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**CONSTRAINTS ON  $g(x, \mu_f^2)$  AND  $\Delta g(x, \mu_f^2)$   
FROM LEPTON PAIR PRODUCTION**

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Outline:

- Introduction
- Next-to-Leading Order QCD Formalism
- Differential Cross Sections at Fixed Target and Collider Energies
- Longitudinal Spin Asymmetries at RHIC
- Summary

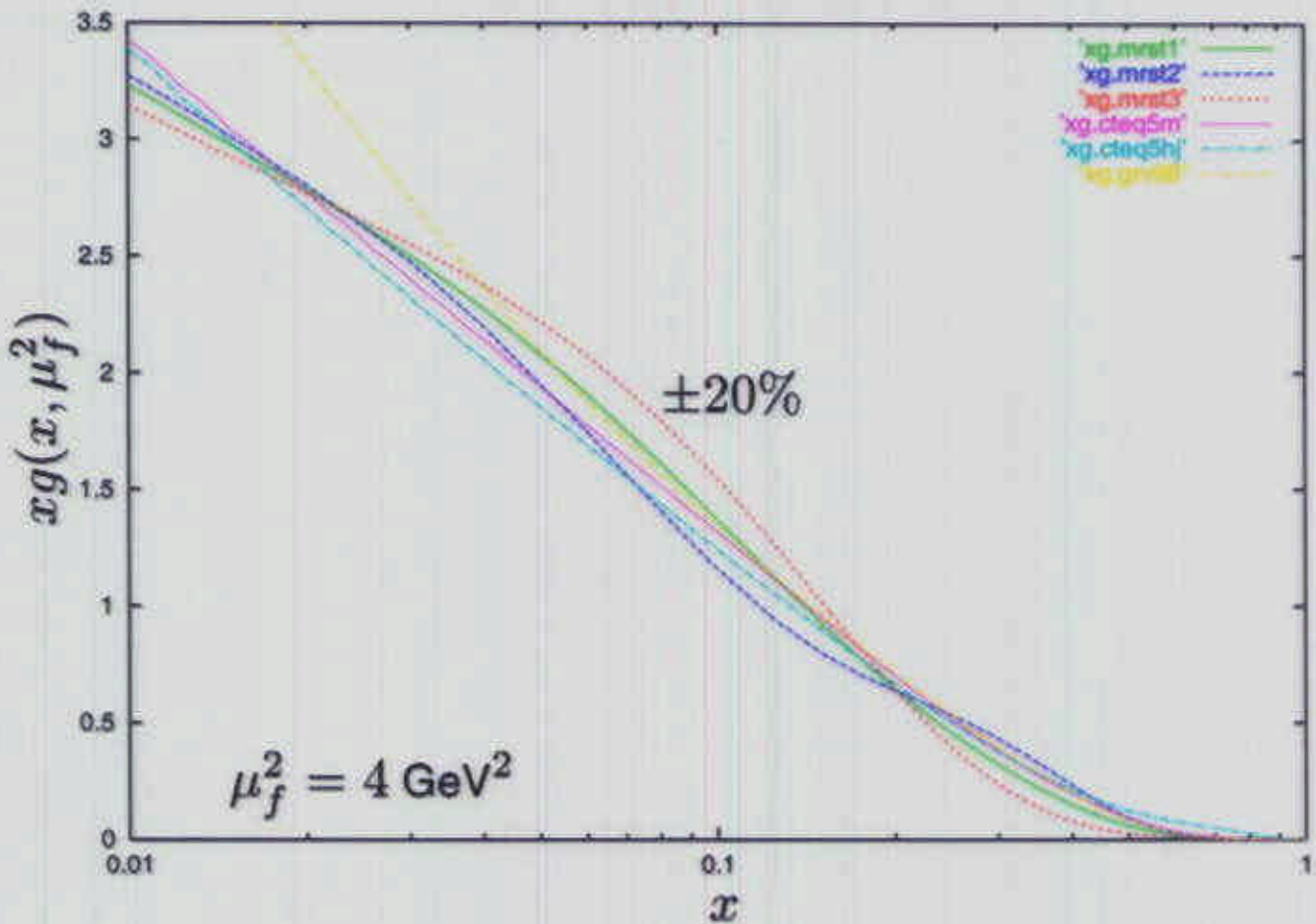
E.L. Berger, L.E. Gordon, M.Klasen, Phys.Rev. D58, 074012 (1998)

E.L. Berger, M.Klasen, Nucl.Phys.Proc.Suppl. 82, 179 (2000)

E.L. Berger, L.E. Gordon, M.Klasen, Phys.Rev. D62, 014014 (2000)

<http://gate.hep.anl.gov/berger/seminars/ICHEPQCD.ps>

## UNPOLARIZED GLUON DISTRIBUTIONS



- A.Martin, R.Roberts, W.Stirling, R.Thorne, Eur.Phys.J. C4, 463 (1998):  

$$xg(x, \mu_0^2 = 1.0\text{GeV}^2) = A_g x^{-\lambda_g} (1-x)^{\eta_g} (1 + \epsilon_g \sqrt{x} + \gamma_g x)$$
- H.L. Lai *et al.* [CTEQ Collaboration], hep-ph/9903282:  

$$xg(x, \mu_0^2 = 1.0\text{GeV}^2) = A_g x^{-\lambda_g} (1-x)^{\eta_g} (1 + \gamma_g x^{A_4})$$
- M. Glück, E. Reya and A. Vogt, Eur. Phys. J. C5, 461 (1998):  

$$xg(x, \mu_0^2 = 0.4\text{GeV}^2) = A_g x^{-\lambda_g} (1-x)^{\eta_g}$$
- H1/ZEUS:  

$$xg(x, \mu_0^2 = 2/7\text{GeV}^2) = A_g x^{-\lambda_g} (1-x)^{\eta_g} (1 + \gamma_g x)$$
- W. Giele, S. Keller, D. Kosower, Phys. Rev. D58, 094023 (1998):  

$$xg(x, \mu_0^2 = 9.0\text{GeV}^2) = A_g x^{-\lambda_g} (1-x)^{\eta_g}$$



## NEW CONSTRAINT: LEPTON PAIR PRODUCTION

- Massive lepton pair production dominated by  $q\bar{q} \rightarrow \gamma^* X$   
 "Drell-Yan process", traditionally  $M_{\gamma^*} = Q$  large,  $Q_T^2$  small  
 → Extract  $\bar{q}(x, \mu_f^2 = Q^2)$  and  $\Delta\bar{q}(x, \mu_f^2 = Q^2)$  from data  
 Complementary to DIS → Extract  $(q + \bar{q})(x, \mu_f^2 = Q^2)$
- Prompt photon production dominated by  $qg \rightarrow \gamma X$ :  
 "QCD Compton process", traditionally  $p_T^2$  large,  $Q^2 = 0$   
 → Extract  $g(x, \mu_f^2 = p_T^2)$  and  $\Delta g(x, \mu_f^2 = p_T^2)$  from data
- Partonic subprocesses at finite  $Q_T, p_T$  are identical:
  - $q\bar{q} \rightarrow \gamma^{(*)} g$
  - $qg \rightarrow \gamma^{(*)} q$
  - Higher order processes
- Focus on modest mass, large transverse momentum,  
 $Q_T > Q/2$
- Lepton pair production dominated by QCD Compton process  
 → Extract  $g(x, \mu_f^2)$  and  $\Delta g(x, \mu_f^2)$  from data
- Relation between lepton pair and virtual photon production

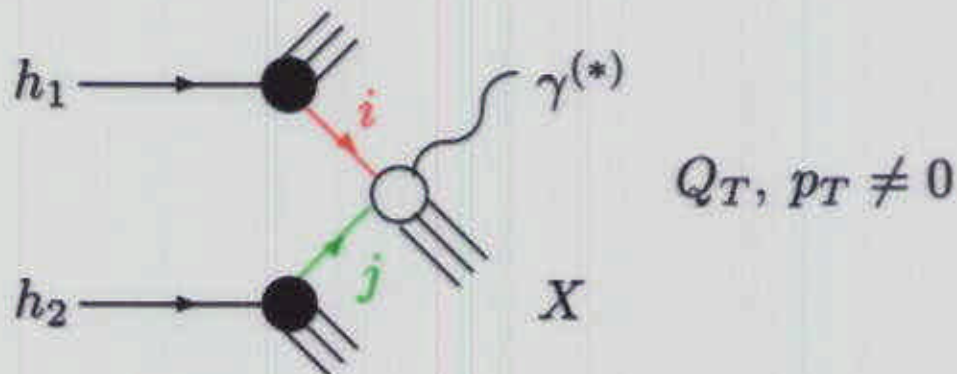
$$\frac{d^3 \sigma_{h_1 h_2}^{l\bar{l}}}{dQ^2 dQ_T^2 dy} = \left( \frac{\alpha_{em}}{3\pi Q^2} \right) \frac{d^2 \sigma_{h_1 h_2}^{\gamma^*}}{dQ_T^2 dy}(S, Q, Q_T, y)$$

"Drell-Yan factor" included in results for  $h_1 h_2 \rightarrow \gamma^* X$

## LEPTON PAIR PRODUCTION

- Advantages:
  - No non-perturbative fragmentation contribution  
→ Phenomenologically cleaner
  - No need to isolate the photon experimentally  
→ Reduces systematic uncertainty  
→ Removes theoretical infrared uncertainty
  - No need for intrinsic  $\langle k_T \rangle$
- Drawbacks:
  - Cross section lower due to “Drell-Yan factor”
  - Range in  $x_g \simeq x_T = \frac{2Q_T}{\sqrt{S}}$  more limited
- Despite more restricted reach, valuable to investigate  $g(x, \mu)$  with a process that has reduced experimental and theoretical systematic uncertainties with respect to prompt photon and hadronic jet production
- Suggestions:
  - Look at regions of low  $Q \simeq 2 \text{ GeV}$ ,  $Q_T$  large perturbation theory still valid
  - Use large bins in  $Q$
  - Avoid  $\rho$ ,  $J/\Psi$ ,  $\Upsilon$  resonances
  - Use otherwise neglected data

## NEXT-TO-LEADING ORDER QCD FORMALISM



- Factorization:

$$\frac{d^2 \sigma_{h_1 h_2}^{\gamma^*}}{dQ_T^2 dy} = \sum_{ij} \int dx_1 dx_2 f_{h_1}^i(x_1, \mu_f^2) f_{h_2}^j(x_2, \mu_f^2) \frac{sd^2 \hat{\sigma}_{ij}^{\gamma^*}}{dt du}(s, Q, Q_T, y; \mu_f^2)$$

$$\frac{d^2 \Delta \sigma_{h_1 h_2}^{\gamma^*}}{dQ_T^2 dy} = \sum_{ij} \int dx_1 dx_2 \Delta f_{h_1}^i(x_1, \mu_f^2) \Delta f_{h_2}^j(x_2, \mu_f^2) \frac{sd^2 \Delta \hat{\sigma}_{ij}^{\gamma^*}}{dt du}(s, Q, Q_T, y)$$

$\mu_f$  = Factorization Scale

- Expansion in  $\alpha_s$ :

$$\frac{d^2 \hat{\sigma}_{ij}^{\gamma^*}}{dt du} = \alpha_s(\mu^2) \frac{d^2 \hat{\sigma}_{ij}^{\gamma^*}, (a)}{dt du} + \alpha_s^2(\mu^2) \frac{d^2 \hat{\sigma}_{ij}^{\gamma^*}, (b)}{dt du} + \alpha_s^3(\mu^2) \frac{d^2 \hat{\sigma}_{ij}^{\gamma^*}, (c)}{dt du} + \mathcal{O}(\alpha_s^3)$$

$\mu$  = Renormalization Scale

2-loop  $\alpha_s$  with 5 flavors

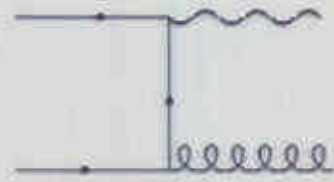
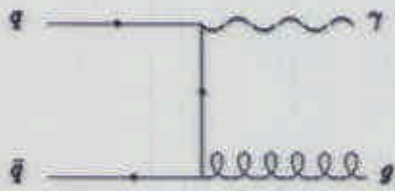
- Choice of Scales:

$$\mu_f = \mu = \sqrt{Q^2 + Q_T^2} \xrightarrow{Q^2 \rightarrow 0} p_T$$

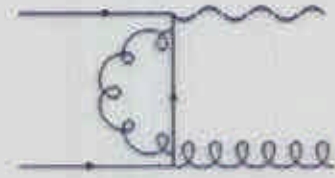


## NEXT-TO-LEADING ORDER QCD FORMALISM

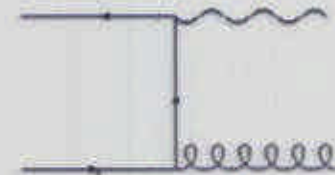
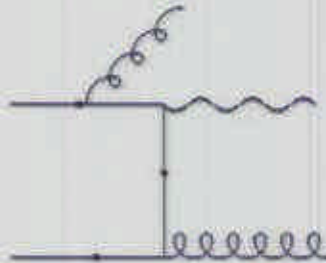
•  $q\bar{q} \rightarrow \gamma^{(*)} X$



(a)



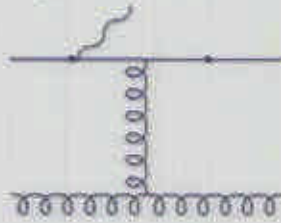
(b)



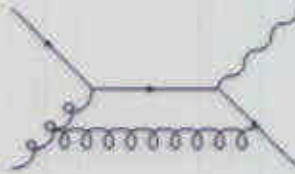
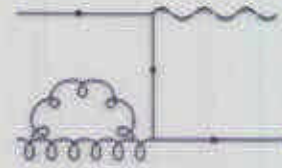
(c)

NEXT-TO-LEADING ORDER QCD FORMALISM

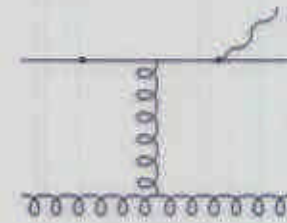
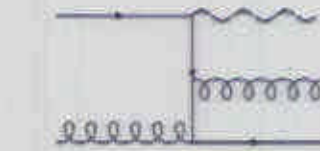
•  $qg \rightarrow \gamma^{(*)} X$



(a)



(b)



(c)

## NEXT-TO-LEADING ORDER QCD FORMALISM

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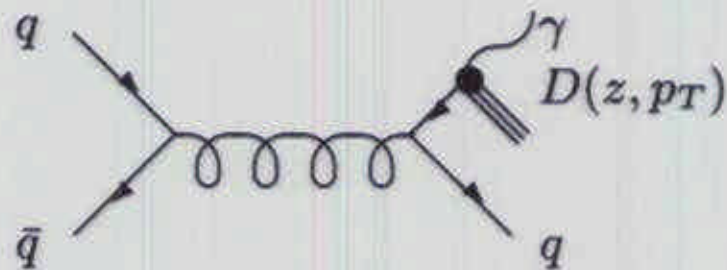
- Gluon emission and gluon loop corrections to the LO  $\mathcal{O}(\alpha_s)$   $q\bar{q} \rightarrow g\gamma^{(*)}$  and  $gq \rightarrow q\gamma^{(*)}$  subprocesses
- Real  $\mathcal{O}(\alpha_s^2)$  subprocesses without  $\mathcal{O}(\alpha_s)$  counterparts:
  - $qq \rightarrow qq\gamma^{(*)}$
  - $gg \rightarrow q\bar{q}\gamma^{(*)}$
  - $q\bar{q} \rightarrow q\bar{q}\gamma^{(*)}$
- Complete set is included in our NLO calculations:
  - Lepton pair production
  - Prompt photon production
- Dimensional regularization: Integration in  $4 - 2\epsilon$  dimensions
- $\overline{\text{MS}}$  renormalization scheme removes UV singularities
- KLN-cancellation of virtual and real IR singularities
- Polarized lepton pair production: Only LO results available
- Correspondence of lepton pair and prompt photon production for the **"Direct Contribution"**:

$$\frac{d^2\sigma_{h_1 h_2}^{\gamma^*}}{dQ_T^2 dy}(S, Q, Q_T, y) \xrightarrow{Q \rightarrow 0} \frac{d^2\sigma_{h_1 h_2}^{\gamma}}{dp_T^2 dy}(S, p_T, y)$$



## NEXT-TO-LEADING ORDER QCD FORMALISM

- Important difference: Prompt photon has a long-distance non-perturbative **"Fragmentation Contribution"**



- Hard partonic subprocess is  $\mathcal{O}(\alpha_s^2)$
- Asymptotic behavior of the fragmentation function:

$$D(z, p_T) \sim \ln p_T^2 \sim \mathcal{O}(\alpha_s^{-1})$$

- Hadronic cross section is  $\mathcal{O}(\alpha_s)$  as the LO direct contribution
- Phenomenologically important at small  $p_T$
- Related to NLO collinear quark-photon singularity:



(a)



(b)



## NEXT-TO-LEADING ORDER QCD FORMALISM

- Prompt photon cross section:

$$\frac{1}{\epsilon} 2K_\gamma \frac{-(t^2 + u^2)(2s^2 + 2st + t^2 + 2su + 2tu + u^2)}{s(t+u)^4} = \frac{1}{\epsilon} f(s, t, u)$$

Dimensional regularization:  $1/\epsilon$  pole

- Drell-Yan cross section:

$$\begin{aligned} & \ln \left[ \frac{s + Q^2 - s_2 + \lambda}{s + Q^2 - s_2 - \lambda} \right] K_{DY} \\ & \left[ \frac{1}{\lambda^5} \left( \frac{3Q^2 u^2 (u-t)(t+u-2s_2)}{s} + \frac{3(s-Q^2)u^2(u^2-t^2)}{Q^2 + s - s_2} \right) \right. \\ & + \frac{1}{\lambda^3} \left( \frac{u(2ss_2 - 2s_2^2 + 2s_2t - su + 4s_2u - tu - 3u^2)}{s} \right. \\ & \quad \left. \left. + \frac{u^2}{Q^2 + s - s_2} \left( -2s - t + \frac{t^2}{s} + 3u - \frac{u^2}{s} \right) \right) \right. \\ & \left. + \frac{1}{\lambda} \left( \frac{1}{s} \left( \frac{3s}{4} - \frac{s_2}{2} + u \right) + \frac{1}{Q^2 + s - s_2} \left( \frac{3s}{2} + \frac{5u}{2} + \frac{2u^2}{s} \right) \right) \right] \\ & + (t \leftrightarrow u) \\ & = \ln \left[ \frac{s + Q^2 - s_2 + \lambda}{s + Q^2 - s_2 - \lambda} \right] g(s, t, u, Q^2). \end{aligned}$$

with  $\lambda = \sqrt{(t+u)^2 - 4Q^2 s_2}$  and  $s_2 = s + t + u - Q^2$ .

Mass regularization: No  $1/\epsilon$  pole, instead  $\ln Q^2$  terms

- $K_\gamma, K_{DY}$  contain color, electric charge, phase space factors
- $g(s, t, u, Q^2) \xrightarrow{Q^2 \rightarrow 0} f(s, t, u)$ . It contains
  - Altarelli-Parisi splitting function  $P_{q \rightarrow \gamma}(z)$
  - Born matrix element  $\hat{\sigma}^{q\bar{q}}$

## CROSS SECTIONS AT FIXED TARGET AND COLLIDER ENERGIES

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### DIFFERENTIAL CROSS SECTIONS AT FIXED TARGET AND COLLIDER ENERGIES

- Collider experiments:

- $p\bar{p} \rightarrow \gamma^{(*)} X$  at  $\sqrt{S} = 1.8 - 2.0$  TeV (CDF, D0)
- $pp \rightarrow \gamma^{(*)} X$  at  $\sqrt{S} = 50 - 500$  GeV (RHIC)
- $pp \rightarrow \gamma^{(*)} X$  at  $\sqrt{S} = 14$  TeV (LHC)
- $p\bar{p} \rightarrow \gamma^{(*)} X$  at  $\sqrt{S} = 630$  GeV (UA1)

- Fixed target experiments:

- $pN \rightarrow \gamma^* X$  at  $p_{\text{lab}} = 800$  GeV,  $N = {}^2\text{H}$  (E772)
- $pN \rightarrow \gamma^* X$  at  $p_{\text{lab}} = 820$  GeV,  $N = \text{C, Ti, Al, W}$  (HERA-B)

- Study size of cross sections as a function of  $Q_T, p_T$  for

- Prompt photon production
- Lepton pair production

- Demonstrate accessibility of lepton pair production

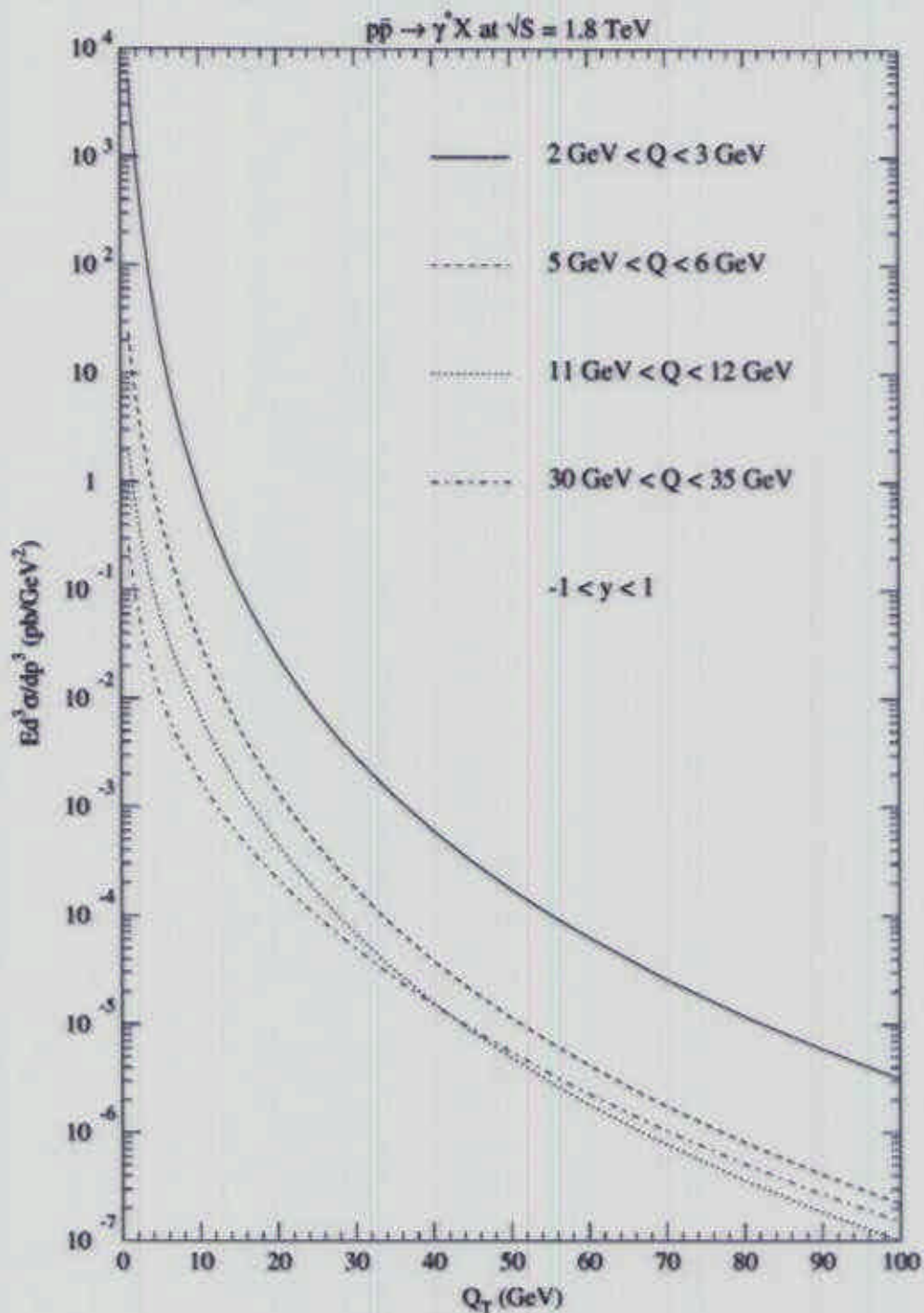
- Show dominance of  $qg$  incident channel for  $Q_T > Q/2$

- Test sensitivity to parton (gluon) densities:

- CTEQ (4M, 5M, 5HJ)
- MRST (central gluon,  $g \uparrow, g \downarrow$ )
- GRV 98

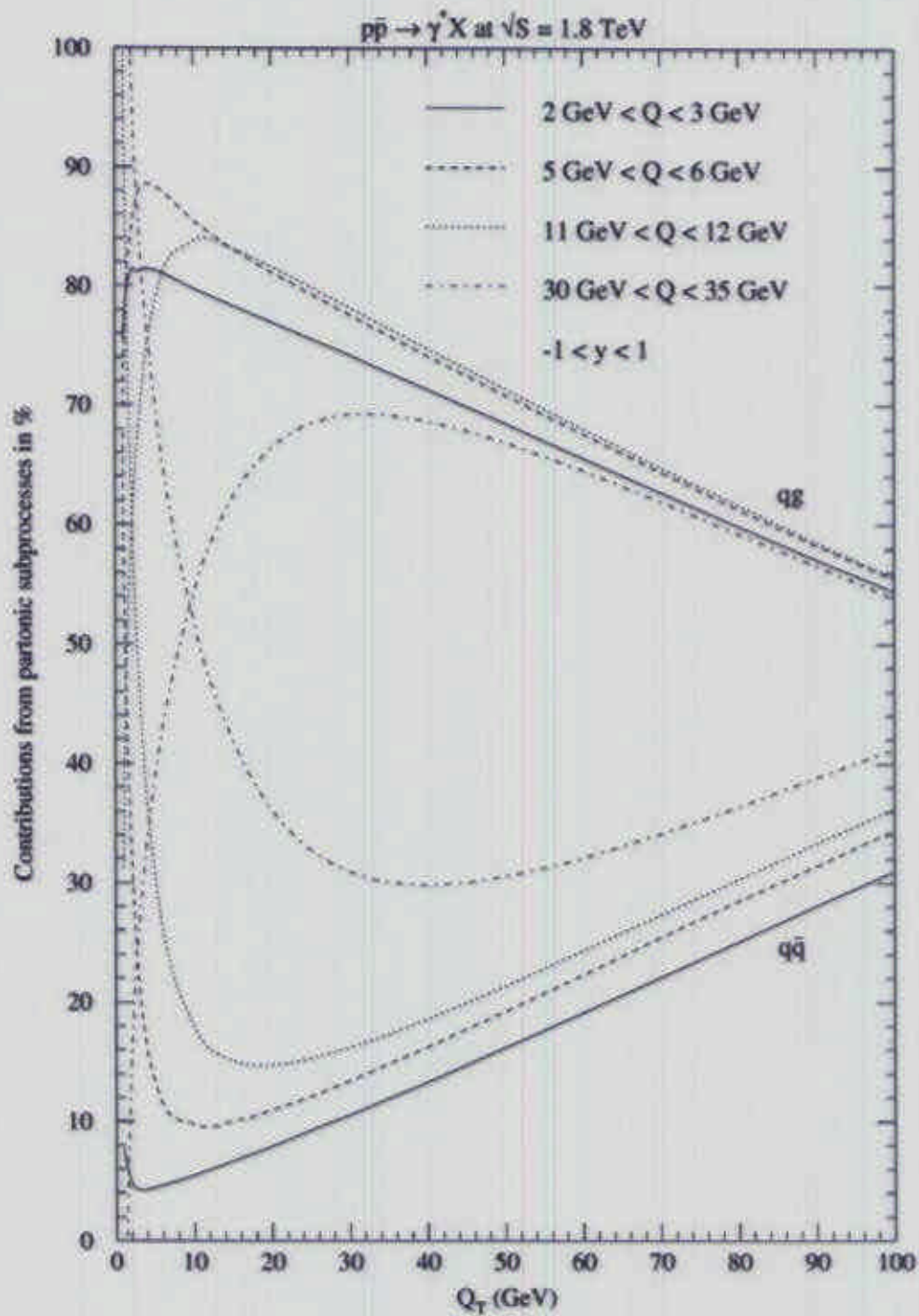


## CROSS SECTIONS AT COLLIDER ENERGIES



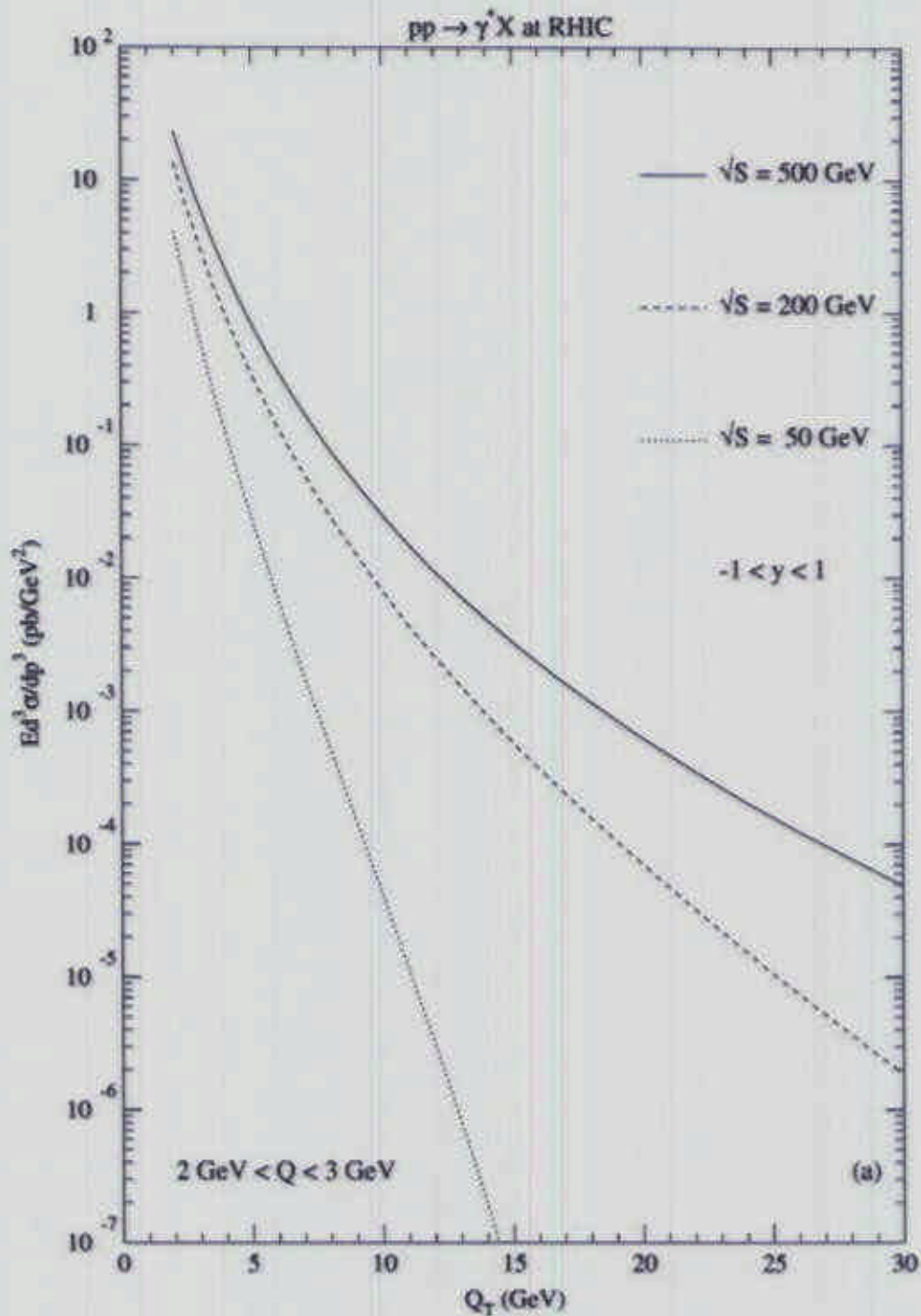
- Lepton pair production at the FNAL Tevatron collider
- “Drell-Yan factor” reduces cross section by factor of 400
- Cross section measurable to  $p_T = 30$  GeV,  $x_T = 0.03$
- Important to look at regions of low  $Q \simeq 2$  GeV,  $Q_T$  large

## CROSS SECTIONS AT COLLIDER ENERGIES



- $qg$  is most the important subprocess for  $Q_T > Q/2$
- Dominance of  $qg$  diminishes with  $Q$  from 80% to 70%
- At large  $Q_T$ , valence dominated  $\bar{q}$  density raises  $q\bar{q}$

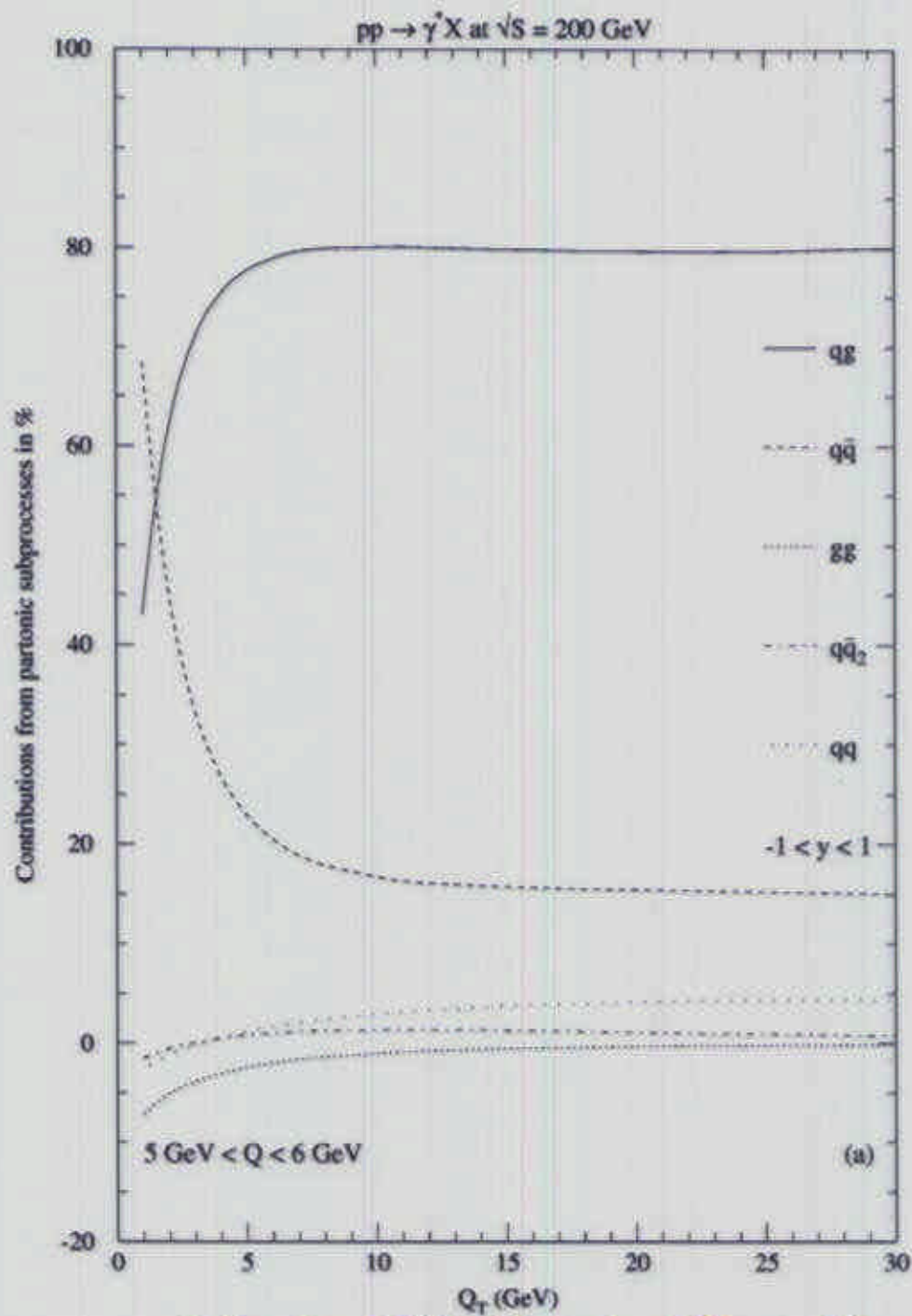
## CROSS SECTIONS AT COLLIDER ENERGIES



- Lepton pair production at different RHIC energies
- $qg$  dominates at the level of 80% for  $Q_T > Q/2$
- Cross section measurable to  $p_T = 7.5, 14, 18.5$  GeV,  
 $x_T = 0.3, 0.14, 0.075$  at  $\sqrt{S} = 50, 200, 500$  GeV

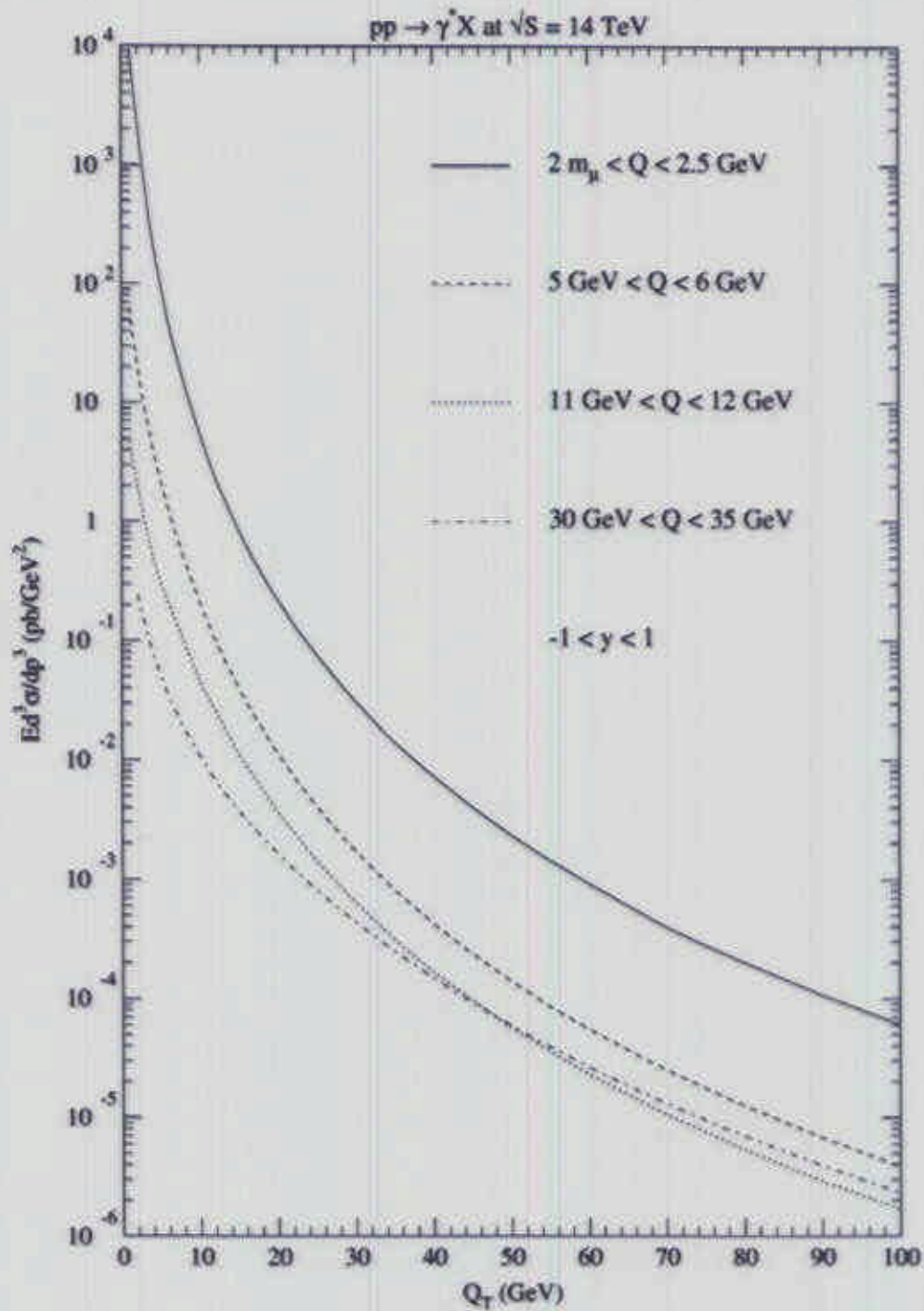


## CROSS SECTIONS AT COLLIDER ENERGIES



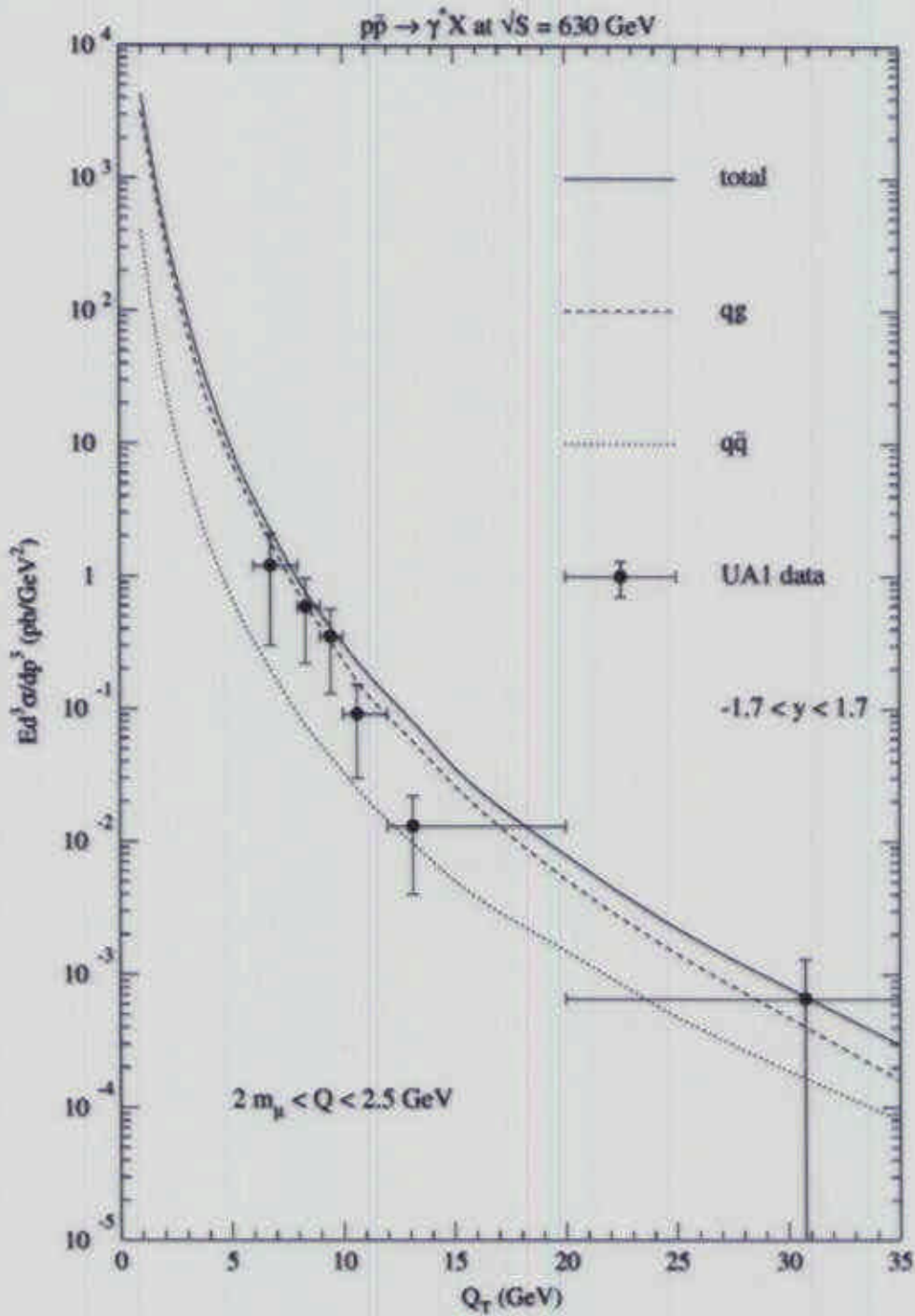
- $qg$  accounts for about 80% of the rate at  $Q_T \simeq Q$
- Subprocesses other than  $q\bar{q}$  and  $qg$  are negligible

## CROSS SECTIONS AT COLLIDER ENERGIES



- Lepton pair production at the CERN LHC collider
- $qg$  dominates at the level of 80% for  $Q_T > Q/2$
- Cross section is an order of magnitude larger than at Tevatron

### CROSS SECTIONS AT COLLIDER ENERGIES



- Lepton pair production at the CERN S $\bar{p}$ pS collider
- UA1 data prove feasibility of measuring low mass muon pairs
- $qg$  is most the important subprocess



## DIFFERENTIAL CROSS SECTIONS

### SENSITIVITY TO QUARK DENSITIES?

- $qg$  Compton subprocess is dominant, but will uncertainties in the quark density compromise the possibility to determine the gluon density?
- Recall (Berger and Qiu, Phys.Rev.D40, 778,(1989)):  
when the Compton subprocess is dominant
- spin-averaged cross section:

$$\frac{Ed^3\sigma_{h_1 h_2}^{ll}}{dp^3} \approx \int dx_1 dx_2 \left( \frac{F_2(x_1)}{x_1} G(x_2) \frac{Ed^3\hat{\sigma}_{qg}^{ll}}{dp^3} + (x_1 \leftrightarrow x_2) \right)$$

- spin-dependent cross section:

$$\frac{Ed^3\Delta\sigma_{h_1 h_2}^{ll}}{dp^3} \approx \int dx_1 dx_2 \left( 2g_1(x_1)\Delta G(x_2) \frac{Ed^3\Delta\hat{\sigma}_{qg}^{ll}}{dp^3} + (x_1 \leftrightarrow x_2) \right)$$

- $F_2(x, \mu_f^2)$  and  $g_1(x, \mu_f^2)$  are **measured** in spin-averaged and spin-dependent deep-inelastic lepton-proton scattering.
- Massive lepton-pairs at large enough  $Q_T$  will determine the gluon density provided the proton structure functions are measured well in deep-inelastic lepton-proton scattering.

## SUMMARY

- Current methods for determining the gluon density (prompt photon, high- $p_T$  jets) valuable but have limitations
- Lepton pair production dominated by  $qg$  for  $Q_T > Q/2$
- Advantages:
  - No non-perturbative fragmentation contribution
  - No need to isolate the photon experimentally
- Drawbacks: Lower cross section, limited range in  $x_T$
- Suggestions: Regions of low  $Q \simeq 2$  GeV, large bins in  $Q$
- Accessibility of  $g(x, \mu_f^2)$ 
  - Tevatron:  $p_T = 30$  GeV,  $x_T = 0.03$
  - RHIC:  $p_T = 7.5, 14, 18.5$  GeV,  
 $x_T = 0.3, 0.14, 0.075$  at  $\sqrt{S} = 50, 200, 500$  GeV
  - Fixed Target:  $p_T = 10$  GeV,  $x_T = 0.52$
- Asymmetries at RHIC: Accessibility of  $\Delta g(x, \mu_f^2)$ 
  - About same size as prompt photon production if  $Q_T \geq Q$
  - $A_{LL} = 20\%, 7.5\%, 3\%$  at  $\sqrt{S} = 50, 200, 500$  GeV
  - Independent of  $Q$  as long as  $Q_T$  is not too small
  - Depend strongly on parametrization of  $\Delta g(x, \mu_f^2)$