+ , $D^+ \rightarrow K^-\pi^+\pi^+$, $\phi\pi^+$, $D_s^+ \rightarrow \phi\pi^+$, K^0K^+ .
 - » Obtain decay vertex point.
- **Reconstruct D production point.**
 - » Pseudo D track and IP profile.
 - Calculate proper time.
 - » $\tau = L^* m(D) / c^* p_D$



D Lifetime Fit



Event by event P.D.F. (probability density function).

$$P(t) = f_{SIG} \int_0^{\infty} dt' \frac{1}{\tau_{SIG}} e^{-t'/\tau_{SIG}} R_{SIG}(t-t')$$

$$+ (1 - f_{SIG}) \int_0^{\infty} dt' [f_{\tau BG} \frac{1}{\tau_{BG}} e^{-t'/\tau_{BG}} + (1 - f_{\tau BG}) \delta(t')] R_{BG}(t-t'),$$

$$R(x) = (1 - f_{tail}) \cdot G(x; S\sigma_t) + f_{tail} \cdot G(x; S_{tail}\sigma_t),$$

$$G(x; \sigma) \equiv \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{x^2}{2\sigma^2}},$$

» τ_D : D lifetime.

» f_{sig} (D mass): signal probability calculated event by event.

» τ_{BG} : Lifetime of BG component.

» $f_{\tau BG}$: Fraction of BG with lifetime.

◆ Resolution function = $(1-f_{tail}) * G(S^* \sigma_\tau) + f_{tail} * G(S_{tail}^* \sigma_\tau)$

» σ_τ : Error of proper-time calculated from track error event by event.

» S , S_{tail} : Global scaling factors.

» f_{tail} : Fraction of the tail part.

◆ Free parameters: τ_D , τ_{BG} , $f_{\tau BG}$, S , S_{tail} , f_{tail} , $(S, S_{tail}, f_{tail})_{BG}$

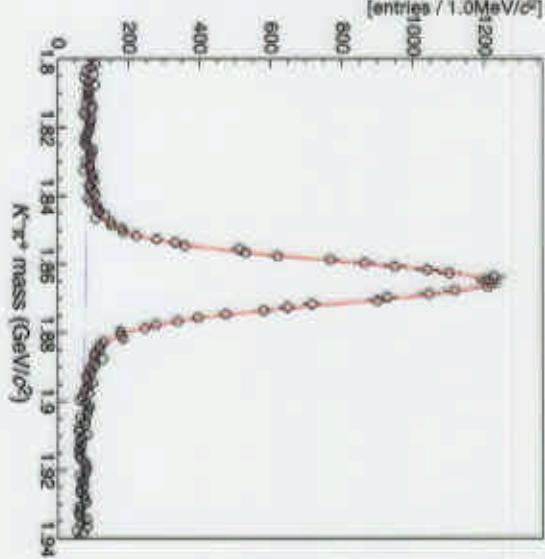
$D^0 \rightarrow K^- \pi^+$ Lifetime Fit



$$\tau_D = (414.8 \pm 3.8 \pm 3.4) \text{ fs}$$

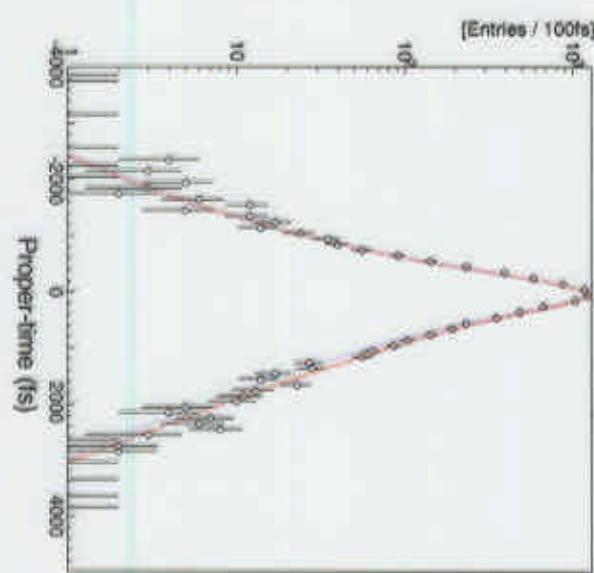
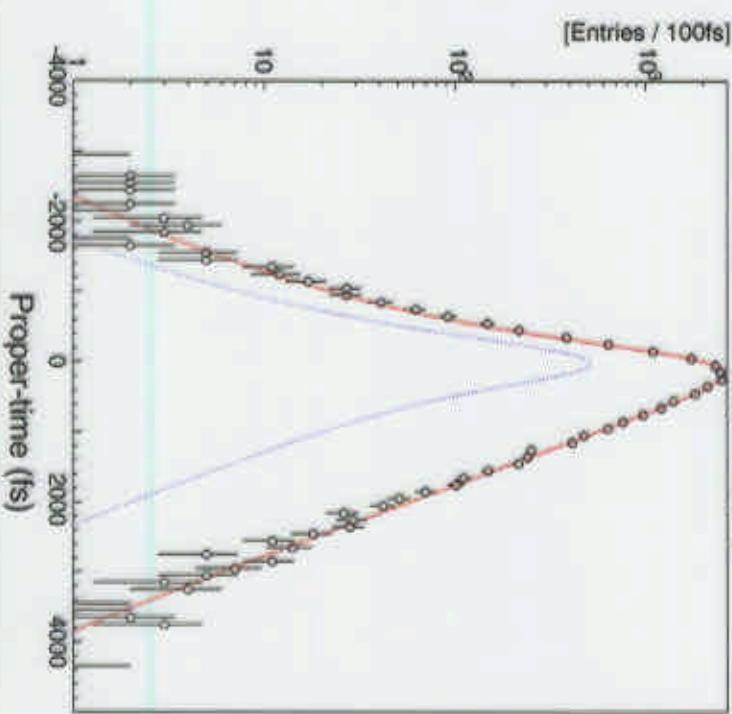
Signal region ($<3\sigma$)

$D^0 \rightarrow K^- \pi^+$ (signal region)



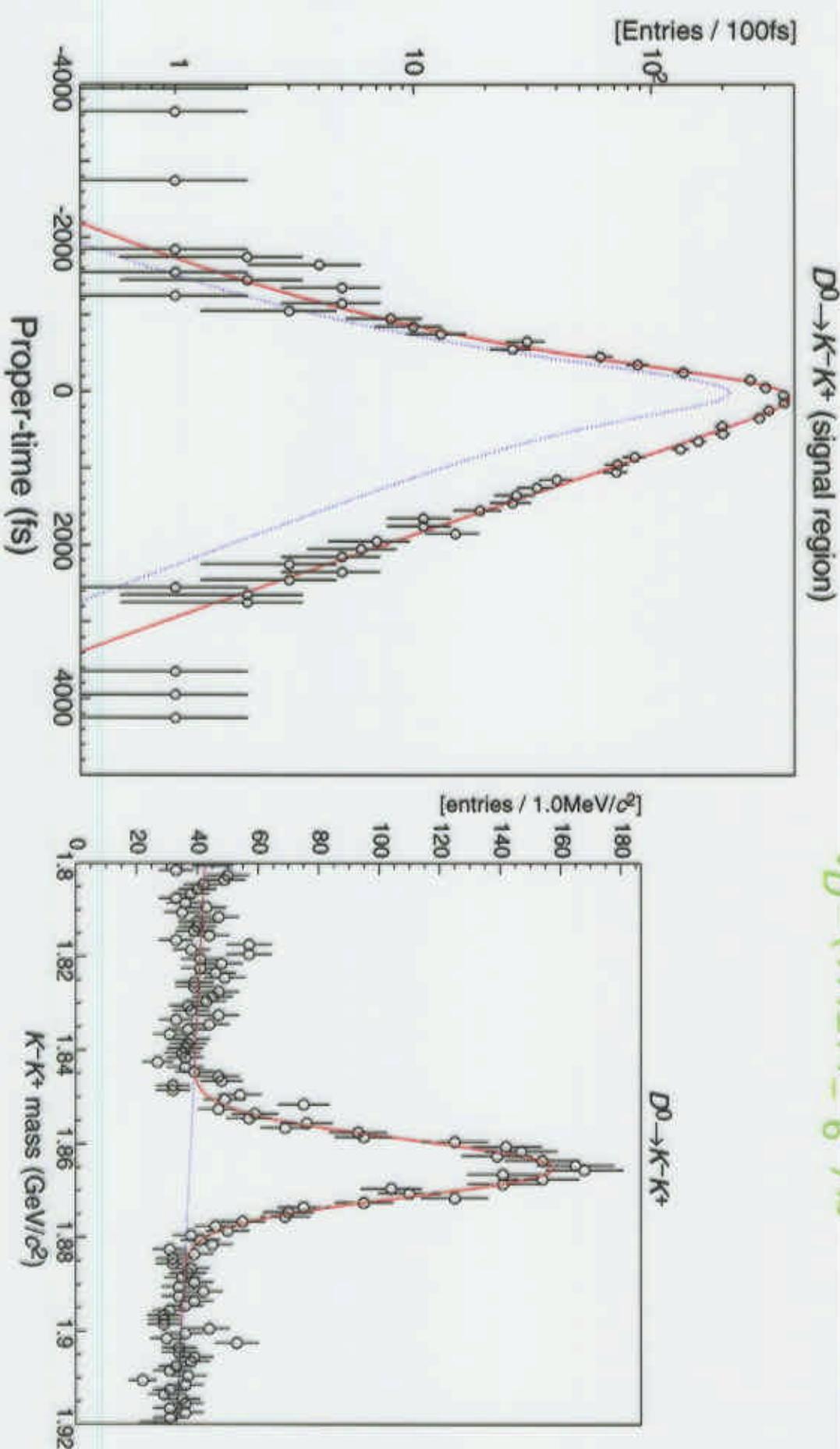
BG region ($>3\sigma$)

$D^0 \rightarrow K^- \pi^+$ (sidelband region)



$D^0 \rightarrow K^- K^+$ Lifetime Fit

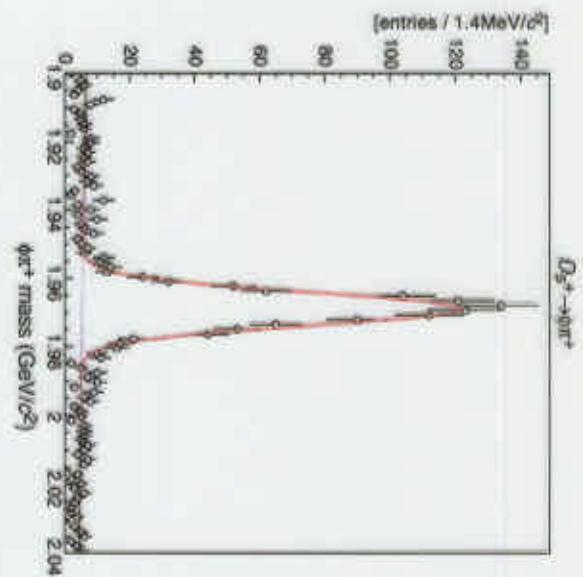
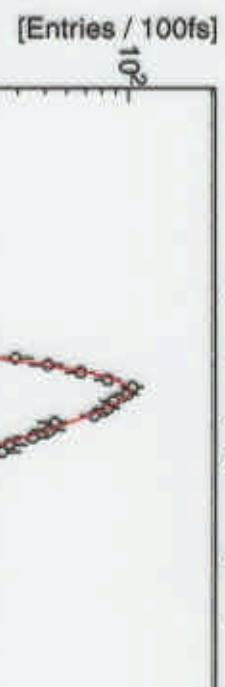
$$\tau_D = (411 \pm 14^{+10}_{-6}) \text{ fs}$$



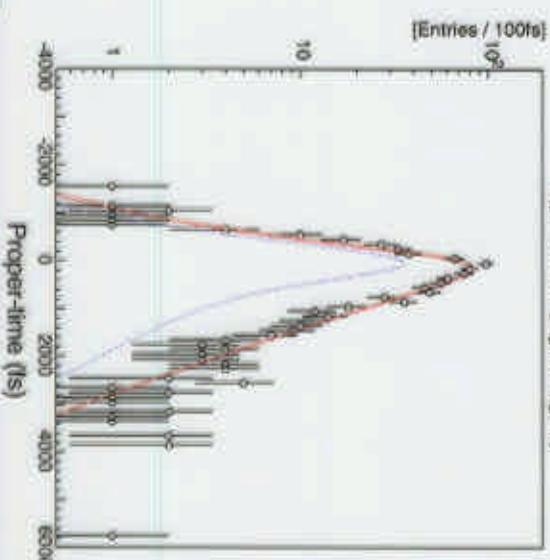
D_s^+ Lifetime Fit



$$\tau_D = 470 \pm 19^{+8}_{-7} \text{ fs}$$



$$\tau_D = 505^{+34+6}_{-33-12} \text{ fs}$$

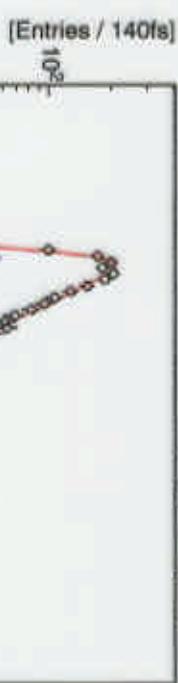


D^+ Lifetime Fit



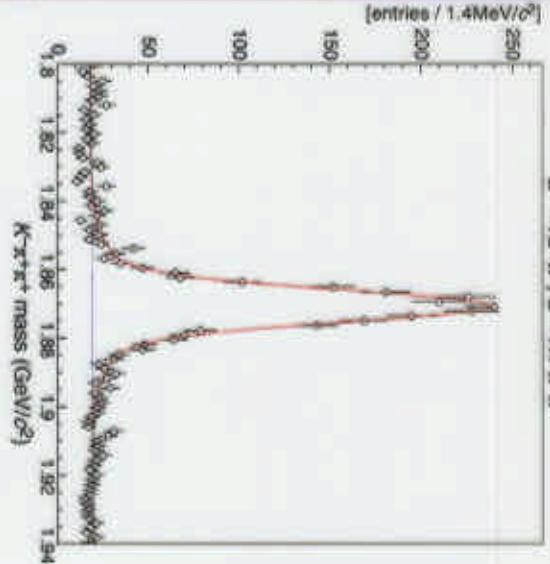
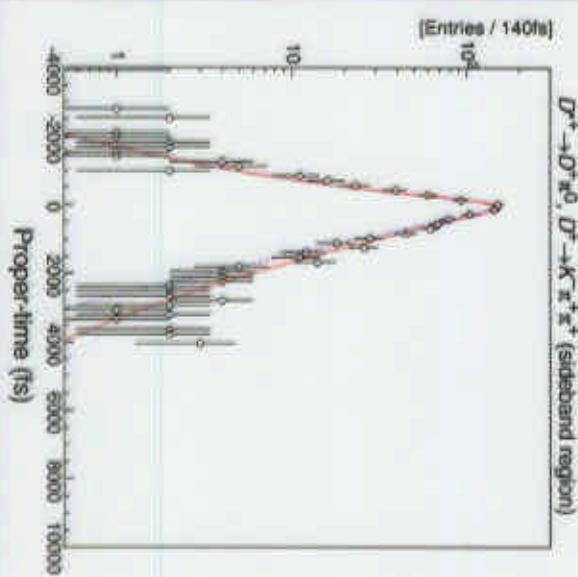
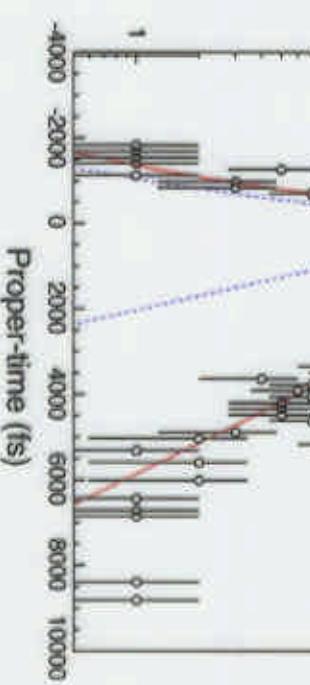
$$\tau_D = 1049^{+25+16}_{-24-19}$$

$D^+ \rightarrow D^+ \pi^0, D^+ \rightarrow K^- \pi^+ \pi^+$ (signal region)



$$\tau_D = 974^{+68+26}_{-62-18} \text{ fs}$$

$D^+ \rightarrow \eta \pi^+$ (signal region)



Systematic Error



Source	$D^0 \rightarrow K^- \pi^+$	$D^0 \rightarrow K^- K^+$	$D_s^+ \rightarrow \phi \pi^+$	$D^+ \rightarrow K^- \pi^+ \pi^+$
IP	+0.2 -0.3	+1.3 -0.4	+1.0 -1.6	+10 -13
Efficiency	±1.8	±1.8	±2.1	±8
Vertexing cuts	±1.0	±2.2	+3.3 -0.5	+7 -3
Decay vertex	±1.9	±1.8	±2.0	±2
Resolution function	+1.5 -1.7	+3.4 -3.6	±1.9	+3 -2
Background fraction	+1.0 -0.4	+8.3 -3.1	+1.5 -2.8	+6 -10
D -mass sideband region	+0.0 -0.6	+0.0 -0.6	-1.1 -0.6	+1 -2
Total	±3.4 +9.7 -5.9	+5.1 -7.0	+16 -19	

B Proper-time Reconstruction

Reconstruction.

- ♦ **Reconstruct specific B decay modes.**

» $\bar{B}^0 \rightarrow D^{*+} \ell^- \nu, (D^{*+} \rightarrow D^0 \pi^+, D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-)$

"Reconstructed" B vertexing

» $B^- \rightarrow D^{*0} \ell^- \nu, (D^{*0} \rightarrow D^0 \pi^0, D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-)$

IP profile

» $\bar{B}^0 \rightarrow D^{*+} \pi^-, B^0 \rightarrow D^+ \pi^-, B^- \rightarrow D^0 \pi^-, (D^+ \rightarrow K^- \pi^+ \pi^+)$

» $\bar{B}^0 \rightarrow \psi K_S, \bar{B}^0 \rightarrow \psi K^0, B^- \rightarrow \psi K^-$

» Obtain decay vertex point.

- ♦ **Reconstruct B decay point.**

» Lepton track, Pseudo D track and IP profile ($D^{*+} \ell^- \nu, D\pi$)

» Two lepton tracks (ψK)

» IP constraint fit.

- IP profile is smeared by B flight length in xy plane.

- ♦ **Reconstruct "tagging"-side B vertex.**

» No flavor tag.

» IP constraint fit.

- ♦ **Calculate proper time.**

» $\Delta t = \Delta z / c \beta \gamma$

"Associated"- B vertexing

IP profile

B primary tracks



B Lifetime Fit



Event by event P.D.F. (probability density function).

$$P(\Delta t) = f_{\text{sig}} \int_{-\infty}^{\infty} d(\Delta t') \frac{e^{-i\Delta t' \mu_{\text{BG}}}}{2\tau_{\text{sig}}} R_{\text{sig}}(\Delta t - \Delta t') + (1 - f_{\text{sig}}) \int_{-\infty}^{\infty} d(\Delta t') [f_{\lambda_{\text{BG}}} \frac{\lambda_{\text{BG}}}{2} e^{-i\Delta t' \lambda_{\text{BG}}} + (1 - f_{\lambda_{\text{BG}}}) \delta(\Delta t')] R_{\text{BG}}(\Delta t - \Delta t')$$

Signal term

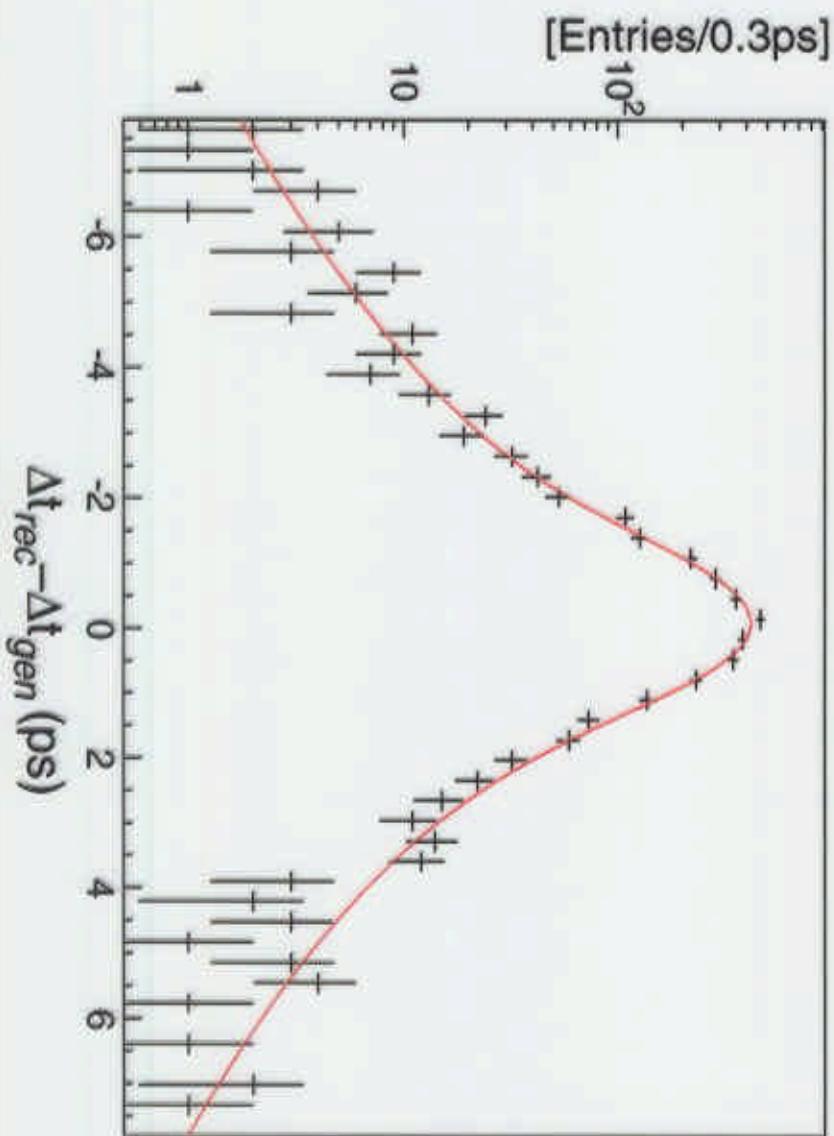
Background term

- » τ_B : B lifetime.
- » f_{sig} : signal probability calculated event by event. (ΔM , or ΔE -Mb sideband)
- » τ_{BG} : Lifetime of BG component.
- » $f_{\tau_{\text{BG}}}$: Fraction of BG with lifetime.
- ♦ $R_{\text{SIG}} = (1 - f_{\text{tail}})^* G(\mu, S^* \sigma_{\Delta \tau}) + f_{\text{tail}}^* G(\mu_{\text{tail}}, S_{\text{tail}}^* \sigma_{\Delta \tau})$
- » μ : Mean value shift of $\Delta \tau$ (due to charm contribution).
- » $\sigma_{\Delta \tau}$: Error of proper-time calculated from error matrix event by event.
- » S : Global scaling factor (obtained from D^0 data sample).
- » S_{tail} : Scaling factor for the tail part of the resolution function.
- Hard scattering, mis-association of SVD hits.
- » f_{tail} : Fraction of the tail part.
- ♦ Free parameters: τ_B , τ_{BG} , $f_{\tau_{\text{BG}}}$, S_{tail} , f_{tail}

Resolution Function

Resolution function

- Sum of many Gaussian.
- Utilize the vertex error calculated from track error.
 - » It can incorporate event by event resolution difference.
- Use larger scaling factor for the vertex with $\chi^2/n > 3$.



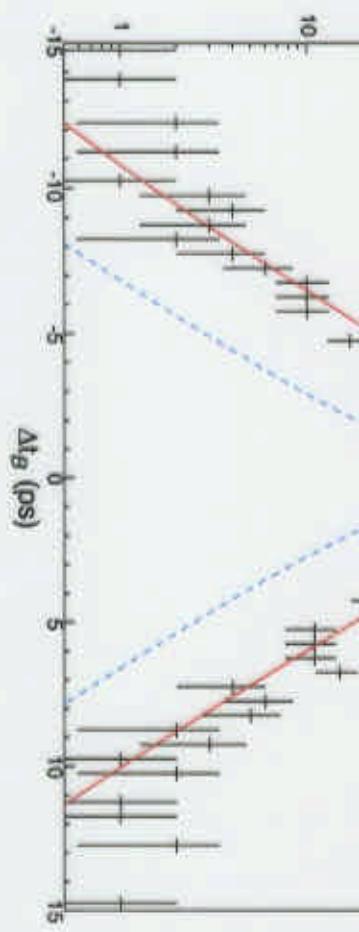
$B \rightarrow D^* \ell \nu$ Lifetime Fit



$\bar{B}^0 \rightarrow D^{*+} \ell^- \nu$ (signal region)

$$(1.50 \pm 0.06^{+0.05}_{-0.04}) \text{ ps}$$

[Entries/0.5ps]

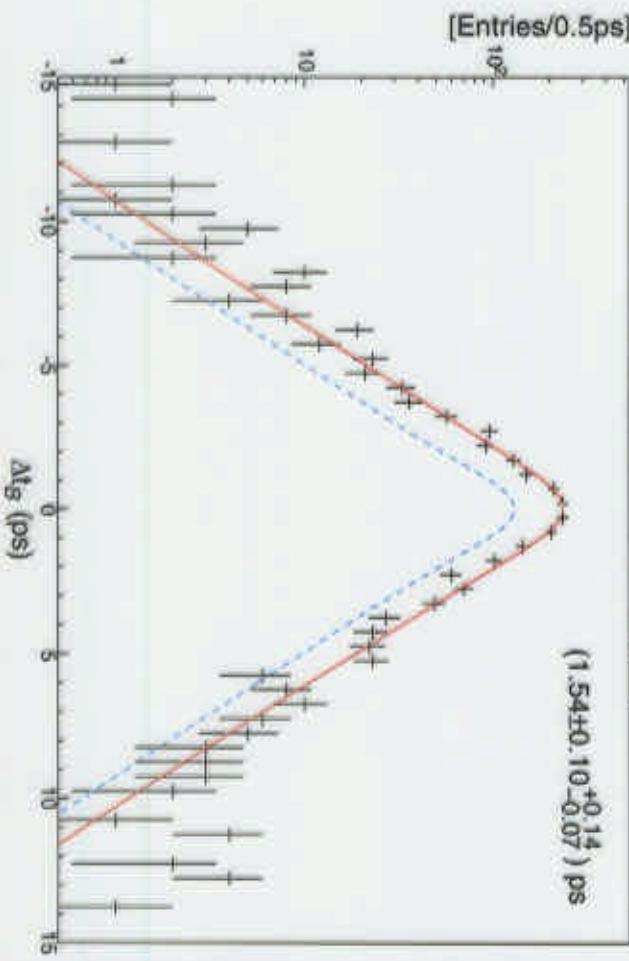


$\bar{B}^0 \rightarrow D^{*+} \ell^- \nu$ (signal region)

$B^- \rightarrow D^{*-} \ell^+ \nu$ (signal region)

$$(1.54 \pm 0.10^{+0.14}_{-0.07}) \text{ ps}$$

[Entries/0.5ps]



$B \rightarrow D\pi$ Lifetime Fit



$\bar{B}^0 \rightarrow D^{*+}\pi^-$ (signal region)

$$(1.55^{+0.18+0.10}_{-0.17-0.07}) \text{ ps}$$

[Entries/0.6ps]

[Entries/0.6ps]

$B \rightarrow D^0\pi^-$ (signal region)

$$(1.73 \pm 0.10 \pm 0.09) \text{ ps}$$

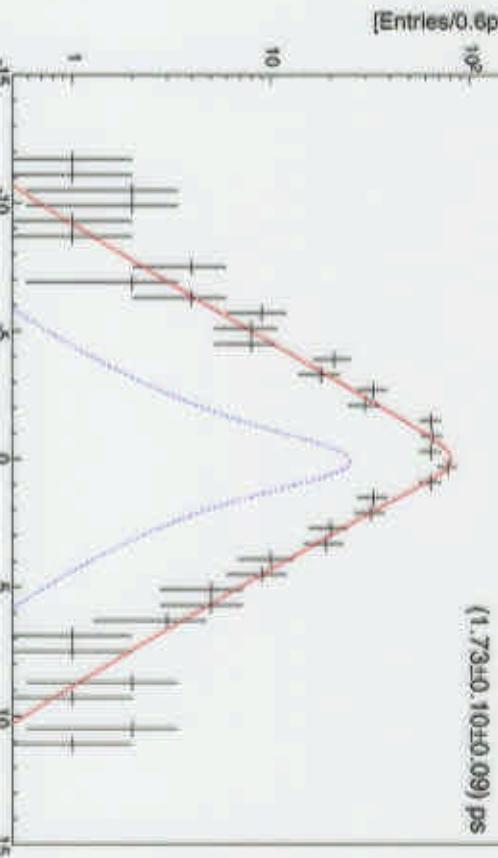
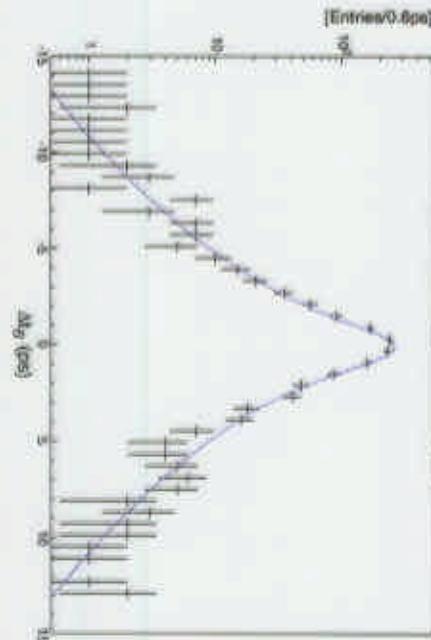
$\bar{B}^0 \rightarrow D^+\pi^-$ (signal region)

$$(1.41^{+0.13}_{-0.12} \pm 0.07) \text{ ps}$$

[Entries/0.6ps]

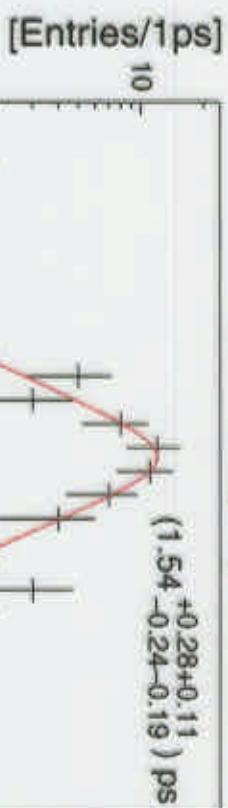
[Entries/0.6ps]

$\bar{B}^0 \rightarrow D^0\pi^-$ (sideband region)



$B \rightarrow \psi K$ Lifetime Fit

$\bar{B}^0 \rightarrow J/\psi K_S$

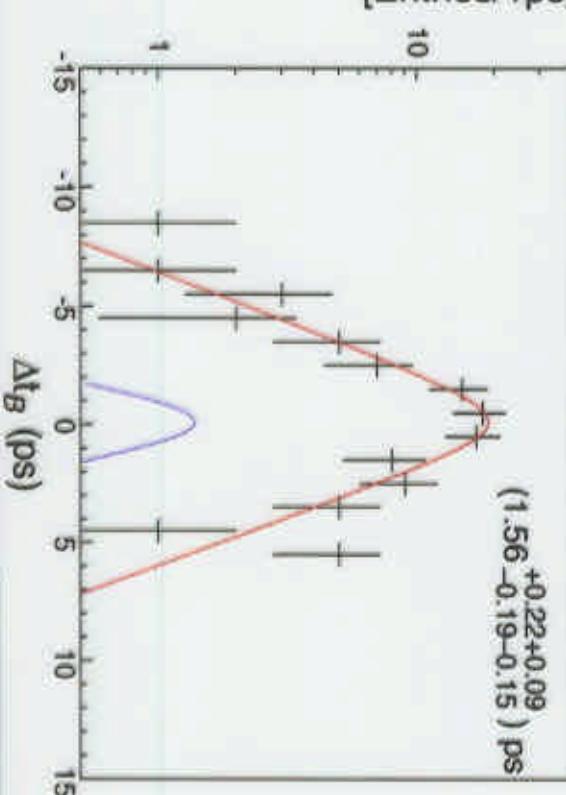


$\bar{B}^0 \rightarrow J/\psi \bar{K}_S$

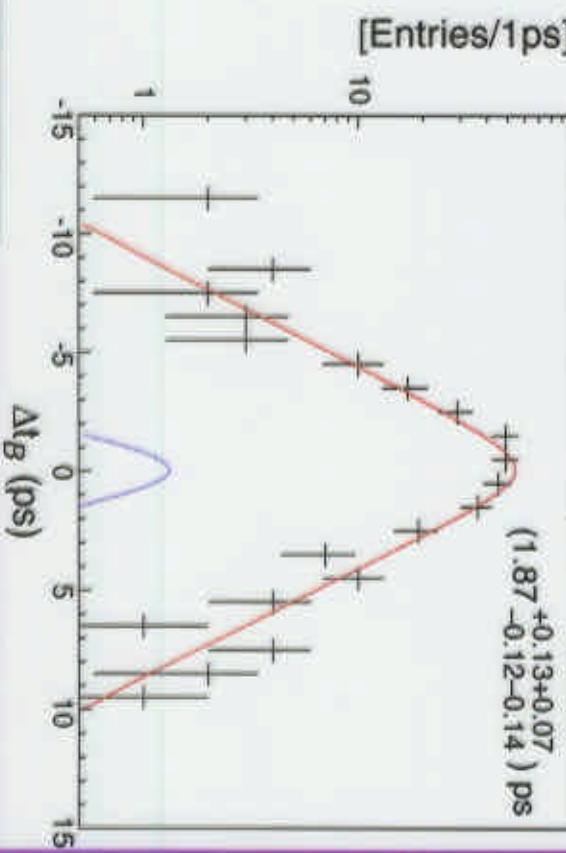
$\Delta t_B \text{ (ps)}$

$(1.56^{+0.22+0.09}_{-0.19-0.15}) \text{ ps}$

[Entries/1ps]



[Entries/1ps]



B Lifetime Summary

\bar{B}^0 lifetime measurements.

Mode	# of signal	Lifetime (ps)
$\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}$	1740	$1.50 \pm 0.06^{+0.06}_{-0.04}$
$\bar{B}^0 \rightarrow D^{*+} \pi^-$	112	$1.55^{+0.18}_{-0.17}{}^{+0.10}_{-0.07}$
$\bar{B}^0 \rightarrow D^+ \pi^-$	187	$1.41^{+0.13}_{-0.12} \pm 0.07$
$\bar{B}^0 \rightarrow J/\psi \bar{K}^{*0}$	92	$1.56^{+0.22}_{-0.19}{}^{+0.09}_{-0.15}$
Combined	-	$1.50 \pm 0.05 \pm 0.07$
$\bar{B}^0 \rightarrow J/\psi K_S$	55	$1.54^{+0.28}_{-0.24}{}^{+0.11}_{-0.19}$

B^- lifetime measurements.

Mode	# of signal	Lifetime (ps)
$B^- \rightarrow D^{*0} \ell^- \bar{\nu}$	730	$1.54 \pm 0.10^{+0.14}_{-0.07}$
$B^- \rightarrow D^0 \pi^-$	440	$1.73 \pm 0.10 \pm 0.09$
$B^- \rightarrow J/\psi K^-$	293	$1.87^{+0.13}_{-0.12}{}^{+0.07}_{-0.14}$
Combined	-	$1.70 \pm 0.06^{+0.11}_{-0.10}$

$$\tau(B^-) / \tau(\bar{B}^0) = 1.14 \pm 0.06^{+0.06}_{-0.05}$$

$$y_{CP} = 0.03^{+0.15}_{-0.18}{}^{+0.05}_{-0.08} \quad (-0.36 < y_{CP} < 0.35 @ 95\% C.L.)$$



Summary



D lifetime results

- Factor of 1.5 improvement is expected with full data set by summer.

Experiment	$\tau(D^0)$ fs	$\tau(D^+)$ fs	$\tau(D_s^+)$ fs	y_{CP} %
PDG99	415 ± 4	1057 ± 15	495 ± 13	—
E791	$413 \pm 3 \pm 4$	—	$518 \pm 14 \pm 7$	$0.8 \pm 2.9 \pm 1.0$
CLEO	$408.5 \pm 4.1^{+3.5}_{-3.4}$	$1034 \pm 22^{+10}_{-13}$	$486 \pm 15 \pm 5$	—
FOCUS	409.2 ± 1.3	—	506 ± 8	$3.42 \pm 1.39 \pm 0.74$
Belle	$414.8 \pm 3.8 \pm 3.4$	$1040^{+23}_{-22} \pm 18$	479^{+17+6}_{-16-8}	$1.0^{+3.8+1.1}_{-3.5-2.1}$ $-7.0 < y_{CP} < 8.7$

B lifetime results

Experiment	$\tau(\bar{B}^0)$ (ps)	$\tau(B^-)$ (ps)	y_{CP}
<i>B</i> lifetime WG	1.548 ± 0.032	1.653 ± 0.028	—
CLEO	—	—	$ y < 0.41 @ 95\% \text{ C.L.}$
Belle	$1.50 \pm 0.05 \pm 0.07$	$1.70 \pm 0.06^{+0.11}_{-0.10}$	$y_{CP} = 0.03^{+0.15+0.05}_{-0.18-0.08}$ $-0.36 < y_{CP} < 0.35$

All results are preliminary.